FOSSIL IMPRINT OF A POWERFUL FLARE AT THE GALACTIC CENTRE ALONG THE MAGELLANIC STREAM

J. Bland-Hawthorn1
Sydney Institute for Astronomy, School of Physics A28, University of Sydney, NSW 2006, Australia

Philip R. Maloney
CASA, University of Colorado, Boulder, CO 80309-0389, USA

Ralph S. Sutherland
Mount Stromlo Observatory, Australia National University, Woden, ACT 2611, Australia

G. J. Madsen
Institute of Astronomy, University of Cambridge, Madingley Rd, Cambridge, CB3 0HA, UK
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ABSTRACT

The Fermi satellite discovery of the gamma-ray emitting bubbles extending 50° (10 kpc) from the Galactic Centre has revitalized earlier claims that our Galaxy has undergone an explosive episode in the recent past. We now explore a new constraint on such activity. The Magellanic Stream is a clumpy gaseous structure free of stars trailing behind the Magellanic Clouds, passing over the South Galactic Pole (SGP) at a distance of at least 50–100 kpc from the Galactic Centre. Several groups have detected faint Hα emission along the Magellanic Stream (1.1 ± 0.3 × 10^{18} \text{ erg cm}^{-2} \text{ s}^{-1} \text{ arcsec}^{-2}) that is a factor of 5 too bright to have been produced by the Galactic stellar population. The brightest emission is confined to a cone with half angle θ_{1/2} = 25° roughly centred on the SGP. Time-dependent models of Stream clouds exposed to a flare in ionising photon flux show that the ionised gas must recombine and cool for a time interval T_{\alpha} = 0.6–2.9 \text{ Myr} for the emitted Hα surface brightness to drop to the observed level. A nuclear starburst is ruled out by the low star formation rates across the inner Galaxy, and the non-existence of starburst ionisation cones in external galaxies extending more than a few kiloparsecs. Sgr A* is a more likely candidate because it is two orders of magnitude more efficient at converting gas to UV radiation. The central black hole (M_\bullet \approx 4 \times 10^{6} M_\odot) can supply the required ionising luminosity with a fraction of the Eddington accretion rate (f_E \sim 0.03–0.3, depending on uncertain factors, e.g., Stream distance), typical of Seyfert galaxies. In support of nuclear activity, the Hα emission along the Stream has a polar angle dependence peaking close to the SGP. Moreover, it is now generally accepted that the Stream over the SGP must be further than the Magellanic Clouds. At the lower halo gas densities, shocks become too ineffective and are unlikely to give rise to a polar angle dependence in the Hα emission. Thus it is plausible that the Stream Hα emission arose from a ‘Seyfert flare’ that was active 1–3 Myr ago, consistent with the cosmic ray lifetime in the Fermi bubbles. Such a flare may have been causally linked to one of the episodes of massive star formation triggered in close proximity to Sgr A* within the last few Myr. Sgr A* activity today is greatly suppressed (70-80 dB) relative to the Seyfert outburst. The rapid change over a huge dynamic range in ionising luminosity argues for a compact UV source with an extremely efficient (presumably magneto-hydrodynamic) ‘drip line’ onto the accretion disk.

1. INTRODUCTION

Nuclear activity powered by a supermassive black hole is a remarkable phenomenon that allows galaxies to be observed to at least a redshift z ≈ 7 (e.g. Mortlock et al 2011). Evidence is beginning to emerge that our Galaxy has experienced possibly related episodes in the recent past. The proximity of the Galactic Centre provides us with an opportunity to study this activity in unprecedented detail.

The first evidence for a large-scale bipolar outflow came from extended bipolar ROSAT 1.5 keV X-ray and MSX 8.3μm mid-infrared emission observed to be associated with the Galactic Centre (Bland-Hawthorn & Cohen 2003). Two observations made clear that this activity must be associated with the centre of the Galaxy: (i) the bipolar structure is not visible in the diffuse ROSAT 0.2–0.5 keV data because the disk is optically thick at these energies; (ii) a hard X-ray bipolar counterpart has never been observed from a blow-out due to a young star cluster, thereby ruling out any association with a spiral arm along the line of sight. Further support for the large-scale wind picture comes from the kinematics of low-column halo clouds observed in absorption along quasar sight lines (Keeney et al 2006). In summary, the wind energetics are estimated to be roughly 10^{55} \text{ erg visible over 20°} (5 \text{ kpc in radius}).

In 2010, spectacular evidence for a powerful nuclear event came from Fermi gamma-ray satellite observations (1–100 GeV) of giant bipolar bubbles extending 50° (10 kpc) from the Galactic Centre (Su et al 2010). The source of the bubbles, whether related to starburst or AGN activity, remains hotly
The Magellanic Stream has detectable H$\alpha$ emission along the Galactic Pole (SGP) through photoionisation. Interestingly, UV bright sources that lit up the Magellanic Stream over the South Galactic Pole from the black hole accretion disk (Su et al 2010; Dobler et al 2010). In this scenario, the cosmic ray cooling times $t_{CR}$ are of order a few million years, suggesting powerful nuclear activity on a similar timescale. This picture implicates very fast nuclear winds with speeds of order $10^4$ km s$^{-1}$.

Guo & Mathews (2012) have recently challenged the wind picture on the grounds that the diffusion coefficient for cosmic rays advected in winds is much lower than required to explain the Fermi bubbles. Instead, they suggest the cosmic rays are carried by bipolar jets from an active galactic nucleus (AGN) which inflated the Fermi bubbles. Spectacular examples of this phenomenon do exist in nearby Seyfert galaxies (e.g. 0313-192; Keel et al 2006). Preliminary evidence for nuclear jets at the Galactic Centre has been discussed by several authors (Su & Finkbeiner 2012; Yusef-Zadeh et al 2012). In the Guo & Mathews model, the jets formed 1–3 Myr ago and endured for 0.1–0.5 Myr with a total energy in the range $10^{55}-57$ erg.

The supermassive black hole associated with the Galactic Centre source Sgr A* has a well established mass with 10% uncertainty ($M_*=4 \times 10^6 M_\odot$; Genzel et al 2003; Meyer et al 2012). At the present time, little is known about past nuclear activity. It is likely that the black hole was far more active before a redshift of unity when galactic accretion was at its peak. But even at the present epoch, there is good evidence for enhanced nuclear activity in interacting $L^*$ galaxies (q.v. Wild et al 2013; Rupke & Veilleux 2013). Direct evidence that the nuclear regions were much brighter in the past comes from ASCA 2–10 keV observations of circumnuclear clouds (Sunyaev et al 1993; Koyama et al 1996) with indications that Sgr A* was $10^5$ times more active within the past 10$^9$ years (q.v. Ponti et al 2010). More compelling evidence on much longer timescales comes from the existence of the Fermi bubbles.

We now show that if our Galaxy went through a Seyfert phase in the recent past, it could conceivably have been so UV bright that it lit up the Magellanic Stream over the South Galactic Pole (SGP) through photoionisation. Interestingly, the Magellanic Stream has detectable H$\alpha$ emission along its length that is at least 5 times more luminous than can be explained by UV escaping from the Galaxy (see §2). Ionisation cones have been observed in several dozen Seyfert galaxies to date. Arguably, the most spectacular example is the S0 galaxy NGC 5252 (Tadhunter & Tsvetanov 1989): orbiting gas streams up to 30 kpc in radius are lit up along bipolar cones due to the nuclear UV flux (Tsvetanov et al 1996). Kreimeyer & Veilleux (2013) have discovered ionisation cones in MR2251-178, a nearby quasar with a weak double-lobed radio source; non-thermal photoionisation is seen out to 90 kpc in radius emphasising the extraordinary reach of AGN activity to the present day.

In principle, the Stream H$\alpha$ emission could have been produced by a starburst event in the Galactic Centre, rather than by a Seyfert flare. However, as we discuss in Appendix B, the required star formation rate of such a starburst is at least two orders of magnitude larger than allowed by the star formation history of the Galactic Centre. An accretion flare from Sgr A* is a much more probable candidate for the ionisation source because (a) an accretion disk converts gas to ionising radiation with much greater efficiency than star formation, thus minimizing the fuelling requirements; (b) there is an abundance of material in the vicinity of Sgr A* to fuel such an outburst, and (c) a rapid decline in the ionising luminosity, needed in both starburst and AGN models to reconcile the present-day lack of activity with the magnitude of the required flare, is prohibitively difficult for starburst models but achievable (and interestingly challenging) for accretion disk models (cf. §5.1). Regardless of the true origin of the Stream’s H$\alpha$ emission, we show that its brightness is a powerful constraint on recent nuclear activity.

In §2, we describe basic properties of the Magellanic Stream and derive the levels of ionisation required to explain the observations. In §3, we carry out time-dependent ionisation calculations and relate to past AGN activity. We suggest follow-up observations in §4 and discuss the implications of our findings in §5. We conclude the paper with extended supplementary material on the gas physics, ionisation requirements and the ionisation spectrum in three appendices.

