



Physics 1901

**Experimental Astronomy –
Graduate Course
Autumn (Apr-May 2014)**

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Course Philosophy

- Alternate between Physical fundamentals: Why instruments look and work the way they do.
- And cool examples: How they work the way that they do.
- On the way we will try and leave you with some useful tools.

Background: Astronomy is Different

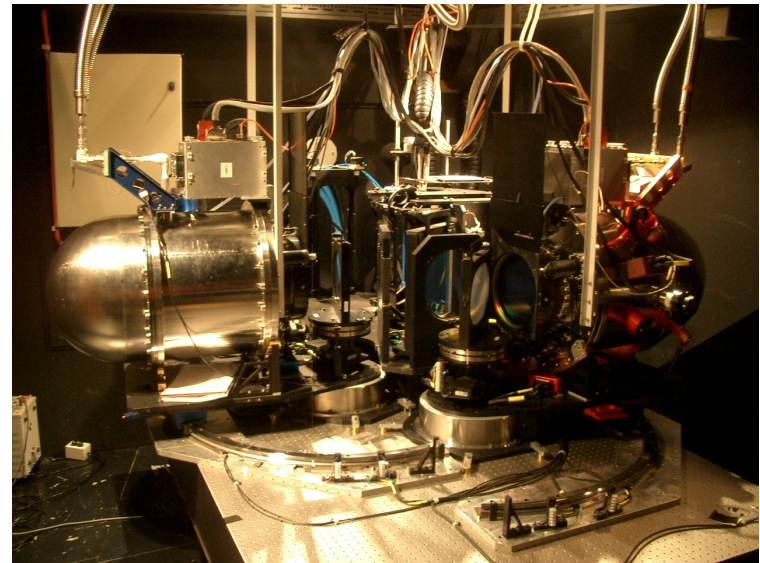
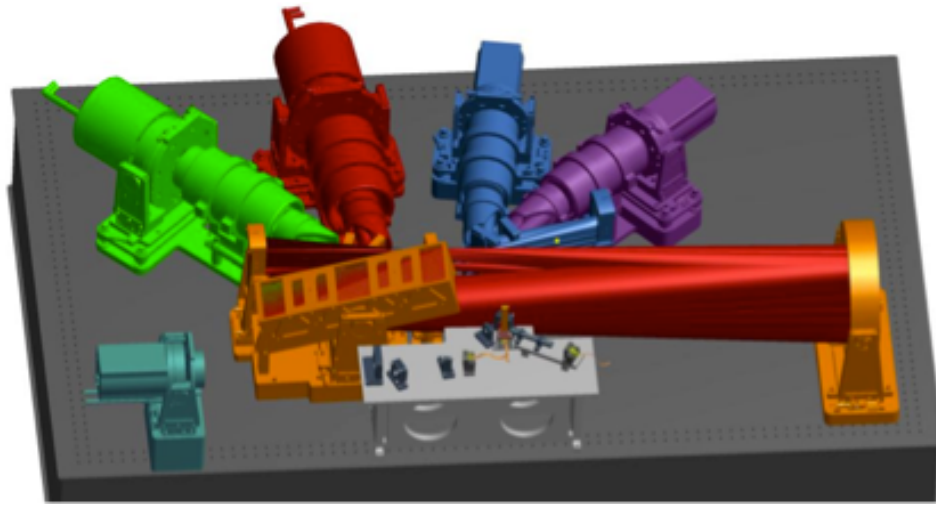
- Universe is the laboratory
- Telescopes are our window into the laboratory
- We can only observe, no interaction
- Limited to phenomena, occurring in the past
- Must take interpret a “snapshot”
- Have only the properties of light
- Cannot measure directly, must infer from the measurement of light.

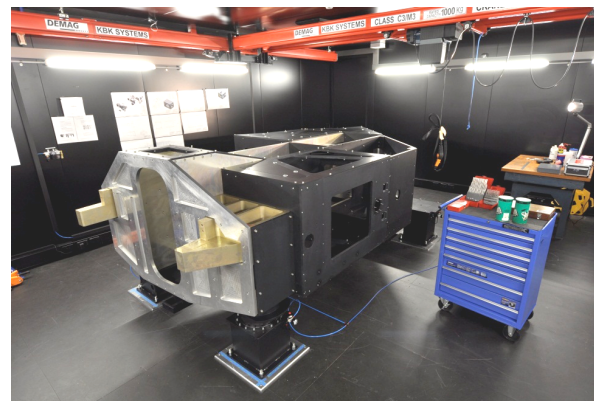
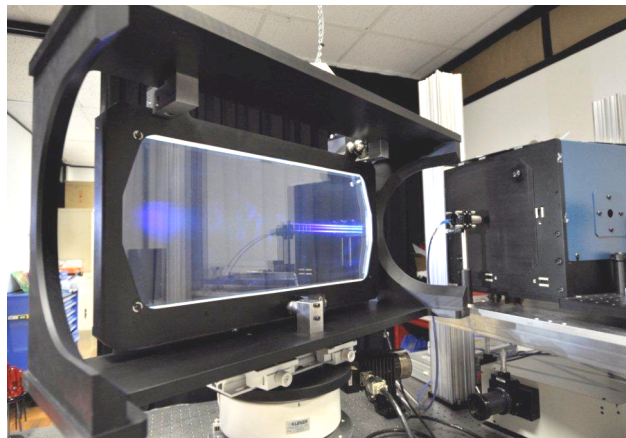
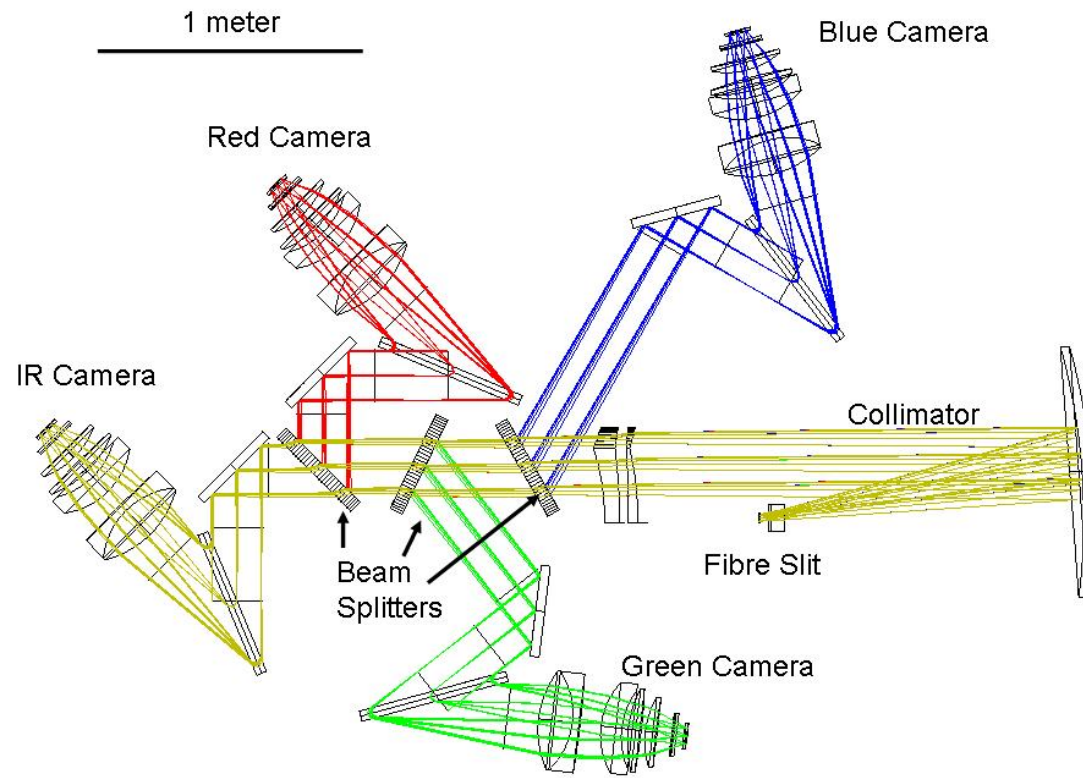
Properties of light

