Lecture 9

## **Momentum**

#### MOMENTUM AND IMPULSE

KJF chapter 9

# Linear Momentum of a Body

We define the momentum of an object as:

$$\underline{p} = m \underline{v}$$

where m = mass and  $\underline{y} = \text{velocity}$ .

p is a vector and is in the same direction as v.  $(Don't\ confuse\ p\ with\ power\ or\ pressure.)$ 

Units: kg.m.s-1

#### Momentum and Newton's 2nd Law

If  $F_{\text{net}}$  and m are constant, then

$$\underline{F}_{\text{net}} = m\underline{a} = m \Delta \underline{v}/\Delta t$$

$$= \Delta m \underline{v} / \Delta t = \Delta \underline{p} / \Delta t$$

Newton originally expressed his second law in terms of momentum.

If *m* or  $\underline{F}$  are NOT constant then:  $\underline{F}_{net} = d\underline{p}/dt$ 

Hecht §4.3 & 7.4

#### Momentum of a system of particles

*Total* momentum p is the vector sum of individual momenta:

$$\underline{p} = \sum \underline{p}_{i} = \sum m_{i} \underline{v}_{i}$$
 (Vector sum!)

Now consider the particles as one system:

N2L becomes:

$$\sum \underline{F}_{\text{ext}} = d\underline{p}/dt$$

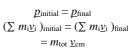
where  $\Sigma \underline{F}_{ext} = net$  external force i.e. not forces between particles in the system.

## Conservation of Momentum

So if  $\sum \underline{F}_{ext} = 0$  for a system

then dp/dt = 0 total momentum is constant

When the particles interact (e.g. billiard ball collision, explosion etc.), if net external force is zero then total momentum before interaction equals total momentum after i.e. momentum is conserved



KJF §9.4



#### Example

Calculate the recoil speed of a pistol (mass 0.90 kg) given that the bullet has mass 8.0 g and emerges from the pistol with a speed of 352 ms<sup>-1</sup>. Assume the momentum of the exhaust gas is negligible.



 $[3.1 \text{ ms}^{-1}]$ 

## **Impulse**

The impulse  $\underline{J}$  of a force is defined as the change in momentum  $\Delta p$  caused by that force.

From Newton's Second Law, if  $\underline{F}$  is constant

$$\underline{F} = \Delta \underline{p} / \Delta t$$

Then

$$\underline{F} \Delta t = \Delta \underline{p} = \underline{J}$$

Example: 1.0 kg object falls under gravity. Calculate the impulse the object experiences due to its weight after falling for 10 s.

[98 kg m s<sup>-1</sup> downwards]

## Impulse (2)

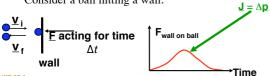
However, if F is not constant

 $\underline{J} = \underline{F}_{av} \Delta t$  or  $\underline{J} = \int \underline{F}(t) dt$ 

i.e. impulse = area under  $\underline{F}$  vs t curve

Remember that if  $\underline{F}$  is constant  $\underline{F}_{av} = \underline{F}$ 

Consider a ball hitting a wall:



## Impulse (3)

$$\underline{J} = \Delta \underline{p} = \underline{F}_{av} \Delta t$$

You can minimise the average force  $\underline{F}_{av}$  during an impact, by increasing the impact time  $\Delta t$ 

e.g. seat belts, driver's air bag, wicket-keeper's glove, thick landing mat for high jumper.

#### **ENERGY**

KJF chapter 10

# What is Energy?

Energy is needed to do useful work.

Energy can move things, heat things up, cool them down, join things, break things, cut things, make noise, make light, and power our electronics, etc.

Energy is a scalar (no direction, not a vector — easy maths!)

S.I. unit of energy is the joule, J

Examples of energy?

- Energy of motion "kinetic energy"
  Stored energy "potential energy": gravitational, elastic, chemical
- Energy in hot objects "thermal energy"

KJF §10.1-10.2

#### **Kinetic Energy**

Simplest form of energy is energy of motion – kinetic energy

 $K = \frac{1}{2} mv^2$ 

where m is mass (kg) and v is magnitude of velocity (ms<sup>-1</sup>).

Unit definition:  $1 J = 1 \text{ joule} = 1 \text{ kg.}(\text{m.s}^{-1})^2 = 1 \text{ kg.m}^2.\text{s}^{-2}$ 

Example: A 1.0 kg mass moves @ 2.0 ms-1. Find K.E.

 $[K = \frac{1}{2} \times 1.0 \text{ kg} \times 4.0 \text{ m}^2.\text{s}^{-2} = 2.0 \text{ J}]$ 

KJF §10.5

13

# **Gravitational Potential Energy**

Stored energy due to height in a gravitational field:

G.P.E. or U = mgh

where m is mass (kg) and h is height above the origin level (m).

The origin position (h = 0) can be freely chosen U is always *relative* to some reference level or position.

Example: A 1.0~kg mass is held 10~m above the ground. Find its G.P.E. relative to the ground.

 $[U = 1.0 \text{ kg} \times 9.8 \text{ ms}^{-2} \times 10 \text{ m} = 98 \text{ J}]$ 

KJF §10.6

# Mechanical Energy

Kinetic energy and potential energy added together are called *Mechanical Energy*.

Potential energy is stored energy resulting from any force which depends only on position (e.g. gravity, force in a spring, electrostatic attraction).

Gravitational potential energy is only one example of this.

KJF §10.3

15

## Law of Conservation of Energy

Energy cannot be created or destroyed (i.e. it is "conserved")

It can only be changed from one form to another

OR

In an isolated system — one where there is no energy transfer into or out of the system — the total energy  $E_{\text{tot}}$  is conserved.

KJF §10.3