2. EXPERIMENT

Target. The Magellanic Stream (Fig. 1a) lies along a great arc that extends for more than 150$^\circ$ (Mathewson, Cleary & Murray 1974; Putman et al 2001; Nidever et al 2008). Fig. 1b illustrates the relationship of the LMC to the Magellanic Stream above the Galactic disk along a circular orbit originating from the Lagrangian point between the LMC and the SMC, at a Galactocentric distance of 55 kpc (Mathewson & Ford 1984). More recent simulations tend to suggest that the LMC-SMC system is infalling for the first time with an orbital period of order a Hubble time (Besla et al 2012; Nichols et al 2011). This implies substantial ellipticity of the orbit with the Stream distance over the SGP falling within the range 80–150 kpc (Model 1; Besla et al 2012). Given the uncertain mass of the Galactic halo (Kafle et al 2012), the drag coefficient of the Stream gas, and the initial orbit parameters of the Magellanic Clouds, the true distance along the SGP is unlikely to exceed 100 kpc (Jin & Lynden-Bell 2008).

The Magellanic Stream is made up of a series of dense gas clumps with column densities that vary over at least a factor of ten (Moore & Davis 1994; Putman et al 2001). Even the diffuse gas between the dense clouds is optically thick to the Lyman continuum (> 1.6 × 10$^{17}$ cm$^{-2}$). In the clouds, a mean column density of $N_\text{H} \sim 7 \times 10^{19}$ cm$^{-2}$ and a mean cloud size of $d_c \sim 1$ kpc leads to a total hydrogen density spanning the range $n_H \sim 0.03 - 0.2$ cm$^{-2}$. This leads to a typical spherical cloud mass of roughly $M_c \sim m_p N_c d_c^2/2 \sim 10^6 M_\odot$, for which $m_p$ is the proton mass. In reality, the gas may have a fractal distribution in density (Bland-Hawthorn et al 2007; Stanimirovic et al 2008; Nigra et al 2012). The mean metallicity of the Magellanic Stream appears to be everywhere one tenth of the solar value (Fox et al 2013) although isolated regions close to the Magellanic Clouds are more enriched (Richter et al 2013).

H$\alpha$ observations. Weiner & Williams (1996) made the remarkable discovery of relatively bright H$\alpha$ emission along the Magellanic Stream when compared to high-velocity clouds

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1 For a review of all estimates of $M_*$ to date, see Kormendy & Ho (2013).
Fig. 1.— (Top) HI column density map of the Magellanic Stream (adapted from Madsen 2012). The coordinates are in Magellanic longitude and latitude ($\ell_M, b_M$), as defined by Nidever et al (2008), and the asterisk indicates the SGP. The linear greyscale shows the column density of HI from the LAB survey (Kalberla et al. 2005), with the 21cm emission integrated over the velocity range of $-450$ km s$^{-1} < v_{LSR} < -100$ km s$^{-1}$. The location and 1$^\circ$ field of view of the new WHAM observations are shown as red and blue circles, corresponding to target and sky observations, respectively. The approximate longitudinal extents of the six Stream complexes (identified by Mathewson & Ford 1984) are shown on the top of the figure.

(Bottom) An illustration of the LMC and the dominant clouds in the Magellanic Stream (Mathewson & Ford 1984) projected onto the Galactic X-Z plane. The orbit of the Stream lies close to the great circle whose Galactic longitude is $\ell = 280^\circ$ (lhs of SGP) and $\ell = 100^\circ$ (rhs of SGP) shown as a dashed line. The blue fan illustrates the proposed ionisation cone from the Galactic Centre.

(HVC) close to the Galactic plane. These detections have been confirmed and extended through follow-up observations (Weiner et al 2002; Putman et al 2003; Madsen 2012) that are summarised in Fig. 2. The figure shows the H$\alpha$ surface brightness observations along the Stream as a function of Magellanic longitude $\ell_M$, where $\ell_M$ is defined in a plane that lies close to a great circle passing through the South Galactic Pole (Nidever 2008). Solid symbols show detections; open symbols show non-detections. In order to minimize the effects of bright, time-variable atmospheric emission lines, the data taken with the Wisconsin H-Alpha Mapper (WHAM) employed an offset sky subtraction technique (Madsen et al 2001). The high spectral resolution of the WHAM data enables us to confirm the association of the ionised gas with the cold Stream gas; the H$\alpha$ and HI velocities are consistent with each other to within $\approx 5$ km s$^{-1}$. The densities and length scales for the H$\alpha$ clouds derived above are within range of the expected values to account for the mean H$\alpha$ surface brightness. Furthermore, the beam size for most of the H$\alpha$ measurements (1$^\circ$ for WHAM) is of order the mean projected cloud size and thus provides an average estimate for the cloud. However, the origin of this emission remains highly uncertain.
Stream ionisation. We adopt physically motivated units that relate the ionising photon flux at a distant cloud to the resultant Hα emission. For this, we need to relate the plasma column emission rate to a photon surface brightness. In keeping with astronomical research on diffuse emission (e.g. WHAM survey – Reynolds et al 1998), we use the Rayleigh unit introduced by aeronomists (q.v. Baker & Romick 1976) which is a unique measure of photon intensity: 1 milliRayleigh (mR) is equivalent to 10^3/4π photons cm^{-2} s^{-1} sr^{-1}. The emission measure $E_m$ for a plasma with electron density $n_e$ is given by (e.g. Spitzer 1978)

$$E_m = \int f_i n_e^2 \, dz$$

which is an integral of H recombinations along the line of sight $z$ multiplied by a filling factor $f_i$. The suffix $i$ indicates that we are referring to the volume over which the gas is ionised. For a plasma at 10^4 K, $E_m$(Hα) = 1 cm^{-3} pc is equivalent to an Hα surface brightness of 330 milliRayleighs (mR). In cgs units, this is equivalent to 1.9 × 10^{-18} erg cm^{-2} s^{-1} arcsec^{-2} which would be a faint spectral feature in a 1 hr integration using a slit spectrograph on an 8m telescope. But for the Fabry-Perot ‘staring’ technique employed in Fig. 2, this is an easy detection if the diffuse emission uniformly fills the aperture. We refer to the Stream Hα emission as relatively bright because it is much brighter than expected for an optically thick cloud at a distance of 50 kpc or more from the Galactic Centre.

The characteristic Hα surface brightness observed along the Stream of $\mu_{H\alpha} \approx 160$ mR (Fig. 2) can be used to set a minimum required ionising photon flux and luminosity for a Galactic Centre flare, assuming that the Stream emission has not begun to fade and that there is no absorption or extinction of the ionising photon flux prior to reaching the Stream. For a slab ionized on one side, this is

$$\varphi_{i,\text{min}} \approx 3.9 \times 10^5 \text{ phot cm}^{-2} \text{ s}^{-1}$$

The implied ionising photon luminosities are then

$$N_{\nu,\text{min}} \approx (1.4 - 4.7) \times 10^{53} \text{ phot s}^{-1}$$

for $D = 55 - 100$ kpc. Any model in which the Stream emission is produced by a nuclear outburst must explain the magnitude of this ionising photon luminosity.

Expected emission via the Galactic stellar population. First we consider the expected emission due to the ionizing radiation from the Galactic stellar population and associated sources. The total flux at a frequency $\nu$ reaching an observer located at a distance $D$ is obtained from integrating the specific intensity $I_\nu$ over the surface of a disk, i.e.

$$F_\nu = \int \frac{I_\nu(n)(\mathbf{n},\mathbf{N}) \, dA}{D^2}$$

where $\mathbf{n}$ and $\mathbf{N}$ are the directions of the line of sight and the outward normal to the surface of the disk, respectively. At this stage, we consider only an isotropic illumination source rather than more complex forms of illumination with a strong polar angle dependence. In this instance, we use the more familiar scalar form of eq. (4) such that

$$\varphi_\nu = \int \frac{F_\nu}{h\nu} \cos \theta \, d\nu$$

where $\varphi_\nu$ is the photoionising flux from the stellar population, $\mathbf{n}, \mathbf{N} = \cos \theta$ and $h$ is Planck’s constant. This is integrated over frequency from the Lyman limit ($\nu = 13.6 \text{ eV}/h$) to infinity to convert to units of photon flux (phot cm^{-2} s^{-1}). The photon spectrum of the Galaxy is a complex time-averaged function of energy $N_\nu$ (photons per unit energy) such that $4\pi D^2 \varphi_\nu = \int_0^\infty N_\nu(E) \, dE$. For a given ionising luminosity, we can determine the expected Hα surface brightness at the distance of the Magellanic Stream. For an optically thick cloud ionised on one side, we relate the emission measure to the ionising photon flux using $E_m = 1.25 \times 10^{-6} \varphi_\nu$ cm^{-6} pc (Bland-Hawthorn & Maloney 1999). The total ionising luminosity of the Galaxy is now well established within a small factor (Bland-Hawthorn & Maloney 1999; Weiner et al 2002; Putman et al 2003). For a total disk star formation rate of 1.1 ± 0.4 M⊙ yr^{-1} (Robitaille & Whitney 2010), the hot young stars produce an integrated photon flux over the disk of $2.6 \times 10^{53}$ photon s^{-1} with very few photons beyond 50 eV.