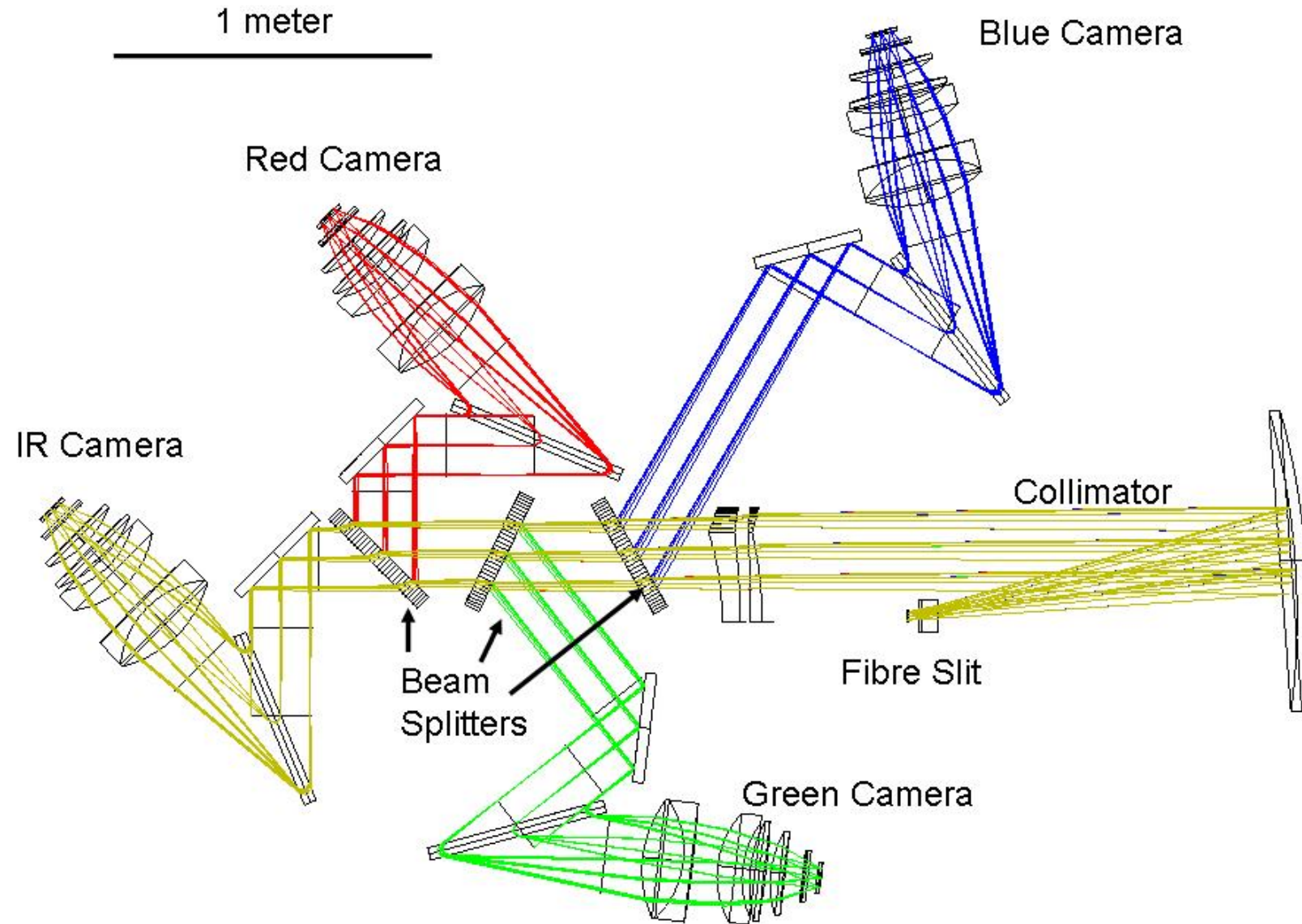
- Intensity, flux, radiance, amplitude
- Angle of arrival, position, image
- Wavelength, frequency, color
- Angular momentum, spin, polarization
- Time variation (in some cases)
- Phase

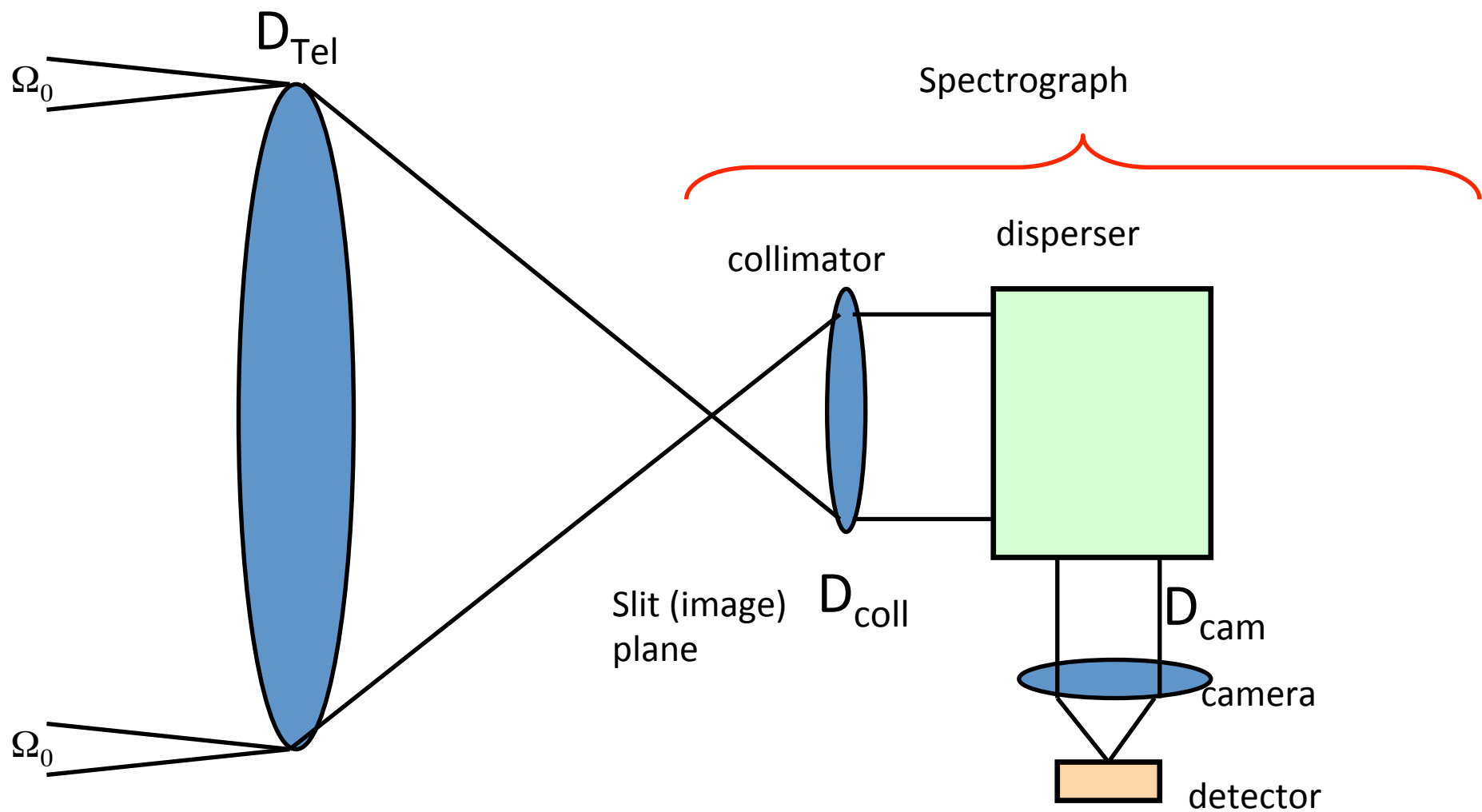
Some questions: (which you should be able to answer at the end of the course)

- What are the parts of a spectrograph
- Why are spectrographs so big?
- What sets the sensitivity?
- How do I estimate the exposure time?









Anamorphic factor,

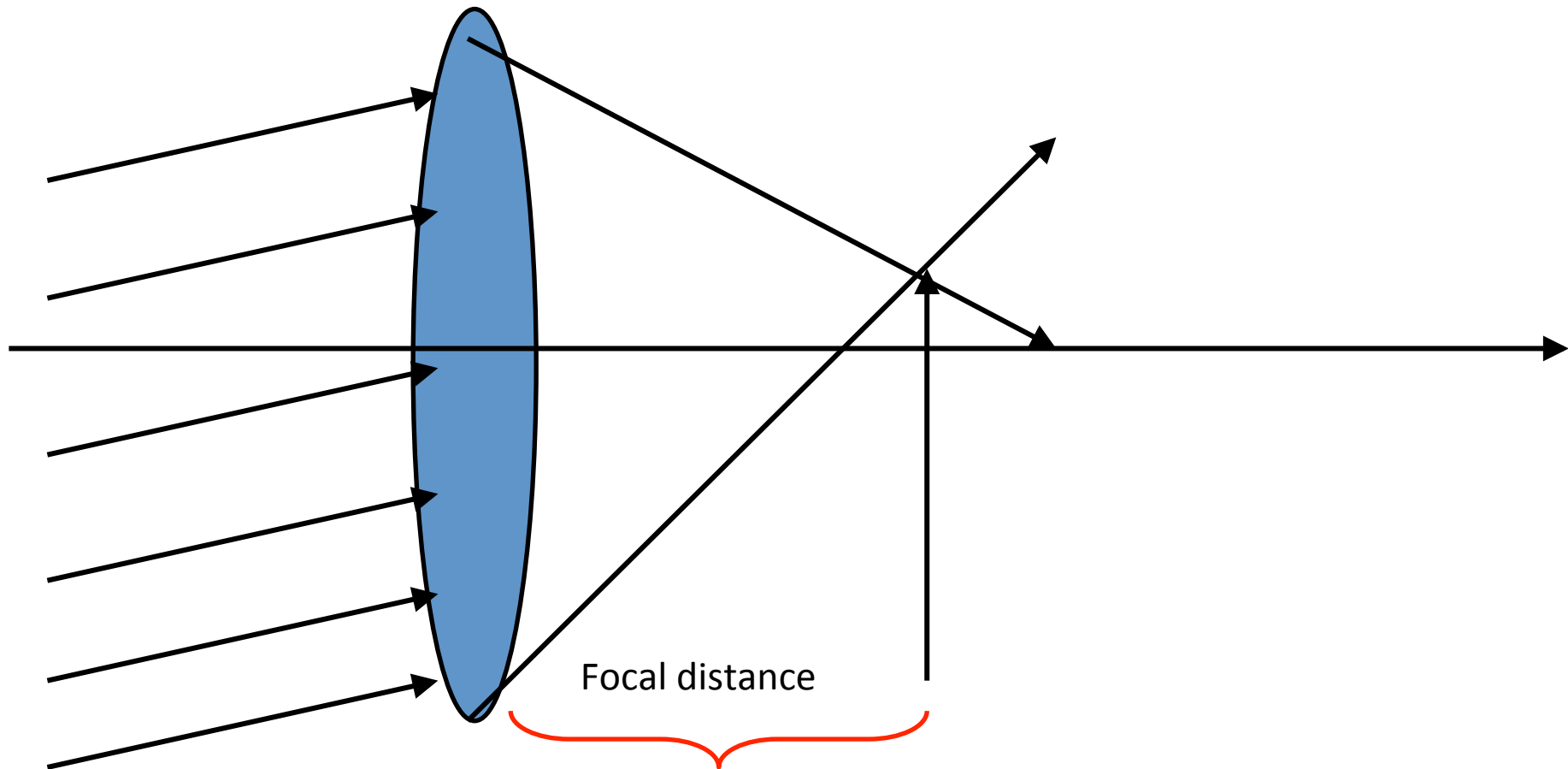
$$r = D_{\text{coll}} / D_{\text{cam}}$$

All about lenses

- Why do lenses form images?
- How do they form images?
- How to describe the process?
- What if I have multiple lenses?

