

$$Z' = Z P_i \Rightarrow Z'|C\rangle = Z P_i |C\rangle = Z|C\rangle$$