The mean vertical opacity of the disk at the Lyman limit is $\tau_L = 2.8 \pm 0.4$, equivalent to a vertical escape fraction of $f_{\star,\text{esc}} \approx 6\%$ perpendicular to the disk ($\mathbf{n}, \mathbf{N} = 1$). The Galactic UV contribution at the distance $D$ of the Magellanic Stream is given by

$$\mu_{\star,\text{H}\alpha} = 21 \zeta \left( \frac{f_{\star,\text{esc}}}{0.06} \right) \left( \frac{D}{55 \text{ kpc}} \right)^{-2} \text{ mR}.$$  

corresponding to $\varphi_\nu \approx 5.1 \times 10^4$ phot s^{-1}. The correction factor $\zeta \approx 2$ is included to accommodate weakly constrained ionising contributions from the old stellar population, hot gas (disk+halo) and the Magellanic Clouds (Slavin et al 2000;
Nuclear spectrum. We now consider the Stream emission due to ionizing radiation powered by the supermassive black hole at the Galactic Centre. Motivated by detailed spectral observations of AGN, we adopt a two-component accretion-disk model for the photon spectrum of the central source. We define the specific photon luminosity for the two-component model by

\[ N_\text{*} = k_1 (E/E_1)^{2/3} e^{-E/E_1} + k_2 (E/E_2)^{-\alpha} e^{-E/E_2} \mathcal{H}(E-E_1) \text{ photon s}^{-1} \text{ eV}^{-1} \tag{7} \]

where \( \mathcal{H}(E-E_1) = 1 \) if \( E > E_1 \) and \( \mathcal{H}(E-E_1) = 0 \) otherwise. The first term on the rhs of eq. (7) represents the cool, optically thin Shakura-Sunyaev spectrum thought to produce the enhanced UV ("big blue bump") emission observed in Seyfert galaxies and quasars (Antonucci 1993). The second term represents the X-ray and gamma-ray emission observed from the source. We choose \( E_1 = 30 \text{ eV} \) for the cool outer blackbody spectrum, \( \alpha = 1.9 \) for the photon spectral index of the X-\( \gamma \) component (i.e., 0.9 for the energy spectral index), and adopt \( E_2 = 100 \text{ keV} \) (Dermer et al 1997).

By integrating eq. (7) weighted by energy, we derive the relative normalisation constants \( k_1 \) and \( k_2 \) (see Appendix C).

The ionising spectrum of NGC 1068 is strongly constrained by \( 2 - 200 \mu\text{m ISO-SWS} \) observations (Alexander et al 2000; Lutz et al 2000). This barred spiral galaxy has the most extensive literature of any Seyfert and serves as a surrogate for the AGN activity at the Galactic Centre. We have used the unattenuated spectrum to normalize our composite model. We find that \( \eta \approx 9 \) (log \( k_1/k_2 = 8.8663 \)) provides a reasonable match to NGC 1068. Our assumed ionising spectrum of the Galaxy's AGN presented in Fig. 3 has the same functional form.

The ionising flux \( \varphi_\text{*} \) follows from eq. (7) such that

\[ 4\pi D^2 \varphi_\text{*} = \int_{I_H=\text{flux}}^\infty N_\text{*}(E)\, dE \]  

for which \( I_H \) is the mass accretion rate. The accretion disk luminosity can limit the accretion rate through radiation pressure. The so-called Eddington limit is given by

\[ L_\text{E} = \frac{4\pi GM_\text{*}m_\text{p}c}{\sigma_T} \tag{9} \]

\[ = 1.4 \times 10^{11} \left( \frac{M_\text{*}}{4 \times 10^6 M_\odot} \right) L_\odot \tag{10} \]

where \( M_\text{*} \) is the black-hole mass and \( \sigma_T \) is the Thomson cross-section for electron scattering.

Radiation pressure from the accretion disk at the Galactic Centre limits the maximum accretion rate to \( \dot{m} \sim 0.2 M_\odot \text{ yr}^{-1} \). Some Seyferts, including NGC 1068 (Begelman & Bland-Hawthorn 1997), radiate at close to the limit. But active galactic nuclei appear to spend most of their lives operating at a fraction \( f_\text{E} \) of the Eddington limit with rare bursts arising from accretion events (Hopkins & Hernquist 2006). For clouds at a distance of 55–100 kpc along the SGP, we now show that only a fraction of the maximum accretion rate is needed to account for the H\text{\textalpha} emission along the Magellanic Stream. The orbital period of the Stream is of order a Hubble time so we can consider the Stream to be a stationary target relative to ionisation timescales.

The dust levels are very low in the Stream (Fox et al 2013); internal and line-of-sight extinctions are negligible. It follows from eq. (10) that the ionising photon luminosity of the Seyfert nucleus is given by

\[ N_\text{*} = 7.2 \times 10^{53} \left( \frac{f_\text{E}}{0.1} \right) \left( \frac{M_\text{*}}{4 \times 10^6 M_\odot} \right) \text{ photon s}^{-1} \tag{11} \]

For the photon spectrum in eq. (7), we find that 20% of the energy falls below the Lyman limit and therefore does not photoionise hydrogen. If the absorbing cloud is optically thick, the ionising flux can be related directly to an H\text{\textalpha} surface brightness.
brightness. The ionising flux is given by

$$\varphi_* = 2.0 \times 10^6 \left( \frac{f_E}{0.1} \right) \left( \frac{f_{\text{esc}}}{1.0} \right) \left( \frac{D}{55 \text{ kpc}} \right)^{-2} \text{ phot cm}^{-2} \text{ s}^{-1}. \quad (12)$$

We have included a term for the UV escape fraction from the AGN accretion disk $f_{\text{esc}} \left( n, N = 1 \right)$. This is likely to be of order unity to explain the integrated energy in observed ionisation cones (Sokolowski et al 1991; Mulchaey et al 1996). Some energy is lost due to Thomson scattering but this is known to be only a few percent in the best constrained sources (e.g. NGC 1068; Krolik & Begelman 1986). In principle, the high value of $f_{\text{esc}}$ can increase $f_{\text{esc}}$ but the stellar bulge is not expected to make more than a 10-20% contribution to the total stellar budget (Bland-Hawthorn & Maloney 2002); a possible contribution is accommodated by the factor $\zeta$ (eq. [6]).

The expected surface brightness for clouds that lie within a putative ‘ionisation cone’ from the Galactic Centre is given by

$$\mu_{\text{H} \alpha} = 825 b \left( \frac{f_E}{0.1} \right) \left( \frac{f_{\text{esc}}}{1.0} \right) \left( \frac{D}{55 \text{ kpc}} \right)^{-2} \text{ mR}. \quad (13)$$

Strictly speaking, this provides us with an upper limit or ‘peak brightness.’ In §3, we show that proper consideration must be given to the physical state of the gas and the time since the event occurred. The recombination emission will fade once the burst duration has passed and the gas begins to recombine and cool. For completeness, we have included a beaming factor $b$ to accommodate more exotic models that allow for mild beaming of the UV radiation (e.g. Acosta-Pulido et al 1990). The solid angle subtended by a half-opening angle of $\theta_{1/2}$ is $\Delta \Omega = 2\pi (1 - \cos \theta_{1/2})$. So the beam factor $b = (1 - \cos \theta_{1/2})^{-1}$ expresses how much of the isotropic radiation is channelled into a cone rather than $2\pi$ sr. For example, $\theta_{1/2} = 22.5^\circ$ is a beam factor $b = 13$; $\theta_{1/2} = 30^\circ$ is a beam factor $b = 7.5$; $\theta_{1/2} = 90^\circ$ is a beam factor $b = 1$ (isotropic emission) adopted for the remainder of the paper. The emission within an ionisation cone can be isotropic if the restriction is caused by an external screen, e.g. a dusty torus on scales much larger than the accretion disk.

3. PAST AGN ACTIVITY

3.1. Timescales

Consider the situation in which we observe the ionisation of the Stream due to a nuclear source. A burst of intense UV at a time $T_B$ in the past, lasting for a period $T_B$, must propagate for a time $T_C \sim 0.18 (D/55 \text{ kpc}) \text{ Myr}$ to reach the Stream. For example, in the Seyfert jet model of Guo & Mathews (2012), $T_B \approx 1 - 3 \text{ Myr}$ and $T_C \approx 0.1 - 0.5 \text{ Myr}$. The ionisation front then moves through the cool gas until the UV is used up. This occurs in a time $T_I \sim 1/(\sigma_H \varphi_*)$ where $\sigma_H$ is the H ionisation cross section. This follows from the fact that the speed of the ionisation front into the neutral gas is $v = \varphi_*/n_H$ where $v$ is the ionisation parameter$^2$ for a neutral H density $n_H$. For the $\text{H} \alpha$ emission levels associated with the Magellanic Stream, $T_I \sim 4 \times 10^5 / (\varphi_*/10^8)$ yr; for simplicity, the extra factors from eq. (12) are not carried over. The time for the gas to reach ionisation equilibrium will be of order $T_I$, and is very short compared to both $T_C$ and the likely values of $T_B$. The $\text{H} \alpha$ emission is then proportional to $\alpha_{\text{H} \alpha} N_e$, where $n_e$ is the electron density, $N_e$ is the column density of ionised gas, and $\alpha_{\text{H} \alpha}$ is the Case B recombination coefficient.

Since the level of activity in the Galactic Center today is far too low to produce the observed $\text{H} \alpha$ emission, the Stream emission in this picture is almost certainly fading from an earlier peak. The time $T_B$ required for the emission to decrease from its peak value to the observed brightness depends on both the time evolution of the burst luminosity and the gas density in the Stream$^3$. Since we observe the Stream as it was $T_C$ years ago, the look-back time to the initial event is $T_B = T_d + 2T_C$ (assuming the burst time $T_B$ is much less than $T_d$). We now revisit these approximations with detailed calculations of the ionisation state of the gas.