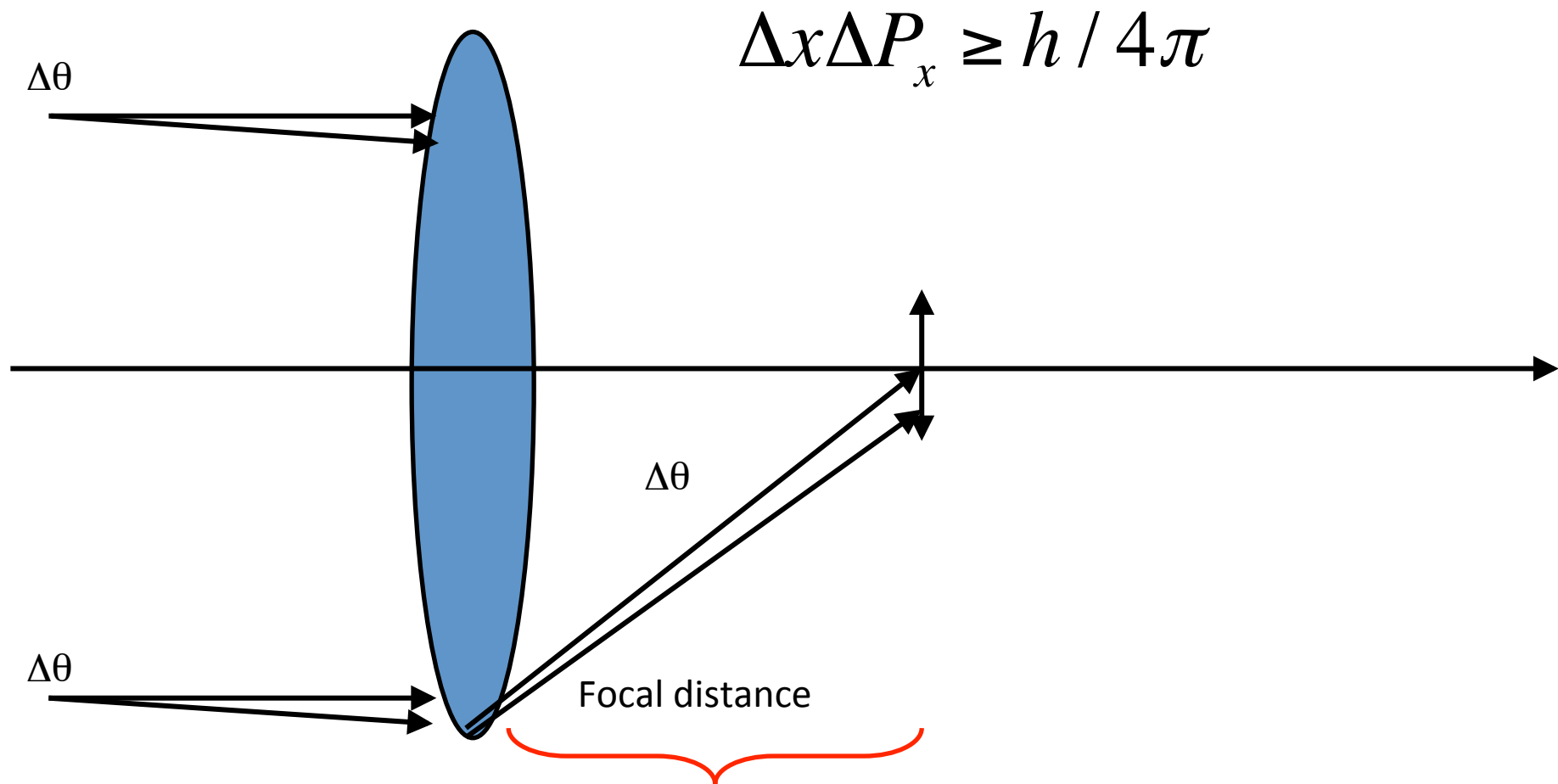
Rule #1

- Parallel rays focus to a point (sort of)



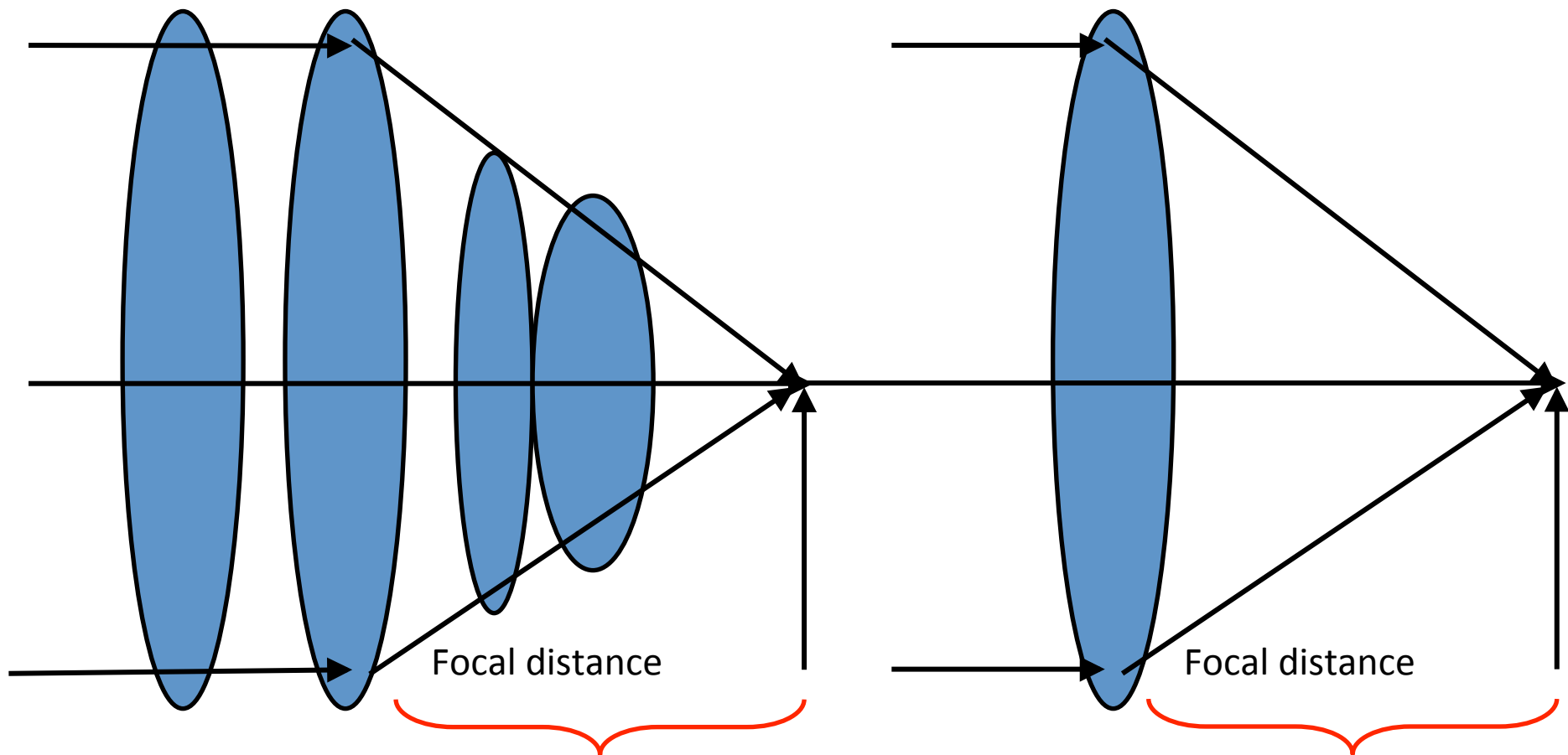
Rule #1

- Parallel rays focus to a point (sort of)



