

Question 10

Note: I'm a little easier on the units and significant figures (lose $\frac{1}{2}$ mark only) in this question because there are a lots of small calculations to do and it would be very easy to get 0.

Note: Don't "go negative" with the signs and units mistakes. For each individual questions, the minimum is zero.

(a) Two methods: kinematics or energy method**Energy:**

Without air resistance, *mechanical energy is conserved*;

$$PE_{\text{initial}} + KE_{\text{initial}} = PE_{\text{final}} + KE_{\text{final}}$$

$$mgh + 0 = 0 + \frac{1}{2}mv^2$$

$$gh = \frac{1}{2}v^2$$

$$v = \sqrt{2gh}$$

$$v = \sqrt{(2 \times 9.81 \times 2.00)} = 6.264 \approx \mathbf{6.26 \text{ ms}^{-1}}$$

(2 marks altogether for derivation and calculation)

Note: Lose 1 mark for each algebraic or numerical mistake

Note: Lose $\frac{1}{2}$ mark for incorrect unit, lose $\frac{1}{2}$ mark if more than 4 sig figures quoted.

OR

Kinematics:

$$v_0 = 0 \text{ (let's say down is +ve)}$$

$$v_f^2 = v_0^2 + 2gs$$

$$v_f^2 = 2gs$$

$$v_f = \sqrt{(2 \times 9.81 \times 2.00)} = 6.264 \approx \mathbf{6.26 \text{ ms}^{-1}}$$

(2 marks altogether for derivation and calculation)

Note: Lose 1 mark for each algebraic or numerical mistake

Note: Lose $\frac{1}{2}$ mark for incorrect unit, lose $\frac{1}{2}$ mark if more than 4 sig figures quoted.

- (b) (i) Because the objects *moved together (or with the same velocity)* as though they were one object after the collision it was "perfectly inelastic" by definition. **(1 mark)**

Note: $\frac{1}{2}$ mark for mentioning "perfectly inelastic", $\frac{1}{2}$ mark for mentioning or implying italicised point

- (ii) At the instant of collision, *momentum WAS conserved. Energy was NOT conserved* (because perfectly inelastic) **($\frac{1}{2}$ mark for each italicised point)**

Note: Strictly speaking, momentum was NOT conserved over the time of the collision because there is an external force, **gravity**, acting on the objects. However, if the time of the collision is short (**or in the wording of the question** "at the instant of collision", momentum is very nearly conserved. **Don't** expect this subtle caveat from the students.

- (c) $P_{\text{initial}} = P_{\text{final}}$ (or they can write Momentum conserved)

$$MV_i + 0 = MV_f + mV_f = V_f (M + m) \text{ (say, +ve is down)}$$

$$V_f = MV_i / (M + m)$$

$$V_f = (525 \times 6.26) / (525 + 25) = 5.975 \approx \mathbf{5.98 \text{ ms}^{-1}}$$

(3 marks altogether for derivation and calculation)

Note: Here they must use a result from the previous question. Don't penalise them a second time for when using an incorrect velocity.

- (d) Assuming constant friction force, pile-driver + pole had a constant deceleration.

Two methods: kinematics or energy method

kinematics method:

$$v_f = 0, v_0 = 5.975 \text{ ms}^{-1} \text{ (let's say down is +ve)}$$

$$v_f^2 = v_0^2 + 2as$$

$$-2as = v_0^2$$

$$a = -v_0^2/2s = -(5.975)^2/(2 \times 0.750) = -23.8 \text{ ms}^{-2} \text{ (upwards)}$$

$$\text{But friction force } F \text{ is; } F = ma = -(525 + 25.0) \text{ kg} \times 23.8 \text{ ms}^{-2} = -13090 \text{ N} \approx -1.31 \times 10^4 \text{ N}$$

$$\text{Magnitude of friction force} \approx 1.31 \times 10^4 \text{ N}$$

(3 marks altogether for derivation and calculation)

Note: Lose 1 mark for each algebraic or numerical mistake

Note: Lose $\frac{1}{2}$ mark for incorrect unit, lose $\frac{1}{2}$ mark if more than 4 sig figures quoted.

Note: Here they must use a result from the previous question. Don't penalise them a second time for using a previously incorrectly calculated quantity.

OR

energy method:

Friction does work on pile-driver + pole to convert KE into thermal E. Work done equals KE lost as thermal E (*i.e.* all of it).

$$\therefore \frac{1}{2}mv^2 = W_{\text{friction}} = Fs \cos\theta = -Fs \text{ (}\cos\theta = 180^\circ \text{ for friction)}$$

$$F = -(\frac{1}{2}mv^2)/s$$

$$F = -(\frac{1}{2}(525+25) \times 5.975^2)/0.750 = -13090 \text{ N} \approx -1.31 \times 10^4 \text{ N}$$

$$\text{Magnitude of friction force} \approx 1.31 \times 10^4 \text{ N}$$

(3 marks altogether for derivation and calculation)

Note: Lose 1 mark for each algebraic or numerical mistake

Note: Lose $\frac{1}{2}$ mark for incorrect unit, lose $\frac{1}{2}$ mark if more than 4 sig figures quoted.

Note: Here they must use a result from the previous question. Don't penalise them a second time for using a previously incorrectly calculated quantity.

Note: It is OK if they were not strict about their use of signs during the derivation in this "work" question, as long as they correctly quote the signs in the final answers. I have told them in lectures it is OK when doing work problems to calculate the absolute values and then to establish signs later.