3.2. UV photoionisation

We use the recently completed MAPPINGS IV code (Dopita et al 2013) to study both isochoric and isobaric cooling at the surface of the Magellanic Stream. The source of the impinging radiation field is the accretion disk model presented in Fig. 3. The models were run by turning on the source of ionization, waiting for the gas to reach ionization/thermal equilibrium, and then by turning off the ionizing photon flux. In Figs. 4 and 5, we present our modelled trends in gas temperature ($T_J$), ionisation fraction ($\chi$) and emission measure ($E_m$) for time-dependent ionisation of the Magellanic stream. Important properties of the medium – ionised column depths, emission measures, cooling times, etc. – are included in Table 1. The sound crossing times of the warm ionised layers are too long ($\sim 10 \text{ Myr}$) in the low density regime relevant to our study for isobaric conditions to prevail. Both a near ($D = 55 \text{ kpc}$) and a far ($D = 100 \text{ kpc}$) distance is considered.

The gas phase abundances are the solar values scaled to [Fe/H] = -1 now well established from HST COS measurements (Fox et al 2013; Richter et al 2013). The upper limits for [OI]630 nm from the WHAM survey indicate that the ionisation fraction in the brightest $\text{H} \alpha$-emitting clouds exceeds $\chi \geq 50\%$ (Madsen et al 2013). For a spherical cloud, its mass is approximately $M_c \sim f_{\text{HI}} d_c^3 / 2$ where the subscript $n$ denotes that the filling factor refers to the neutral cloud prior to external ionisation. For a fixed cloud mass (or equivalently, cloud column density $N_c$), the filling factor is inversely related to the H I gas density. Any value other than unity leads to higher gas densities, and shorter recombination times. While the cloud geometry and the volume filling factor are uncertain (Fox et al 2010), self-consistent ionisation parameters $q$ are obtained at all times and lie within the range $\log q \approx 5.6 - 7.6$ ($\log u \approx -5$ to -3).

In Fig. 5, the initial photoionising flash rapidly heats the gas to a peak temperature before the gas begins recombining at a rate that is inversely proportional to $n_H$ as expected (§2). We observe that the recombination rate is faster than the cooling rate during this period. The initial flash produces high ionisation states (e.g. He II, [O III] emission lines) but these fade rapidly. In Fig. 4, the increase in electron density leads to a maximum $\text{H} \alpha$ brightness which then also fades. The Balmer decrement $H_o/\beta$ is everywhere in the range 3.0 – 3.1 until very late times when it begins to climb, except now the flare ionisation signal has almost faded from view. While the decrement is sensitive to dust extinction, the low metallicity of the Stream has negligible impact on this diagnostic (see §5).

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$^2$ This is often defined as the dimensionless ionisation parameter $u = q/c$.

$^3$ This is discussed in detail in §5.1 and Appendix A.
Fig. 4.—MAPPINGS IV time-dependent isochoric calculations of the change in Hα surface brightness after a Seyfert flare has occurred at the Galactic Centre. (Left) D = 55 kpc, $f_E = 0.1$; (Right) D = 100 kpc, $f_E = 0.1$. From left to right, the pre-ionised gas densities are 1.0, 0.3, 0.1, 0.03, 0.01 cm$^{-3}$. The clouds have 0.1 $Z_\odot$ metallicity and are irradiated by an AGN accretion disk (see text). The mean surface brightness of the Stream near the SGP (160 mR) is shown as a horizontal dashed line. Physical properties of the models are to be found in Table 1.

Fig. 5.—MAPPINGS IV time-dependent calculations of how the ionised surface of a dense gas clouds cools with time: (Left) electron temperature $T_e$; (Right) ionisation fraction $\chi$. We show the isochoric (constant density) models where the densities in cm$^{-3}$ are indicated; isobaric models cool twice as fast at late times. The H$_1$ clouds have 0.1 $Z_\odot$ metallicity and are irradiated at $D = 55$ kpc by an AGN accretion disk ($f_E = 0.1$) at the Galactic Centre (Fig. 3).

At late times, the Hα surface brightness in all cases scales as $t^{-2}$; see Appendix A.

In Table 1, we show key properties of the models as a function of the pre-ionisation gas densities. The realistic cases are shown as emboldened values where we have ignored small factor uncertainties; the remaining models exceed the properties (either local or column density) of the Stream clouds. Column 5 shows the times $T_d$ for the emission to drop to the canonical surface brightness of 160 mR (see Fig. 2). The look-back times are shown in Column 6; note that the light propagation time ($2T_C$) dominates the high density extremes. These timescales are in line with published models of the Fermi bubbles (§1). The lower ionising flux at the 100 kpc distance (since the peak luminosity in the models is fixed) leads to shorter look-back times because the gas requires less time to reach 160 mR.

**Distance vs. Flare Luminosity.** It is clear from Fig. 4 that lower ionising fluxes or larger Stream distances lead to shorter inferred timescales for the Seyfert flare event. To within a small factor, the ionisation model $(D, f_E) = (55 \text{ kpc}, 0.1)$ is equivalent to the $(100 \text{ kpc}, 0.3)$ model once all timescales are considered. Conversely, the ionisation model $(D, f_E) = (100 \text{ kpc}, 0.1)$ is equivalent to the $(55 \text{ kpc}, 0.03)$ model. In Appendix A, we present a simplified model for the evolution of the ionisation fraction and Hα surface brightness from the Stream which is in good agreement with the MAPPINGS models shown in Fig. 4, which we use to discuss in more detail the constraints that can be placed on the flare energetics and evolution in §5.1.

**Variations in Hα brightness.** An attractive aspect of the Seyfert flare model is the ability to accommodate the brightest Hα measurements and the scatter about the elevated mean surface brightness (160 mR) compared to the expective Galactic ionisation level. An interesting question is whether the scatter...
reflects variations in gas density (geometry) or photon arrival time (finite $T_R$). In Fig. 6, we show the relation between $\mu_\alpha$ and $n_H$ at a fixed time over a range of times from 0.5 Myr to 5 Myr. For an impulsive burst, it is possible to accommodate all of the detections at a fixed time, certainly within the first few Myr of the Seyfert event. But the very short ionisation timescale $T_I$ (§3.1) means that we are unlikely to see temporal variations of the source: the Stream emission is unaffected by any variations in incident ionising flux that occurred longer than $\sim T_I$ ago. Source luminosity variations on longer timescales will be modulated by a transfer function that depends on the gas density (see Appendix A); any observable fluctuations in $H\alpha$ are likely the result of variations in density and hence recombination timescale. The most relevant epoch in interpreting the Stream emission is the end of the flare.

From the last column in Table 1, we conclude that a powerful flare event occurred 1–3 Myr ago. The inferred magnitude of the event depends on a number of factors, in particular, the poorly constrained distance to the Magellanic Stream (see §5 and Appendix A), but it must have been at levels associated with the most energetic Seyfert activity ($f_E > 0.01$).

4. FUTURE TESTS OF THE MODEL

In Seyferts with moderately low mass black holes, the jet/wind/cone axis can be strongly misaligned with the spin axis of the galaxy (Cecil 1988; Mulchaey et al 1996) but there are many counter examples (Duric et al 1983; Wehrle & Morris 1987, 1988; Keel et al 2006). The Fermi bubbles and the X-ray bipolar structure are roughly aligned with the SGP. These features fill most of the conic volume in our model within 10 kpc, and presumably the outflow has swept any halo gas aside. We assume that the ionisation cone in the Seyfert flare model is also aligned with the SGP ($\ell_M \approx 303^\circ$). Thus to account for the brightest clouds in the Stream (Fig. 2), the half-opening angle $\theta_{1/2}$ of the cone is at least 25° to accommodate enhanced emission at the same angle from the SGP ($\ell_M \approx 278^\circ$).

Any gas clouds caught within the cones at smaller distances will be roasty by the Seyfert nucleus. However, almost all the known high velocity clouds reside close to the Galactic Plane ($b < 30^\circ$; Putman et al 2012). There are few known HVCs close to the SGP although evidence for ionised HVCs has been presented (Lehner & Howk 2010). In our model, most of the HVCs will be fully ionised within the ionisation cone. Interestingly, there is one sight line close to $\ell_M = 308^\circ$ where the $H\alpha$ surface brightness is up to 4 times higher than our benchmark flare value of 160 mR (Fig. 2). A possible explanation is that some of the Stream clouds are somewhat closer than the canonical distance of 55 kpc.

A competing model for the $H\alpha$ emission uses a radiative hydrodynamic simulation to demonstrate the possibility of a slow shock cascade acting along the Stream (Bland-Hawthorn et al 2007). Arguably, this is the only serious attempt to date to explain the Stream $H\alpha$ emission. But this model does not work well if the Stream at the SGP is at the larger distance of $D \approx 100$ kpc. Given that one end (front) of the Stream is tied to the LMC-SMC system, this would require the far trailing end (back) of the Stream to subtend a large angle to the halo, being more radial than tangential to the halo. This has two problems: (i) the $H\alpha$ emission would be almost entirely confined to the front of the Stream; (ii) the back of the Stream would be undetectable.