Rule #2

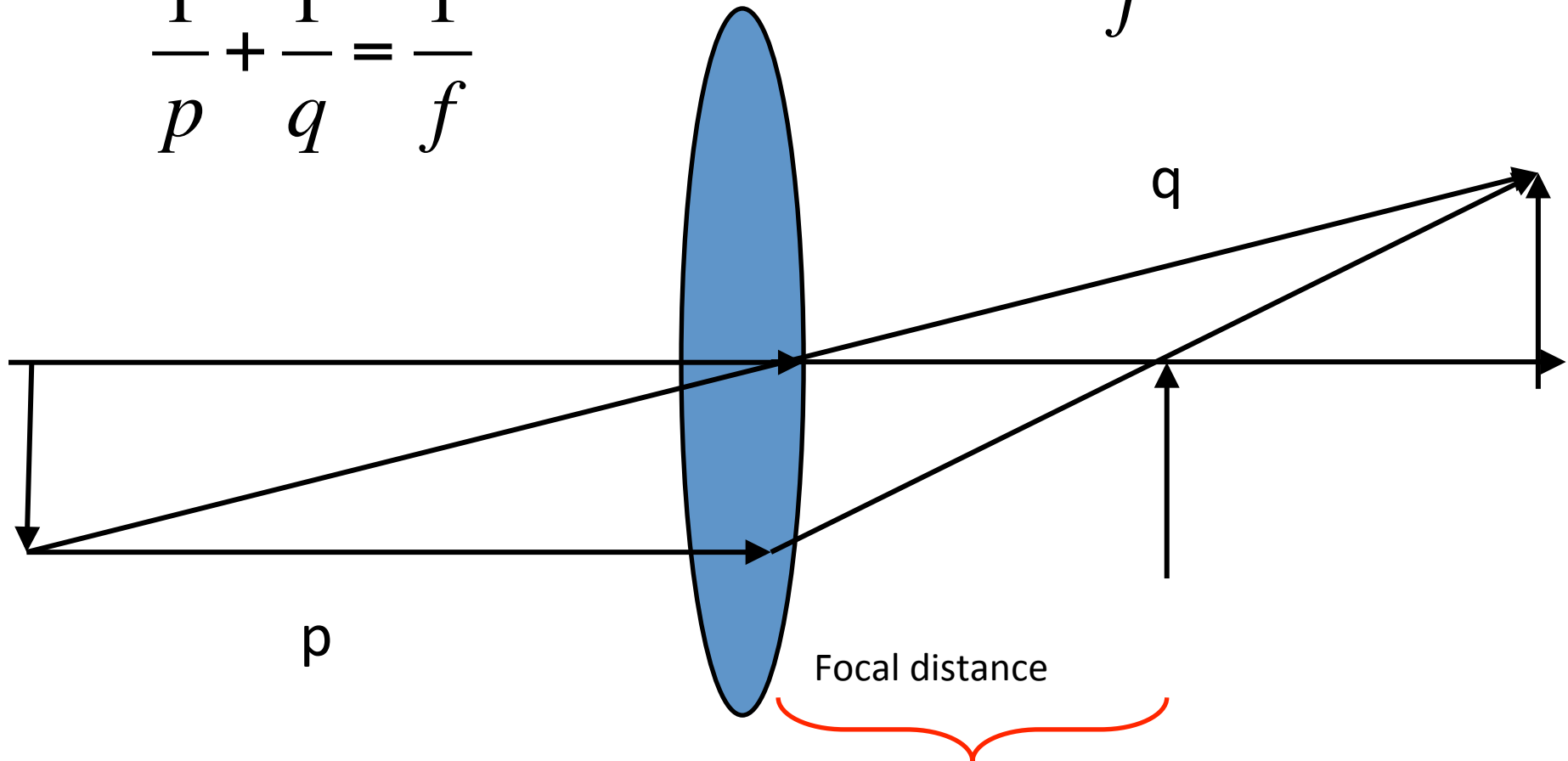
Any system of lenses can be represented by an equivalent lens of the same EFL



