

$$\pm X_{\text{in}} X_{\text{out}} |C\rangle_{\mathcal{L}} \equiv |C\rangle_{\mathcal{L}},$$