For the near distance of $D = 55$ kpc, for most optical diagnostics, the slow shock cascade may be difficult to disentangle or distinguish from our model of AGN photoionisation. The diluteness of the predicted AGN field, with ionisation parameters in the range $\log q = 5.6 - 7.6$ ($\log u \approx -5$ to -3), tends to produce shock-like emission line diagnostics. The high energy part of the big blue bump ($50 - 100$ eV) can excite He$^+$ and [O iii], with enhanced ratios to H$\beta$ of about 0.3 and 1 respectively. But these occur at the peak of the flash and fade rapidly, and only for the near-field Stream (Fig. 4a). The high

### Table 1

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<th>$n_H$ (cm$^{-3}$)</th>
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<th>$\mu_{H\alpha}$ (cgs)</th>
<th>$\mu_{H\alpha}$ (mR)</th>
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(b) 100 kpc

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energy tail in eq. (7) can excite a few atoms with high ionization cross sections but the radiation field in X-rays is very dilute, and the metal fraction is low ([Fe/H] ≈ -1; Fox et al. 2013).

We are presently re-running the shock cascade models at higher resolution and with the updated ionisation diagnostics in MAPPINGS IV. This will be the focus of a later paper. The shock cascade has a slightly elevated density-weighted temperature ($T_e \gtrsim 12,000$ K) compared to the time-averaged Seyfert flare model ($T_e \approx 10,000$ K). But both models produce comparable emission in the optical diagnostic [S ii], [N ii] and [O i] emission lines.

A promising diagnostic is the Balmer decrement Hα/Hβ which is typically enhanced in slow shock models (Bland-Hawthorn et al. 2007). The dust content in the Magellanic Stream has negligible impact on this line ratio. Diffuse optical detection surveys to date have largely focussed on the 500–700 nm window in part because Hβ is harder to detect along most of the Stream (Reynolds et al. 1998). In our Seyfert flare models, the Balmer decrement at the distance of the Stream has negligible impact on this line ratio. Diffuse optical detection surveys to date have largely focussed on the 500–700 nm window in part because Hβ is harder to detect along most of the Stream (Reynolds et al. 1998). In our Seyfert flare models, the Balmer decrement at the distance of the Stream is in the range 3.0–3.1 for detectable emission, rising slowly at late times when the recombination emission has largely faded. In the shock cascade model, the Balmer decrement exceeds 3.1 and can reach values that are 50% higher.

5. NEW INSIGHTS ON AGN ACTIVITY

5.1. Accretion disk

Sgr A* provides us with a front-row seat on the daily life of a supermassive black hole4. Nuclear activity today at the Galactic Centre is remarkably quiescent given the rich supply of unstable gas within the circumnuclear disk (Requena-Torres et al. 2012). This observation has driven the rapid development of accretion disk models over the past twenty years: a comprehensive review is given by Genzel et al. (2010). It is now believed that Sgr A* is a radiatively inefficient accretion flow (RIAF) fuelled by poor angular momentum transport at all radii in part due to strong outflows, magnetic fields and convection in the innermost accretion zone (Blandford & Begelman 1999; Hawley & Balbus 2002; cf. Jolley & Kuncic 2008).

The observed material within a few parsecs of Sgr A* can readily account for the 0.02–0.2 Mʘ yr⁻¹ accretion rate required in our model. Stellar accretion events are expected once every 40,000 years on average (Freitag et al. 2006). There are indications of infalling gas clouds over the past 10 Myr. One such cloud impact possibly triggered the formation of a kinematically distinct ~ 10⁴ Mʘ cluster within ~ 0.1 pc of Sgr A*, traced by ~ 80 massive young stars with ages in the range 2.5–8 Myr (Paumard et al. 2006; Lu et al. 2013). Wardle & Yusef-Zadeh (2008) draw attention to the “~50 km s⁻¹ cloud” known to have passed through the Galactic Center within the last 1 Myr. These events bracket our inferred epoch for the Seyfert flare which may have been causally linked to one of these or a related event.

We do not know what the peak luminosity of the AGN burst was, or the timescale on which it decayed. Such information would shed light on the nature of the accretion event, whether an individual star ($T_B \sim 10^{3–3}$ yr) or an infalling cloud on much longer timescales. However, we can use the simplified model for the Stream emission developed in Appendix A, which is in good agreement with the detailed MAPPINGS IV results for the time-dependent Hα surface brightness, to place constraints on these quantities.

As in Appendix A, define $\rho$ to be the ratio of the observed $\mu_{160}$ to its peak value. This is also equal to the ratio of the minimum required ionizing flux (eq. [2]) or ionizing luminosity (eq. [3]), to their peak values, as well as the minimum required value of the Eddington fraction $f_{E,\text{min}}$ to its peak during the burst. Using eq. (2) and eq. (12) for the ionizing flux from the AGN (with $f_{E,\text{esc}}$ set to 1), we can write this minimum Eddington fraction as

$$f_{E,\text{min}} = 0.02 \left( \frac{D}{55 \text{ kpc}} \right)^2$$

(14)

In the limit where the e-folding time for decay of the burst $\tau_e$ is much shorter than the recombination timescale $\tau_{\text{rec}}$, we have the analytic result

$$f_{E,\text{peak}} = f_{E,\text{min}} (1 + \tau_e)^2$$

(15)

where $\tau_e$ is the dimensionless age of the burst as measured in recombination times. (This is simply another form of eq. [A23]). Using eq. (A9) for $\tau_{\text{rec}}$ and eq. (14) for $f_{E,\text{min}}$, we have calculated the required peak value of $f_E$ as a function of gas density $n_H$ and burst age $T_B$, for both $D = 55$ kpc and 100 kpc. Assumining that the present-day Eddington fraction of Sgr A* is ~ 10⁻⁸ (Genzel et al. 2010), we can also calculate the required value of the e-folding time $\tau_e$; the inferred value of peak $f_E$ at a given $T_B$ determines the number of e-folding times that have passed in the age of the burst.

The results are shown in Fig. 7. The grey upper right portion of the diagrams is where $f_{E,\text{peak}}$ exceeds 1; this occurs sooner at higher $n_H$ (more recombination times) and larger $T_B$ (more e-folding times $\tau_e$). This condition is violated more readily for $D = 100$ kpc, since a greater $\varphi_I$ is needed to produce the same Hα surface brightness; this also means the minimum allowed value of $f_E$ is ~ 3.3 times larger. However, a broad range of reasonable $f_E$ is allowed for burst ages greater than ~ 1 Myr in both cases; a larger Distance disk favors lower $n_H$ (to increase $\tau_{\text{rec}}$) and larger $f_{E,\text{peak}}$.

Although we have assumed that $\tau_e \rightarrow 0$ in Fig. 7, the results are not very sensitive to this assumption: in Appendix A, we show that $\tau_{\text{rec}}/\tau_e$ is likely to be a factor of order a few; for these values, there are modest shifts of the curves from the instantaneous decline case (see Fig. 10 in Appendix A).

In our interpretation, Sgr A* was far more active in the past. Rapid and stochastic variations in AGN activity are to be expected (Novak et al. 2011, 2012). Depending on the Stream distance, for plausible $n_H$ and $T_B$, the required Eddington fraction $f_E$ is of order 0.03–0.3 which is a factor of 10⁻⁸–times higher than the quiescent state today.5 The most extreme event witnessed in models by Novak et al (2011, their Fig. 6) is a transition from $f_E \sim 10^{-3}$ to $f_E \sim 3 \times 10^{-8}$ in a few Myr (45 dB). This happens when there is a lot of material in the accretion disk around the black hole. The AGN heats up the ISM and terminates additional infall, and then the mass drains out of the disk with an e-folding time of about 0.1 Myr.

5 While such an event would be spectacular to behold using modern astronomical techniques, to an ancient observer, escaping shafts of light that managed to pierce through the heavy dust obscuration towards Earth would have been at least an order of magnitude fainter than the full moon.

4 http://swift-sgra.com provides regular updates on energetic episodes at the Galactic Centre. At the time of writing, much interest has been sparked by the anticipated “G2 cloud” collision – a warm cloud of several Earth masses – expected to occur in 2014 (Gillessen et al. 2013).
Fig. 7.— The constraints on the Sgr A* burst peak Eddington fraction $f_{E, \text{peak}}$ (blue contours) and burst decay $\tau_e$-folding time (magenta contours) as a function of Stream gas density $n_H$ and burst age $T_0$, for the case of very rapid burst decline. The grayed-out region requires $f_{E, \text{peak}} > 1$. (Left): $D = 55$ kpc. (Right): $D = 100$ kpc.

The timescale of the drop is roughly the characteristic time to clear the accretion disk (G. Novak, private communication).

But our new result demands 70-80 dB suppression within a time frame of only $\sim 1-5$ Myr. Such a rapid variation requires an extremely efficient and well confined ‘drip line’ to prevent the fresh gas from being sheared by the accretion disk which would wash out extreme fluctuations in UV luminosity (S. Balbus, private communication). Magnetic fields – required to mediate angular momentum transport – are expected to thread through a RIAF disk and these are almost certainly needed to achieve the severe confinement and rapid fuelling.