Thin lens

$$\frac{1}{p} + \frac{1}{q} = \frac{1}{f}$$

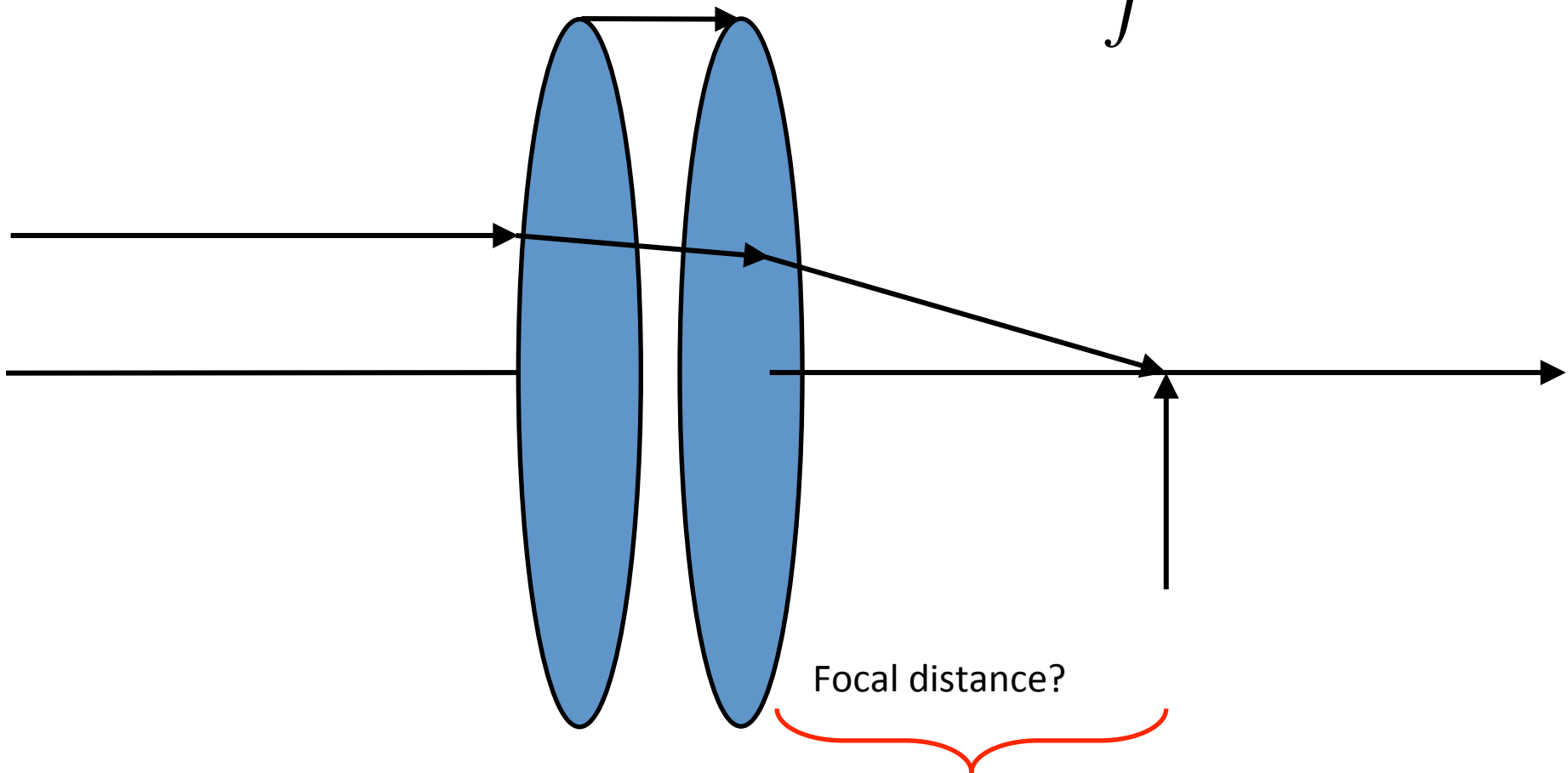
$$\frac{1}{f} = \phi$$



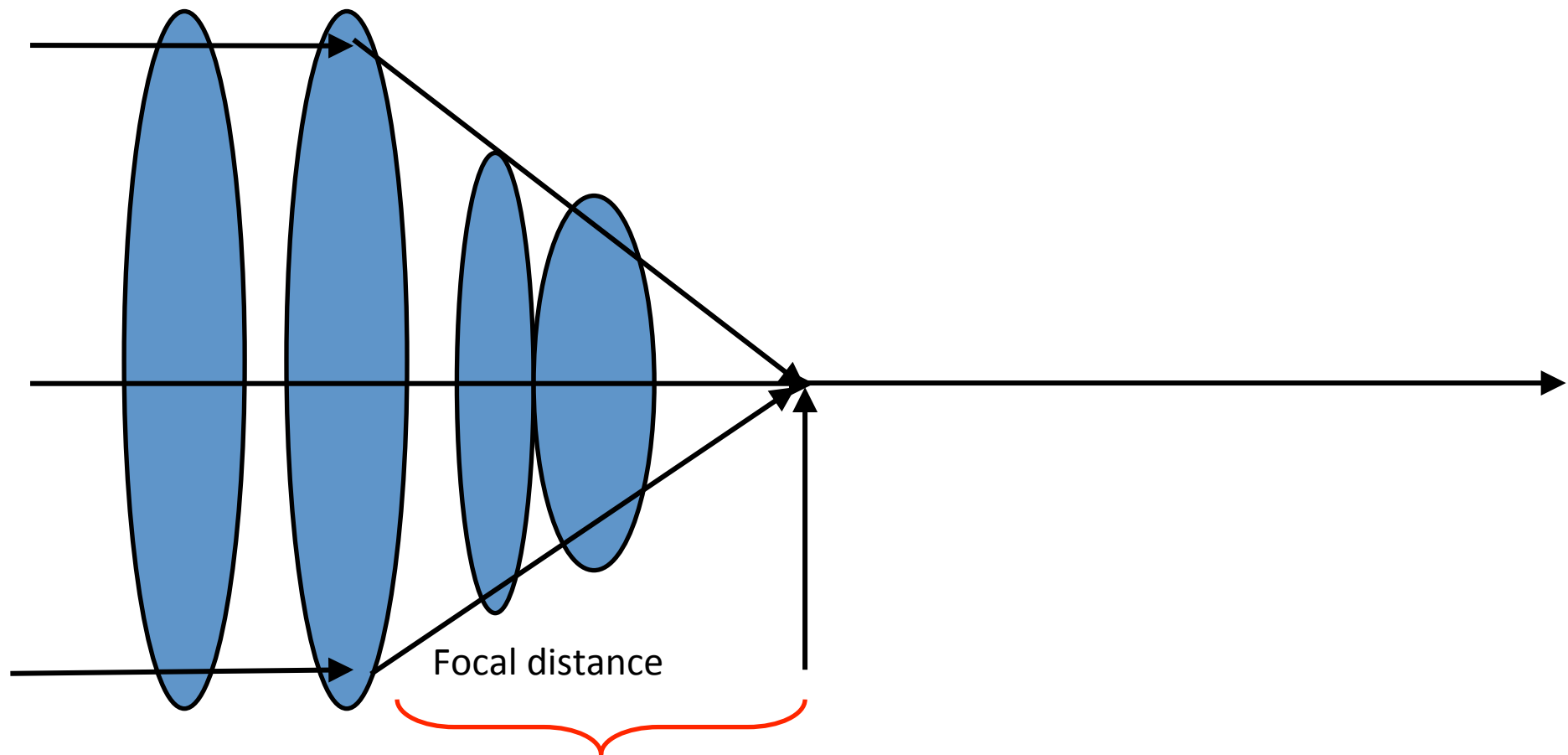
Two Thin lens

$$\phi_{system} = \phi_1 + \phi_2 - t\phi_1\phi_2$$

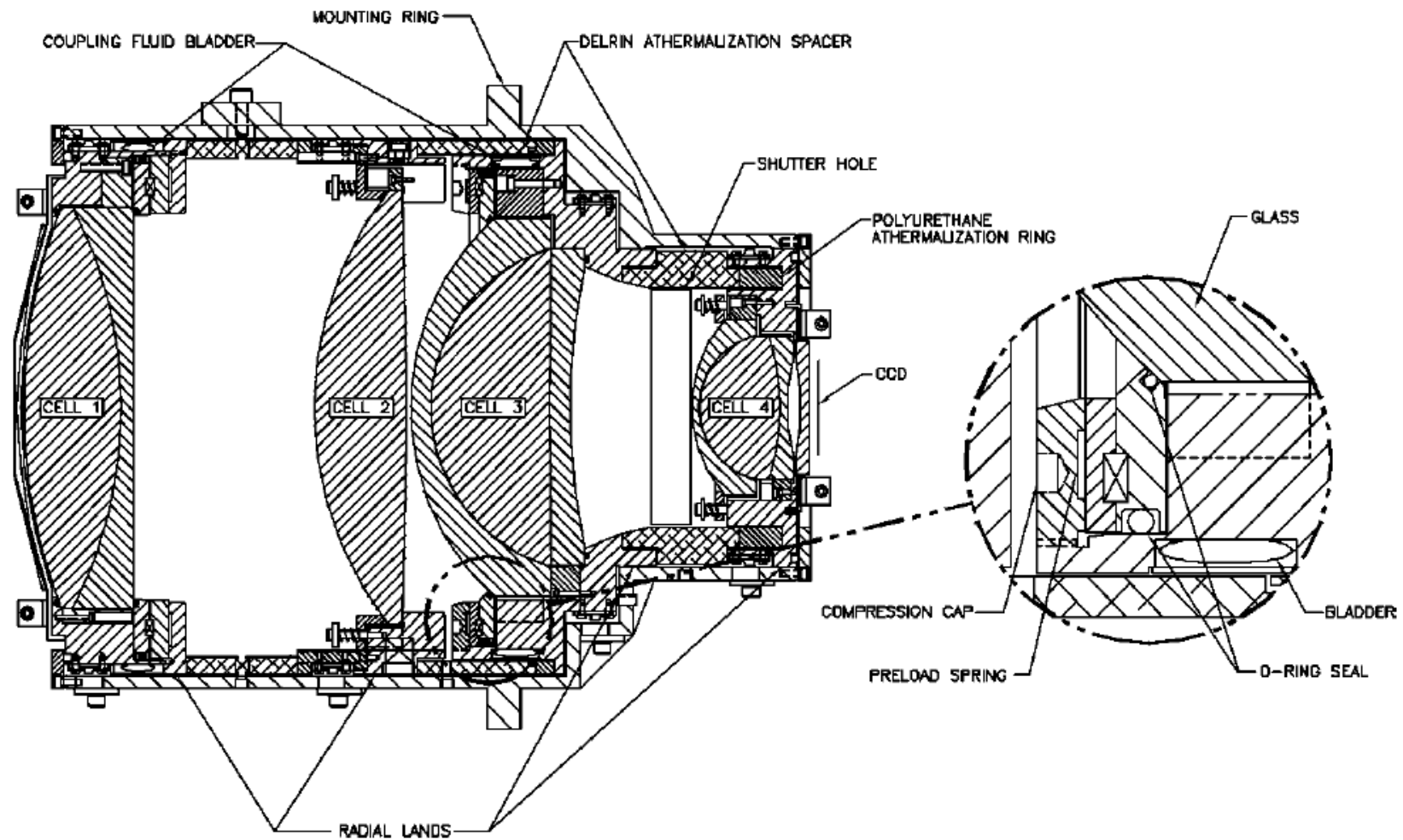
$$\frac{1}{f} = \phi$$



How to deal with this?

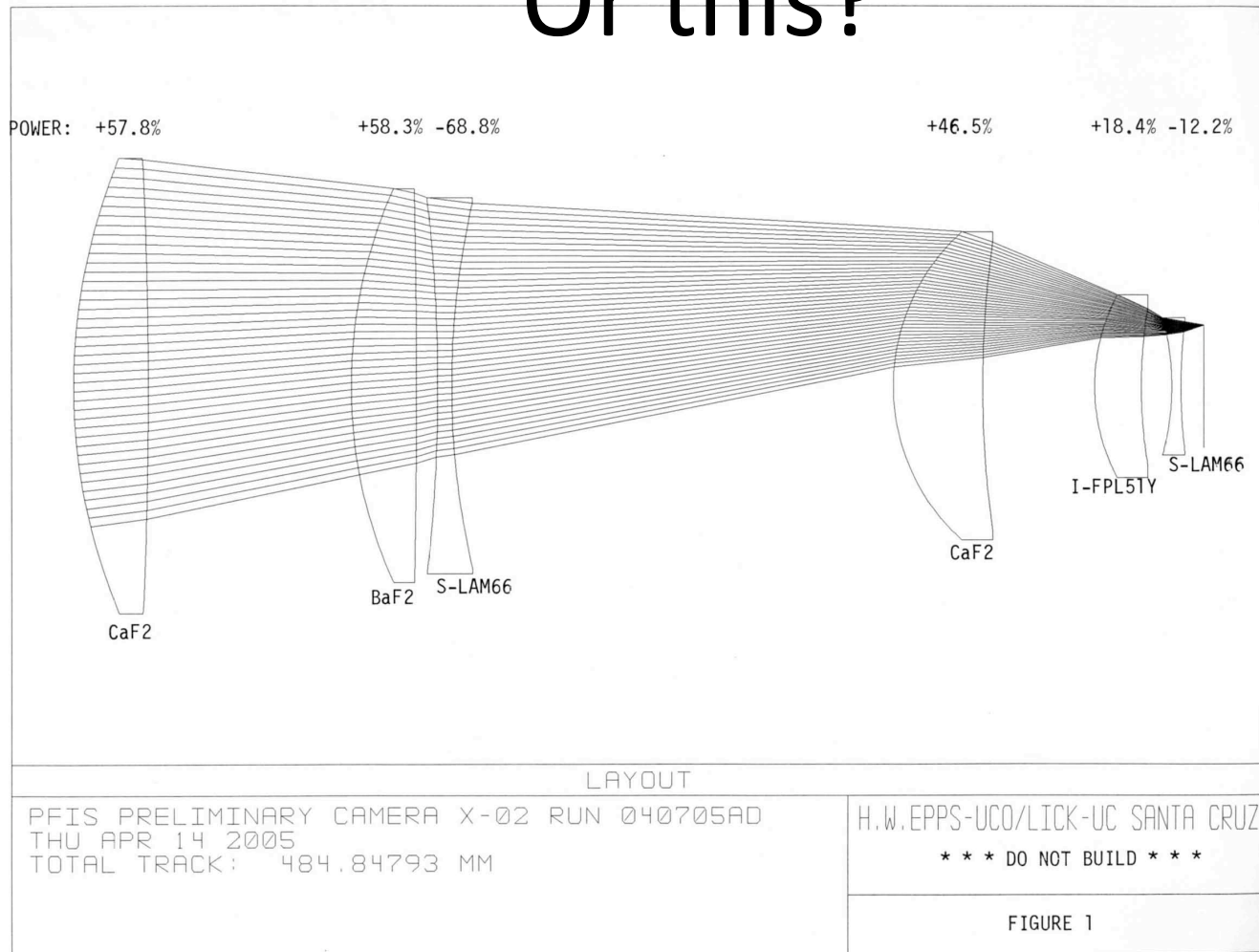


Or this?



Sheinis et al, *Proc. SPIE* Vol. **3786**, p. 413-426.1999.

Or this?