In time, we may learn about the detailed structure of the evolving accretion disk before, during and after a major outburst (Ho 2008). If the Seyfert flare model is ultimately confirmed to be the correct explanation for the Stream’s partial ionisation, it provides us with a very interesting and spatially resolved probe of the escaping radiation. We refrain from considering more sophisticated accretion disk/jet models, with their attendant beaming, until more progress is made in establishing the true source of the ionising radiation and the Stream’s trajectory. A stronger case must be made for preferring this model over another (i.e. the shock cascade). But we note that the green horizontal line in Fig. 2 is not a good fit to most of the data points. An inverted low amplitude parabola centred on the SGP does better. This can be understood in terms of an accretion disk radiation field with a polar angle component; such models have been presented (e.g. Madau 1988; Sim et al 2010). But the trend to lower Magellanic longitude can also be explained if the Stream subtends a large angle to the Galactic halo.

5.2. UV line-driven wind

It is evident that the explosive nuclear activity that created the extended X-ray, microwave and gamma-ray radiation gave rise to a large-scale outflow from the Galactic Centre. Both starburst and AGN activity are likely to be operating from the central regions. While their time-averaged energetic outputs may be similar, they operate with very different duty cycles and temporal behaviour (Alexander & Hickox 2012). The Fermi observations have been discussed extensively in the context of accretion disk activity associated with the well established supermassive black hole (Su et al 2010; Guo & Mathews 2012) although alternative starburst models have been presented (Carretti et al 2013). Starbursts drive large-scale winds very effectively and may assist with the observed bipolar activity. But as already mentioned (§1; see also Appendix B), starburst activity cannot account for the Stream Hα emission.

Is it possible to associate the powerful radiative phase with the wind phase? Regrettably, there are few published accretion disk models that provide both the ionising luminosity and mechanical luminosity of the central source. For our discussion, we use the well prescribed models of Proga & Kallman (2004; hereafter P-K) that build on their earlier work (Proga, Stone & Kallman 2000).

In the P-K wind models, the relatively high radiation UV flux and opacity (mainly due to line transitions) supply a strong radiative force that is able to lift gas over the photosphere. This gas provides significant column density to block the X-rays otherwise the wind becomes overionised and the flow switches off. The line-driven wind is launched from the part of the disk where most of the UV is emitted. In effect, the inner disk wind shields the outer wind. The high value of $\eta$ in eq. (7) is consistent with our assumption that the UV radiation dominates over X-rays and powers the large-scale wind (Proga, Stone & Kallman 2000).

The P-K wind reaches velocities roughly twice the escape velocity from the launching region. So this gives velocities of about $10,000$ km s$^{-1}$ for a system with $M_\ast = 10^8 M_\odot$, although maybe somewhat less for the supermassive black hole associated with the Galactic Centre. With this velocity it will take only 0.1 Myr to reach a distance of 1 kpc, and 1 Myr to reach 10 kpc. The disk wind mass loss rate is roughly 10% or so of the disk accretion rate and therefore does not cause a signif-
icant reduction of the accretion rate. The wind is unlikely to ionise cold gas at the distance of the Stream.

Using the Proga models, Sim et al (2010) computed spectral energy distributions as a function of viewing angle as seen from the accretion disk. They compute the ionisation and excitation structure of the wind and track multiple scattering of the photons. The polar radiation field depends on photon energy and the escaping radiation is confined to a cone. The X-ray and the UV radiation come from different directions; the former propagate parallel to the UV photosphere whereas the latter is normal to it. Therefore the column density for the X-rays is much higher than for the UV as expected, although some leakage is observed.

We observe that something like this may be happening in detailed observations of nearby active galaxies. In an integral field study of ten galactic winds, Sharp & Bland-Hawthorn (2010) compared five starbursts and five AGNs. The AGN winds show clear evidence for non-thermal ionisation from the central source across the wind filaments to the radial limits of the data. But AGN ionisation cones are not always associated with winds. For example, the most famous of the Seyfert ionisation cones is NGC 5252 (Tadhunter & Tsvetanov 1989) which is not associated with an energetic outflow. In the context of the P-K model, we associate these cones with AGNs where strong X-rays escape from the nuclear which serve to suppress the line-driven wind. This distinction may become less clear cut if more powerful line-driven winds (presumably from more massive black holes) are able to drive shocks in the gas along the ionisation cone. Thus ionisation cones may be detectable in X-rays even while the central source irradiates the cone exclusively with UV. Shocked gas tends to radiate at a higher temperature compared to photoionised gas, and this may allow these cases to be separated.

Line-driven winds struggle with black hole masses as low as that associated with Sgr A* unless the accretion rate is close to the Eddington limit. If the Stream ionisation is due to a burst of radiation from a P-K disk, then \( f_\alpha \sim 1 \) is an order of magnitude more than is need to account for the observed H\( \alpha \) emission for the canonical Stream distance (55 kpc), although it would aid ionisation of the Stream at the larger distance. In principle, \( f_{\alpha, ESC} \) could be lower than our assumed value of 100%. But the high limit is consistent with what we know about ionisation cones (e.g. Mulchaey et al 1996) and is a consequence of the P-K wind model where the wind has cleared a channel for the UV emission (Proga & Kallman 2004; Sim et al 2010).

6. CONCLUSIONS

We have shown how the Magellanic Stream is lit up in optical emission lines at a level that cannot be explained by disk or halo sources. A possible explanation is a shock cascade caused by the break-up of clouds and internal collisions along the Stream (Bland-Hawthorn et al 2007) but this becomes untenable if the Stream is much further than the canonical distance of 55 kpc.

We have introduced time-dependent ionisation calculations with MAPPINGS IV for the first time in order to present a promising Seyfert flare model that adequately explains the observed photoionisation levels along the Magellanic Stream. The model works at both the near and far Stream distances, and can be tested in future observations. A ‘slow shock cascade’ is expected to produce a steeper Balmer decrement (H\( \alpha \)/H\( \beta \) > 3.1) than the flare model. Since the Magellanic Stream has a very low dust fraction ([Fe/H] \( \approx \) -1), this is likely to be the most accessible discriminant between the models. Other useful diagnostics (He\( \Pi \)/H\( \beta \), [O\( \Pi \)]/H\( \beta \)) reach peak values shortly after the Seyfert flash but fade rapidly.

We cannot yet identify the specific event which triggered the burst of Seyfert activity although the stellar record tells us the last 10 Myr have been very active (Ponti et al 2013). The time lag between an accretion event and the onset of starburst or AGN activity (or how these operate together) is a major unsolved problem in astrophysics. The inner tens of parsecs provide many possible cloud candidates, assuming it was not largely consumed, many on highly elliptic orbits. If our model is correct, it provides many new challenges for the burgeoning field of Galactic Centre research. Regardless of the origin of the emission, the Stream provides an important constraint on past AGN activity and on models that attempt to explain the Fermi gamma-ray bubbles.

7. ACKNOWLEDGMENT

This work came about during the April 2013 “Fermi Bubbles” workshop held at KIPAC Stanford organised by Dmitry Malyshev and Anna Frankowiac. We acknowledge insightful conversations with Steve Balbus, Bill Mathews, Daniel Proga, Greg Novak, Bruce Draine and Kyler Kuehn. JBH is indebted to James Binney for early comments on the manuscript. We are particularly grateful to Roger Blandford and the participants of the Kavli workshop without whom this paper may not have been realised. We thank the referee for suggestions that led to more detailed discussions in the appendix.
A. SIMPLE MODEL FOR TIME-DEPENDENT EVOLUTION OF THE IONISATION FRACTION AND H\textsc{\textalpha} SURFACE BRIGHTNESS

Consider the following simple model for the Stream clouds: a uniform density gas of pure hydrogen, with a photon flux $\varphi_i$ normally incident upon it. If the gas has been exposed to the ionising photons for long enough to reach ionisation equilibrium, then all of the photons will be absorbed in a length $L$ given by

$$\alpha n_H^2 L = \varphi_i$$  \hspace{1cm} (A1)

where $\alpha$ is the recombination coefficient. This is just the condition that the column recombination rate equals the incident flux. Thus

$$L = \frac{\varphi_i}{\alpha n_H^2}$$  \hspace{1cm} (A2)

To simplify even further, assume that for depth $d < L$ into the Stream gas, the gas is completely ionised, while for $d > L$, it is neutral. Hence all the emission measure comes from $d < L$, and we will also ignore any effects of absorption on $\varphi_i$, so the region with $d < L$ can be treated as uniform.

Now suppose that the ionisation rate decreases from the initial value for which the equilibrium was established. Without loss of generality, we can assume an exponential decline for $\varphi_i$, with a characteristic timescale for the ionising source $\tau_s$ (Sharp & Bland-Hawthorn 2010). The time-dependent equation for the electron fraction $x_e = n_e/n_H$ is

$$\frac{dx_e}{dt} = -\alpha n_H x_e^2 + \zeta x_e + \zeta$$

$$= -\alpha n_H x_e^2 + \zeta_0 e^{-t/\tau_s} (1 - x_e)$$  \hspace{1cm} (A3)

where $\zeta$ is the ionisation rate per atom.

Consider first the case where $\tau_s \rightarrow 0$, so that $\varphi_i$ declines instantaneously to zero. Then the second and third terms in eq. (A3) vanish, and we just have

$$\frac{dx_e}{dt} = -\alpha n_H x_e^2$$  \hspace{1cm} (A4)

This is easily solved with the substitution $u = x_e^{-1}$, and with the initial condition $x_e = 1$ at $t = 0$ we get

$$x_e = \frac{1}{1 + \alpha n_H t}$$  \hspace{1cm} (A5)

Defining the recombination timescale

$$\tau_{rec} = 1/\alpha n_H$$  \hspace{1cm} (A6)

this is simply

$$x_e = (1 + t/\tau_{rec})^{-1}$$  \hspace{1cm} (A7)

To evaluate eq. (A7) for the conditions in the Stream, we use $\alpha_H = 2.6 \times 10^{-13}$ cm$^3$ s$^{-1}$ for the recombination coefficient (appropriate for hydrogen at $10^4$ K), and use the fiducial values $\varphi_i = 10^6 \varphi_0$ phot s$^{-1}$, $n_H = 0.1 n_{-1}$ cm$^{-3}$. Then

$$L = 125 \frac{\varphi_0}{n_{-1}} \text{pc}$$  \hspace{1cm} (A8)

$$\tau_{rec} = 1.2 \times 10^{6}/n_{-1} \text{yr}$$  \hspace{1cm} (A9)

and the emission measure

$$E_m = L n_e^2 x_e^2 = 1.25 \varphi_0 x_e^2(t) \text{cm}^{-6} \text{pc}$$  \hspace{1cm} (A10)

so the gas density enters explicitly only through the recombination time. The resulting H\textsc{\textalpha} emission will be

$$\mu_{H\alpha} = 413 \varphi_0 x_e^2(t) \text{ mR}$$  \hspace{1cm} (A11)

or, with eq. (A7)

$$\mu_{H\alpha} = 413 \varphi_0 (1 + t/\tau_{rec})^{-2} \text{ mR}$$  \hspace{1cm} (A12)

In the lefthand panel of Fig. 8, we plot the prediction of eq. (A12) for the H\textsc{\textalpha} surface brightness as a function of time for $\varphi_0 = 2$, as used in eqs. (10) and (11) for $D = 55$ kpc. Comparison with the left-hand panel of Fig. 4 shows that this simple model agrees well with the detailed MAPPINGS results, except for the highest densities. The discrepancy is largely because eq. (A12) predicts that $x_e$ depends only on $t/\tau_{rec}$, and hence $x_e$ remains close to unity (and thus $\mu_{H\alpha}$ at its peak value) only if $t/\tau_{rec}$ is small, but that is not true for the highest densities at the earliest times for the range of times that are plotted. However, it clearly does a good job of reproducing the late-time behaviour ($\mu_{H\alpha} \propto (t/\tau_{rec})^{-2}$), to which all the models in Fig. 4 asymptote.

Equation (A3) does not have an analytic solution when the time-dependence of $\varphi_i$ is included. However, it is easily solved numerically and can be transformed into a more useful form with some trivial definitions. Define the dimensionless time $\tau$ by

$$\tau \equiv \alpha n_H t = t/\tau_{rec} ;$$  \hspace{1cm} (A13)
\[ \gamma = \tau_{\text{rec}}/\tau_i^0 \] (A14)

where \( \tau_i^0 \) is the ionisation time at \( t = 0 \), and

\[ \beta = \tau_{\text{rec}}/\tau_s \] (A15)

the ratio of recombination to ionising photon luminosity e–folding times. Then eq. (A3) becomes

\[ \frac{dx_e}{d\tau} = -x_e^2 + \gamma e^{-\beta \tau} (1 - x_e) \] (A16)

We can write the ionisation rate per H atom as

\[ \zeta \approx C_i \varphi_i \sigma_0 \] (A17)

where \( \sigma_0 \) is the H ionisation cross-section at threshold and \( C_i \) is a constant of order unity that depends on the shape of the spectrum. The ionisation time \( \tau_i^0 \) then evaluates to

\[ \tau_i^0 = 5000 \frac{C_i}{\varphi_6} \text{ yr} \] (A18)

and we can write \( \gamma \) as (using eq. [A9] for \( \tau_{\text{rec}} \))

\[ \gamma = 240 \frac{\varphi_6}{C_i n_{-1}} \] (A19)

The resulting H\( \alpha \) surface brightness obtained from the solution of eq. (A16) for the ionisation fraction, normalized to the peak value, is shown in the righthand panel of Fig. 8 for \( \gamma = 240 \) and values of \( \beta \) from 0.2 to \( \infty \) (the case shown in the lefthand panel). However, an important point from this analysis can be derived simply from the form of eq. (A16). As just shown, \( \gamma \) must be large – this is inevitable from the assumption that the gas in the H\( \alpha \)-emitting region is highly ionised to begin with. Hence the ionisation fraction (and thus the H\( \alpha \) emission) will not begin to decline substantially until

\[ e^{-\beta \tau} \sim 1/\gamma \] (A20)

and thus until \( \tau \) reaches the critical value

\[ \tau_c \sim \frac{\ln \gamma}{\beta} \] (A21)

Physically, this is just a reflection of the requirement that the ionisation time must be longer than the recombination time before the ionisation fraction begins to drop. If \( \beta \ll 1 \) — the ionising photon flux is decreasing on a timescale longer than the recombination timescale — the ionisation fraction (and thus the H\( \alpha \) emission) will not begin to decline substantially until many recombination times have passed.

The numerical solutions of eq. (A16) show that the expression (A21) for the critical time is quite accurate: for \( \gamma = 240 \), it predicts \( \tau_c \approx 0.55, 5.5, 11, \) and 27 for \( \beta = 10, 1, 0.5, \) and 0.2, respectively. Since \( \tau_i \) depends only logarithmically on \( \varphi_i \) and the gas density \( n_H \), the precise values of these quantities are unimportant — all that matters is that, generically, \( \ln \gamma \sim 1 \). Unless \( \tau_i \) is much shorter than \( \tau_{\text{rec}} (\beta \gg 1) \), the decline of \( x_e \) — and thus of \( \mu_{\text{H}\alpha} \) — is substantially delayed from the instantaneous \( \varphi_i \)
turn-off case. (Note also that for $\beta < 1$, the decline is steeper once it begins. This is because the derivative of $x_\alpha$ with respect to $\ln \tau$ has its maximum at $\tau_e$ — physically, there is simply more time available between the steps of $\ln \tau$ at these later times.)

This simple model can also be used to address another very important issue. We do not know a priori what the peak luminosity of the burst was, or the timescale on which it decayed. All we know is that the peak H$\alpha$ surface brightness was at least equal to the present-epoch value. Define

$$\rho = \frac{\rho_{\text{H}\alpha, \text{obs}}}{\rho_{\text{H}\alpha, \text{peak}}}$$

which is also equal to the ratio of minimum to peak ionizing photon luminosity $N_{i,\text{min}}/N_{i,\text{peak}}$ and to the ratio of the minimum required Eddington fraction to the peak value, $f_{E,\text{min}}/f_{E,\text{peak}}$. Consider first the limit of $\tau_i \to 0$. From eq. (A7), we have

$$\rho = \left(1 + t/\tau_{\text{rec}}\right)^{-2}$$

(cf. eq. [A12]). The time needed for the H$\alpha$ surface brightness to decline to its observed value, in units of the recombination time, is simply

$$\tau_{\rho} = \rho^{-1/2} - 1$$

The value of $\tau_{\rho}$ predicted by eq. (A24) agrees reasonably well with the models presented in Fig. 4. For $D = 55$ kpc, $\rho \simeq 0.2$, and so $\tau_{\rho} = 1.24$. Using eq. (A9) for $\tau_{\text{rec}}$, the values from Table 1 give $\tau_{\rho} = 1.08 - 1.2$, while for the $D = 100$ kpc model, $\rho \simeq 0.64$, so the predicted value of $\tau_{\rho} = 0.25$, while the derived values range from 0.25 to 0.35. The differences between the prediction and the calculated values result from the simplification of eq. (A9) in assuming a constant recombination coefficient that is independent of time and ignores the different temperature histories as shown in Fig. 5.

For the case of non-instantaneous decline of the burst luminosity, we can easily solve for $\tau_{\rho}$ numerically for different values of $\beta$. One difference from the results shown in the righthand panel of Fig. 8 is that we must define $\gamma$ consistently with the choice of $\rho$; this can be seen by noting that eq. (A14) for $\gamma$ can be written, using eq. (2) for $\varphi_{i,\text{min}}$ and eq. (A9) for $\tau_{\text{rec}}$, as

$$\gamma = \frac{93.6}{\rho^{n-1}}$$

which we use to specify $\gamma$ as a function of $\rho$.