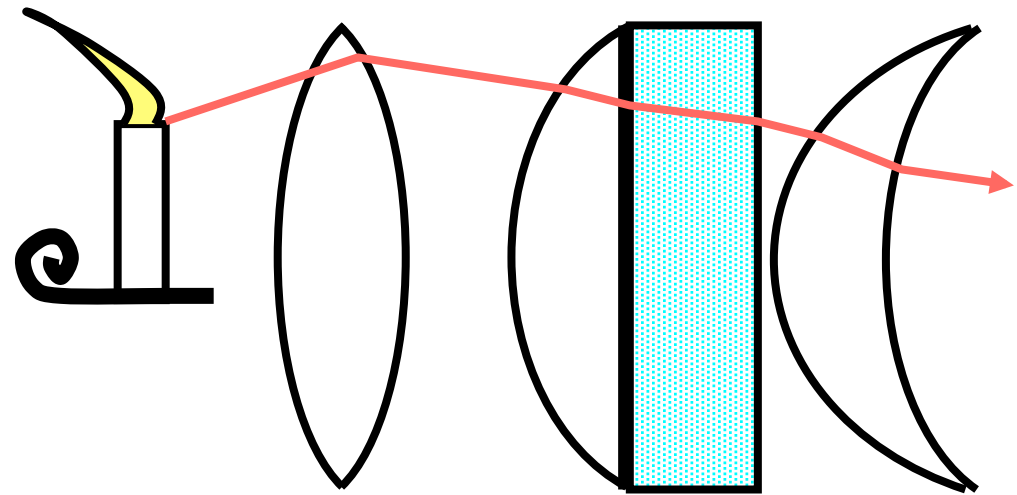


Need a tool to describe lenses

- Paraxial raytrace?

ABCD Matrix Concepts

- Ray Description
 - Position
 - Angle
- Basic Operations
 - Translation
 - Refraction
- Two-Dimensions
 - Extensible to Three



Ray Vector

$$\mathcal{V}_1 = \begin{pmatrix} x_1 \\ \alpha_1 \end{pmatrix}$$

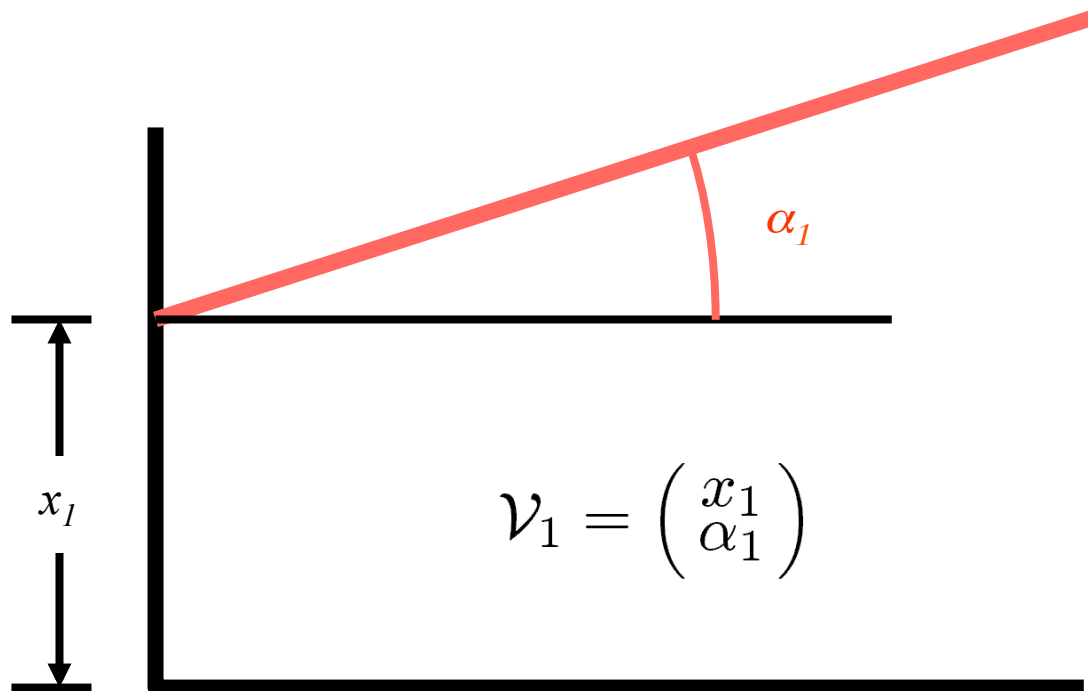
Matrix Operation

$$\mathcal{V}_{out} = \mathcal{M}\mathcal{V}_{in}$$

System Matrix

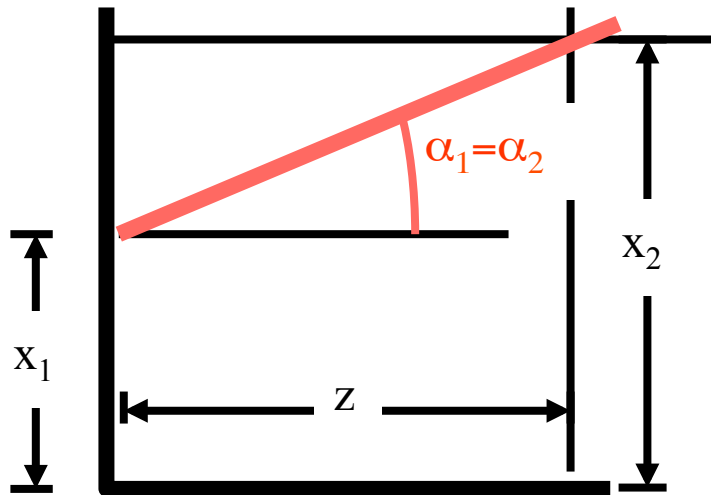
$$\mathcal{M}_{25} = \mathcal{R}_5 \mathcal{T}_{45} \mathcal{R}_4 \mathcal{T}_{34} \mathcal{R}_3 \mathcal{T}_{23}$$

Ray Definition



Translation Matrix

- Slope Constant
- Height Changes



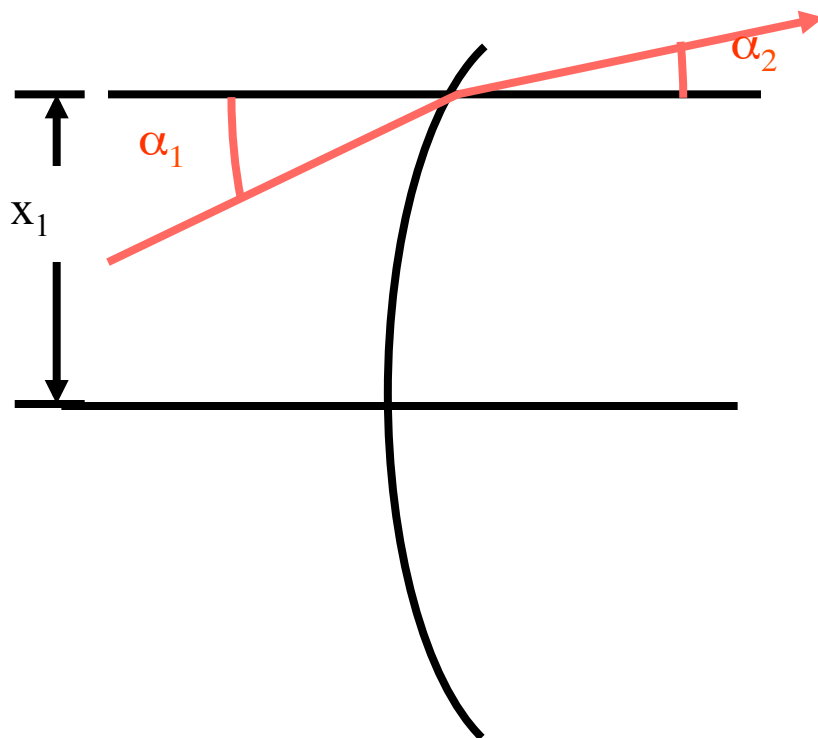
$$x_2 = x_1 + z \left. \frac{dx}{dz} \right|_{x_1}$$

$$\alpha_2 = \alpha_1$$

$$\begin{pmatrix} x_2 \\ \alpha_2 \end{pmatrix} = \begin{pmatrix} 1 & z \\ 0 & 1 \end{pmatrix} \begin{pmatrix} x_1 \\ \alpha_1 \end{pmatrix} = \mathcal{T}_{12} \begin{pmatrix} x_1 \\ \alpha_1 \end{pmatrix}$$

Refraction Matrix (1)

- Height Constant
- Slope Changes



$$x'_1 = x_1$$

$$n\theta = n'\theta' \quad (\theta \text{ Ref. to Normal})$$

$$\phi = x_1/R_1 \quad \theta_1 = \phi + \alpha_1 \quad \theta'_1 = \phi + \alpha'_1$$

$$n'_1 (\phi + \alpha'_1) = n_1 (\phi + \alpha_1)$$

$$\alpha'_1 = \frac{n_1 - n'_1}{n'_1 R_1} x_1 + \frac{n'_1}{n'_1} \alpha_1$$

$$\begin{pmatrix} x'_1 \\ \alpha'_1 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ \frac{n_1 - n'_1}{n'_1 R_1} & \frac{n'_1}{n'_1} \end{pmatrix} \begin{pmatrix} x_1 \\ \alpha_1 \end{pmatrix}$$

Refraction Matrix (2)

Previous Result

$$\begin{pmatrix} x'_1 \\ \alpha'_1 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ \frac{n_1 - n'_1}{n'_1 R_1} & \frac{n_1}{n'_1} \end{pmatrix} \begin{pmatrix} x_1 \\ \alpha_1 \end{pmatrix}$$

Recall Optical Power

$$P_1 = \frac{n'_1 - n_1}{R_1}$$

$$\begin{pmatrix} x'_1 \\ \alpha'_1 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ -P_1/n'_1 & n_1/n'_1 \end{pmatrix} \begin{pmatrix} x_1 \\ \alpha_1 \end{pmatrix} = \mathcal{R}_1 \begin{pmatrix} x_1 \\ \alpha_1 \end{pmatrix}$$

$$\mathcal{R}_1 = \begin{pmatrix} 1 & 0 \\ \frac{-\text{Power}}{\text{Final Index}} & \frac{\text{Initial Index}}{\text{Final Index}} \end{pmatrix}$$