The solutions for $\tau_{\rho}$ are shown in Fig. 9. The left panel assumes a Stream gas density fixed at $n_H = 0.1$ cm$^{-3}$, and shows the results for several different values of $\beta$ (as in Fig. 7). The offset between the curves with different $\beta$ is a direct reflection of the delay in the decline of $\rho_{\text{H}\alpha}$ seen in the righthand panel of Fig. 8. In the righthand panel of Fig. 9, $\beta$ has been fixed at 3 (see below), and $\tau_{\rho}$ is plotted against $\rho$ for several different densities. From eq. (A25), for fixed $\rho$ the value of $\gamma$ increases with decreasing density $n_H$, which is why the curves flatten out as $n_H$ declines to the lowest values. The spread is much smaller than in the variable-$\beta$ curves shown in the lefthand panel, especially for small values of $\rho$; this is because $\tau_e$ depends only on $\ln \gamma$ whereas it depends linearly on $1/\beta$, as discussed above (eq. [A21]). The steep decline as $\rho \to 1$ seen in both panels of Fig. 10 is imposed by the initial condition $x_\alpha = 1$ at $\rho = 1$. The convergence of all the models to the same steep rise as $\rho \to 0$ results from the negligible size of the ionization term at late times ($\tau \gg \tau_e$), so that they all approach the $x_\alpha \propto \tau^{-2}$ solution (A7) for the instantaneous-decline case.
We use these results in §5.1 to discuss the constraints on the peak luminosity and decay timescale of the Sgr A* flare. Here we note that $\beta$ is likely to be at least a few. In terms of the Eddington fraction and the burst age $T_o$, we can evaluate eq. (A24) to get

$$n_H T_o \lesssim 1.2 \times 10^5 \left( \frac{7.1}{(D/55 \text{ kpc})} - 1 \right) \text{ cm}^{-3} \text{ yr}$$

(A26)

for $f_{E, \text{peak}} = 1$. This gives the largest possible value for $\tau_s$. In §5.1, we infer a central flare that has faded by 80 dB, or approximately 18 $e$-folding times, since the burst peak. With eq. (A26), we then get that $\tau_s \lesssim 4(2) \times 10^5/n_H$ for $D = 55(100) \text{ kpc}$. This implies $\beta \gtrsim 3 - 6$ for the Stream distances: burst decay times longer than $\tau_s \sim a \times 10^5 \text{ yr}$ are unlikely, given the probable age of the Fermi bubbles. In Fig. 10 we show the required value of Eddington fraction $f_E$ as a function of burst age $T_o$ and gas density $n_H$ for these two cases. Comparison with Fig. 7 in §5.1 shows that the differences from the case $\beta \to \infty$ are modest.

![Fig. 10](image-url)

We mention briefly one further important point. The gas recombination/cooling times can obscure any natural variations in the source ionising luminosity. As discussed in the text, the Stream Hα emission must arise from a fading source, but the fading time of the Hα emission is limited by the gas recombination time, which imposes a transfer function on the luminosity variations. The source variation timescale $\tau_s$ could in principle be shorter, and the luminosity variations even more dramatic, than what we infer. In reality, the transfer function will be even more complex than what is implied by the simple model used here, since the real Stream gas has distributions of gas density and column density. In general, when comparing numerical models of AGN variability with the Stream emission (e.g. Novak et al 2011), the modelled data stream must be temporally convolved with a function whose bandwidth will depend on the gas density.

### B. THE IMPLAUSIBILITY OF A STARBURST ORIGIN OF THE FLARE

Equation (3) provides a minimum estimate for the ionising photon luminosity needed to explain the Stream Hα emission of $N_i \sim a \times 10^5 \text{ phot s}^{-1}$ — this assumes no fading of the emission and no significant absorption of the ionising photon flux. What starburst parameters does this imply?

Maloney (1999) quotes a ratio of ionising photon luminosity to star formation rate of

$$N_i/M_* \sim 10^{53} \text{ phot s}^{-1} M_{\odot}^{-1} \text{ yr}$$

(B1)

with substantial caveats on starburst age, upper and lower mass cutoffs, etc. This number agrees very well with the properties of the massive young star clusters formed in the Galactic Centre over the past several Myr: the Quintuplet, the Arches, and the Nuclear Cluster, which have total stellar masses $\sim 10^4 M_{\odot}$, ages in the range 1–7 Myr, and $N_i \sim 10^{51} \text{ phot s}^{-1}$ (Figer, McLean, & Morris 1999). Even for burst timescales as short as 1 Myr, the resulting star formation rates $M_* \sim 0.01 M_{\odot} \text{ yr}^{-1}$, giving ionising photon luminosities per unit SFR in agreement with (B1). We can also use these observations to estimate the ionising photon flux per unit mass of stars formed: this is

$$N_i/M_* \sim 10^{47} \text{ phot s}^{-1} M_{\odot}^{-1}.$$  

(B2)
Powering the Stream emission at the minimal levels of eq. (3) thus requires a SFR of

\[ \dot{M}_* \sim 1.4 - 4.7 \, M_\odot \, \text{yr}^{-1} \]  \tag{B3} \]

and a total mass of stars formed of

\[ M_* \sim (1.4 - 4.7) \times 10^6 \, M_\odot \]  \tag{B4} \]

The requirement of eq. (B3) exceeds by \( \sim \) two orders of magnitude all estimates of the SFR in the Galactic Centre within the last 1–100 Myr (e.g. Pfuhl et al 2011, their Fig. 14, and many references therein; see also above). A similar problem arises with the mass of stars in the Galactic Centre as a function of age (Pfuhl et al 2011). This number for the SFR is likely to be a substantial underestimate, since we have neglected extinction in the vicinity of the star-forming regions: for the three young Galactic Centre clusters discussed above, a large fraction of the emitted ionising photons are absorbed locally.

In fact, the situation is even worse than this: any such nuclear starburst would have to have declined in luminosity by \( \sim \) 2 orders of magnitude from the required peak luminosity to the present epoch, indicating that the peak SFR and the mass of stars formed in the burst would need to be even larger than the estimates of eqs. (B3) and (B4). Hence starburst models for the Stream \( \mu \) problem arise with the requirement of eq. (B3) exceeds by \( \sim \) two orders of magnitude from the required peak luminosity to the present epoch, indicating that the peak SFR and the mass of stars formed in the burst would need to be even larger than the estimates of eqs. (B3) and (B4). Hence starburst models for the Stream \( \mu \) are simply not viable: the required star formation rates greatly exceed anything seen in the star formation history of the Galactic Centre.

C. SPECTRAL ENERGY DISTRIBUTION OF AN ACCRETION DISK

Our model for the accretion disk comprises a ‘cool’ big blue bump and a ‘hot’ power law component. We define the specific photon luminosity for the two-component spectrum by

\[ N_* = k_1(E/E_1)^{-2/3} e^{-E/E_1} + k_2(E/E_2)^{-\alpha - 1} e^{-E/E_2} \chi(E - E_1) \text{ phot s}^{-1} \text{ eV}^{-1}, \]  \tag{C1} \]

where \( \chi(E - E_1) = 1 \) if \( E > E_1 \) and \( \chi(E - E_1) = 0 \) otherwise. Then the total AGN luminosity is given by

\[ L_* = \int_0^\infty E N_* dE \]

\[ = k_1 E_1^2 \int_0^\infty e^{1/3} e^{-c} dc + k_2 E_2^2 \int_{w_2}^\infty \mu^{1-\alpha} e^{-\mu} d\mu \]

\[ = L_0 + L_2 \]  \tag{C2} \]

where \( c = E/E_1, \mu \equiv E/E_2, \) and \( w_2 \equiv E_1/E_2. \)

Taking the hydrogen ionisation potential, \( I_H = 13.59844 \mathrm{eV} \), and \( w_1 = I_H/E_1 \), the AGN ionising luminosity is found by integrating from the Lyman limit to infinity,

\[ L_{i,*} = \int_{w_1}^\infty E N_{i,*} dE \]

\[ = k_1 E_1^2 \int_{w_1}^\infty e^{1/3} e^{-c} dc + k_2 E_2^2 \int_{w_2}^\infty \mu^{1-\alpha} e^{-\mu} d\mu \]

\[ = L_1 + L_2 \]  \tag{C3} \]

where the limit for the second integral remains the same since \( w_2 > w_1. \)

The big blue bump total contribution remains the same since \( w_2 > w_1. \)

The big blue bump total contribution is

\[ L_0 = k_1 E_1^2 \Gamma \left( \frac{4}{3} \right) \]  \tag{C4} \]

where \( \Gamma(a) \) is the complete gamma function. The big blue bump ionising contribution is

\[ L_1 = k_1 E_1^2 \Gamma \left( \frac{4}{3}, w_1 \right) \]  \tag{C5} \]

and, finally, the third integral (the power-law X-ray + gamma-ray contribution) is

\[ L_2 = k_2 E_2^2 \Gamma(2-\alpha, w_2) \]  \tag{C6} \]

where we use the incomplete gamma function, \( \Gamma(a,b), \) and \( \alpha \) must be less than 2. Here we adopt a photon spectral index of \( \alpha = 1.9. \)

If we define \( \eta = L_1/L_2, \) so that \( L_2 = L_{i,*} / (1 + \eta) \) and \( L_1 = \eta L_2, \) then we can write \( k_1 \) and \( k_2 \) as

\[ k_1 = L_{i,*} E_1^{-2} \left[ \frac{\eta}{\Gamma(4/3, w_1)(1+\eta)} \right], \]  \tag{C7} \]
The scaling coefficient ratio \( k_1/k_2 \) is independent of \( L^{\star} \), such that

\[
\frac{k_1}{k_2} = \eta \left[ \frac{E_2^2}{E_1^2} \frac{\Gamma(2-\alpha, w_2)}{\Gamma(4/3, w_1)} \right].
\]

(C9)

Once the AGN luminosity \( L^{\star} \) and UV to X-\( \gamma \) ratio (\( \eta \)) are specified, the normalisation constants \( k_1 \) and \( k_2 \) follow immediately (see §2).

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