Cascading Matrices (1)

Generic Matrix: $\mathcal{M} = \begin{pmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{pmatrix}$

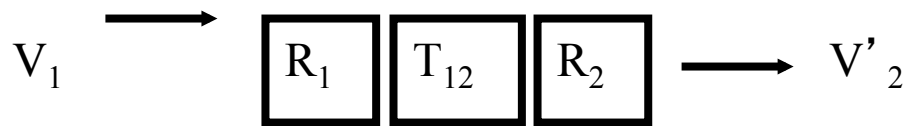
Determinant (You can show that this is true for cascaded matrices)

$$\text{Det } \mathcal{M} = \frac{n}{n'}$$

$$\begin{pmatrix} x'_2 \\ \alpha'_2 \end{pmatrix} = \mathcal{R}_2 \begin{pmatrix} x_2 \\ \alpha_2 \end{pmatrix}$$

$$\begin{pmatrix} x_2 \\ \alpha_2 \end{pmatrix} = \mathcal{T}_{12} \begin{pmatrix} x'_1 \\ \alpha'_1 \end{pmatrix}$$

$$\begin{pmatrix} x'_1 \\ \alpha'_1 \end{pmatrix} = \mathcal{R}_1 \begin{pmatrix} x_1 \\ \alpha_1 \end{pmatrix}$$

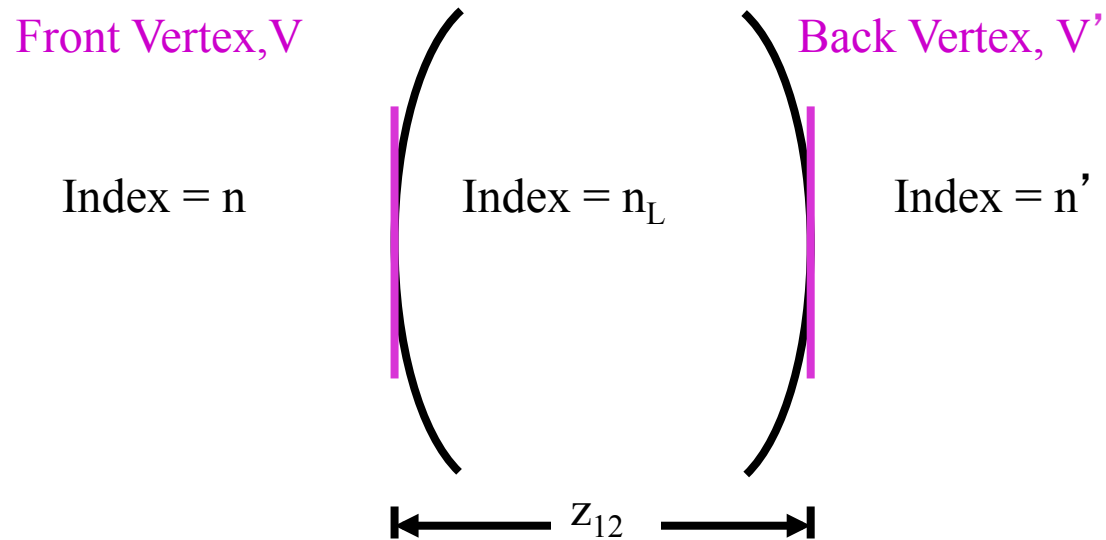


Light Travels Left to Right, but
Build Matrix from Right to Left

$$\begin{pmatrix} x'_2 \\ \alpha'_2 \end{pmatrix} = \mathcal{R}_2 \mathcal{T}_{12} \mathcal{R}_1 \begin{pmatrix} x_1 \\ \alpha_1 \end{pmatrix}$$

$$\mathcal{M}_{12} = \mathcal{R}_2 \mathcal{T}_{12} \mathcal{R}_1$$

The Simple Lens (Matrix Way)



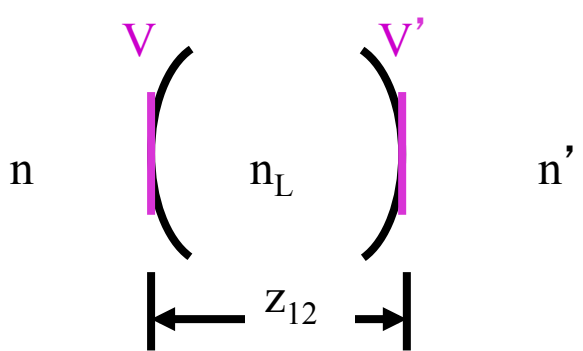
$$\mathcal{M}_{VV'} = \mathcal{R}_2 \mathcal{T}_{12} \mathcal{R}_1$$

Building The Simple Lens Matrix

$$\mathcal{M}_{VV'} = \mathcal{R}_1 \mathcal{T}_{12} \mathcal{R}_1$$

$$= \begin{pmatrix} 1 & 0 \\ \frac{-P_2}{n'_2} & \frac{n_2}{n'_2} \end{pmatrix} \begin{pmatrix} 1 & z_{12} \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ \frac{-P_1}{n'_1} & \frac{n_1}{n'_1} \end{pmatrix}$$

$n_1 = n \quad n'_2 = n' \quad n'_1 = n_2 = n_\ell$



Simple Lens Matrix

$$\begin{pmatrix} 1 & 0 \\ \frac{-P_2}{n'} & \frac{n_\ell}{n'} \end{pmatrix} \begin{pmatrix} 1 & z_{12} \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ \frac{-P_1}{n_\ell} & \frac{n}{n_\ell} \end{pmatrix}$$

The Thin Lens Again

Simple Lens Matrix

$$\begin{pmatrix} 1 & 0 \\ -\frac{P_2}{n'} & \frac{n_\ell}{n'} \end{pmatrix} \begin{pmatrix} 1 & z_{12} \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ -\frac{P_1}{n_\ell} & \frac{n}{n_\ell} \end{pmatrix} \xrightarrow{\quad} \mathcal{M}_{VV'} = \begin{pmatrix} 1 & 0 \\ -\frac{P_t}{n'} & \frac{n}{n'} \end{pmatrix}$$

$z_{12} = 0$ \nearrow $P_t = P_1 + P_2$

In General: $P_1 = \frac{n_\ell - n}{R_1}$ $P_2 = \frac{n' - n_\ell}{R_2}$

Glass in Air $P_1 = \frac{n_\ell - 1}{R_1}$ $P_2 = -\frac{n_\ell - 1}{R_2}$

Thin Lens in Air Again

$$P_1 = \frac{n_\ell - 1}{R_1} \quad P_2 = -\frac{n_\ell - 1}{R_2} \quad P_t = P_1 + P_2$$

$$\mathcal{M}_{VV'} = \begin{pmatrix} 1 & 0 \\ -P_t & 1 \end{pmatrix}$$

$$P_t = \frac{1}{f}$$

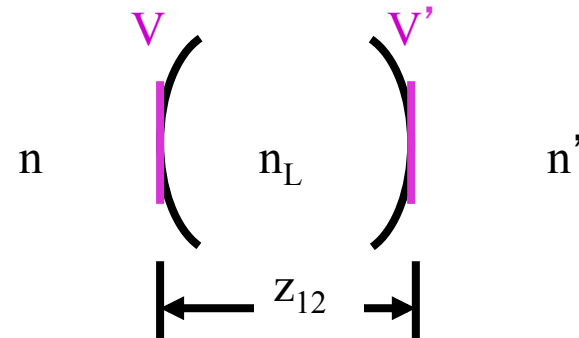
$$\frac{1}{f} = (n - 1) \left[\frac{1}{R_1} - \frac{1}{R_2} \right]$$

Thick Lens Compared to Thin

$$\begin{pmatrix} 1 & 0 \\ \frac{-P_2}{n'} & \frac{n_\ell}{n'} \end{pmatrix} \begin{pmatrix} 1 & z_{12} \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ \frac{-P_1}{n_\ell} & \frac{n}{n_\ell} \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ -\frac{P_t}{n'} & \frac{n}{n'} \end{pmatrix} + \frac{z_{12}}{n_\ell} \begin{pmatrix} -P_1 & n \\ \frac{P_1 P_2}{n'} & P_2 \frac{n}{n'} \end{pmatrix}$$

Thin Lens Plus Correction

$$\text{Geometric Thickness} = z'_{12} = \frac{z_{12}}{n_\ell}$$



Matrix example 1

Example #1, the Keck Telescope

$$R2 := \begin{pmatrix} 1 & 0 \\ \frac{-2}{-4.737} & -1 \end{pmatrix} \quad R1 := \begin{pmatrix} 1 & 0 \\ \frac{-2}{-34.972} & -1 \end{pmatrix} \quad T12 := \begin{pmatrix} 1 & -15.395 \\ 0 & 1 \end{pmatrix}$$

$$SYS := R2 \cdot T12 \cdot R1$$

$$SYS = \begin{pmatrix} 0.12 & 15.395 \\ -6.7 \times 10^{-3} & 7.5 \end{pmatrix}$$

$$f := \frac{-1}{SYS_{1,0}}$$

$$f = 149.245$$

$$R3 := \begin{pmatrix} 1 & 0 \\ \frac{-1}{2.286} & 1 \end{pmatrix} \quad R4 := \begin{pmatrix} 1 & 0 \\ \frac{-1}{0.307} & 1 \end{pmatrix}$$

$$T23 := \begin{bmatrix} 1 & (17.8469 + 2.286) \\ 0 & 1 \end{bmatrix} \quad T34 := \begin{pmatrix} 1 & 2.54 \\ 0 & 1 \end{pmatrix}$$

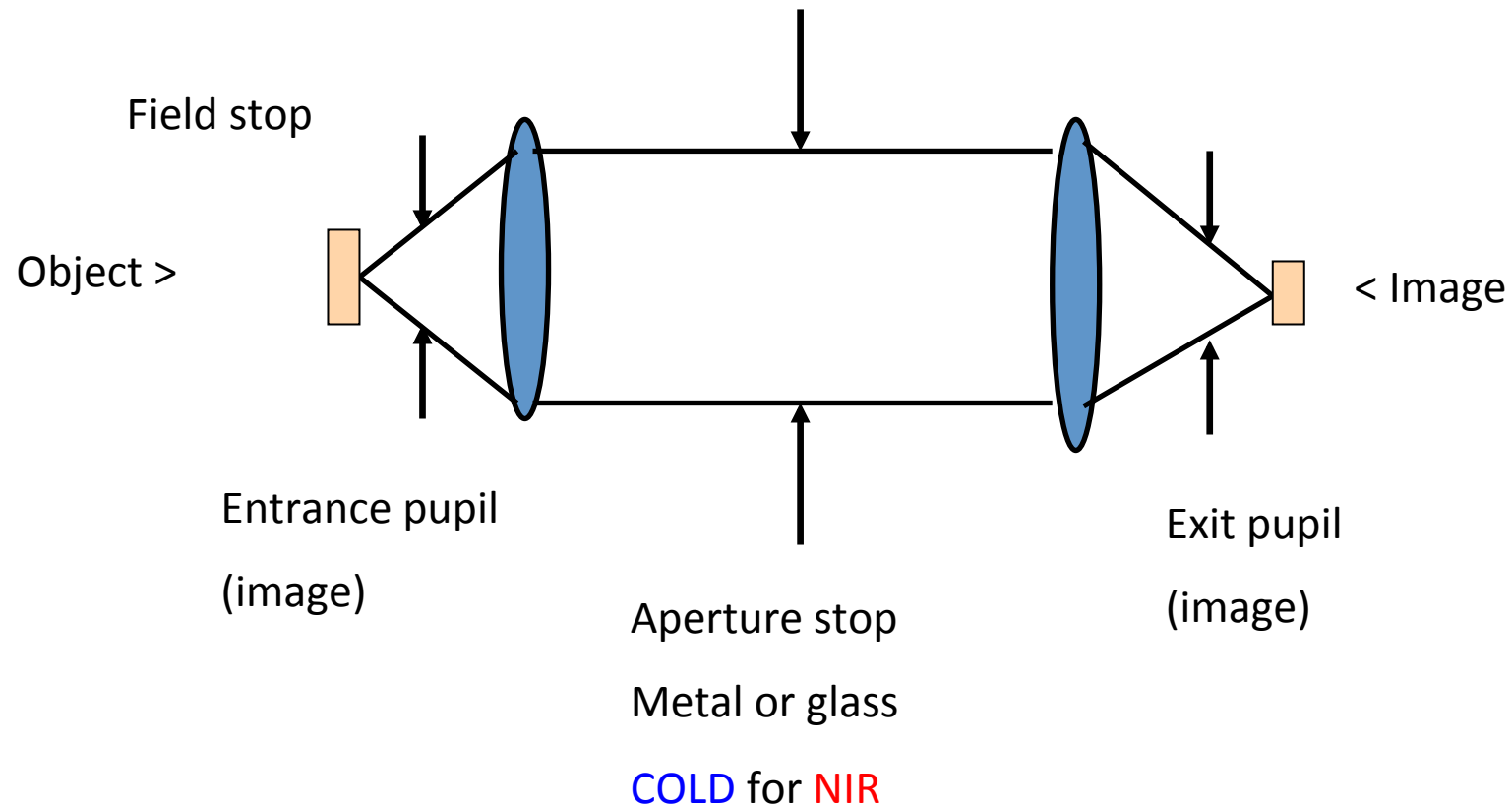
$$SYS2 := R4 \cdot T34 \cdot R3 \cdot T23 \cdot R2 \cdot T12 \cdot R1$$

$$SYS2 = \begin{pmatrix} -0.015 & 0.562 \\ 0.05 & -67.117 \end{pmatrix}$$

$$efl := \frac{-1}{SYS2_{1,0}}$$

$$efl = -20.043$$

Basic optics definitions



- Entrance Pupil is the image of the stop in all optics *upstream* of the stop.
- Aperture Stop, the physical aperture (metal, or lens edge) that limits the bundle of rays through the system for any field point. In Astronomy, this usually is the primary mirror for optical systems and the secondary mirror for NIR systems, not always . For NIR systems this is usually imaged onto a cold aperture somewhere inside the Dewar. (often with an Offner relay, (A. Offner, Opt. Eng 14, 131, 1975))
- Exit pupil is the image of the stop in all optics *downstream* of the stop.

Cameras

- Reflective
 - Two Mirror correct for spherical and coma
 - Un-obscured 3-mirror an-astigmat corrects for spherical, coma and astigmatism, (Paul-Baker, Merseinne Schmidt) (i.e Angel, Woolf and Epps, 1982 SPIE, 332, 134A)
- Transmissive
 - Epps cameras
- Catadioptric
 - Schmidt

Reflective Cameras

- Pro's

- Off axis unobscured
- Diamond turning is an option for NIR (visible), aspheres can be implemented inexpensively
 - Post polish for visible, nickel over aluminum
- Metal mirrors, good thermal characteristics, can have mounts machined in
- Fewer surfaces, better emissivity?

- Con's

- Surface roughness > scattered light
- Hard to align
- Hard to diagnose

Transmissive Cameras

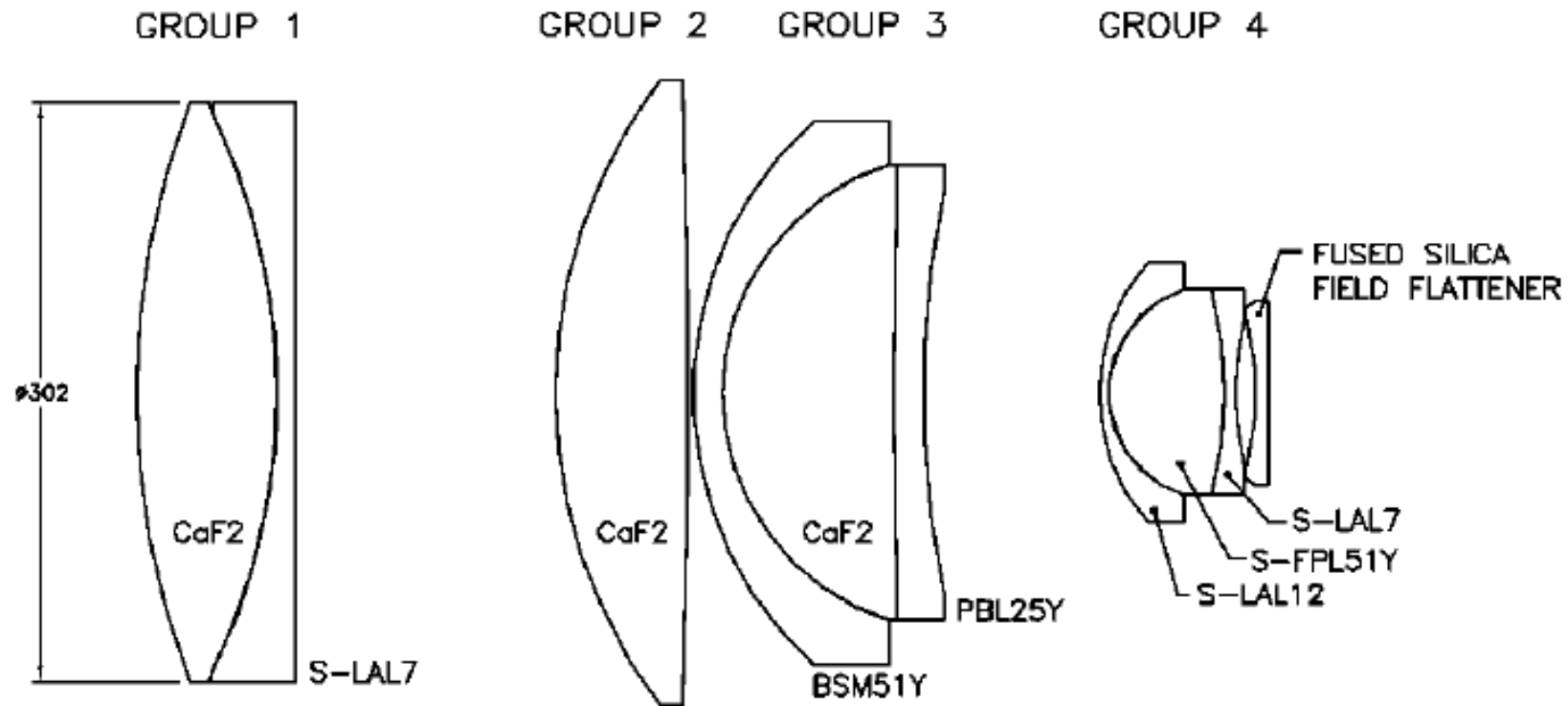
- Pro's

- Unobscured,
- All-spherical, or rotational symmetric aspheres on glass (by hand, expensive)
- Diamond turning is an option for NIR (visible?), aspheres can be implemented expensively on limited number of materials usually crystals (CaF₂, BaF₂, ZnSe, Germanium, Silicon)
- Alignment and diagnostics are easier.

- Con's

- Mounting is harder, athermalization is harder
- Surface roughness > scattered light off aspheres

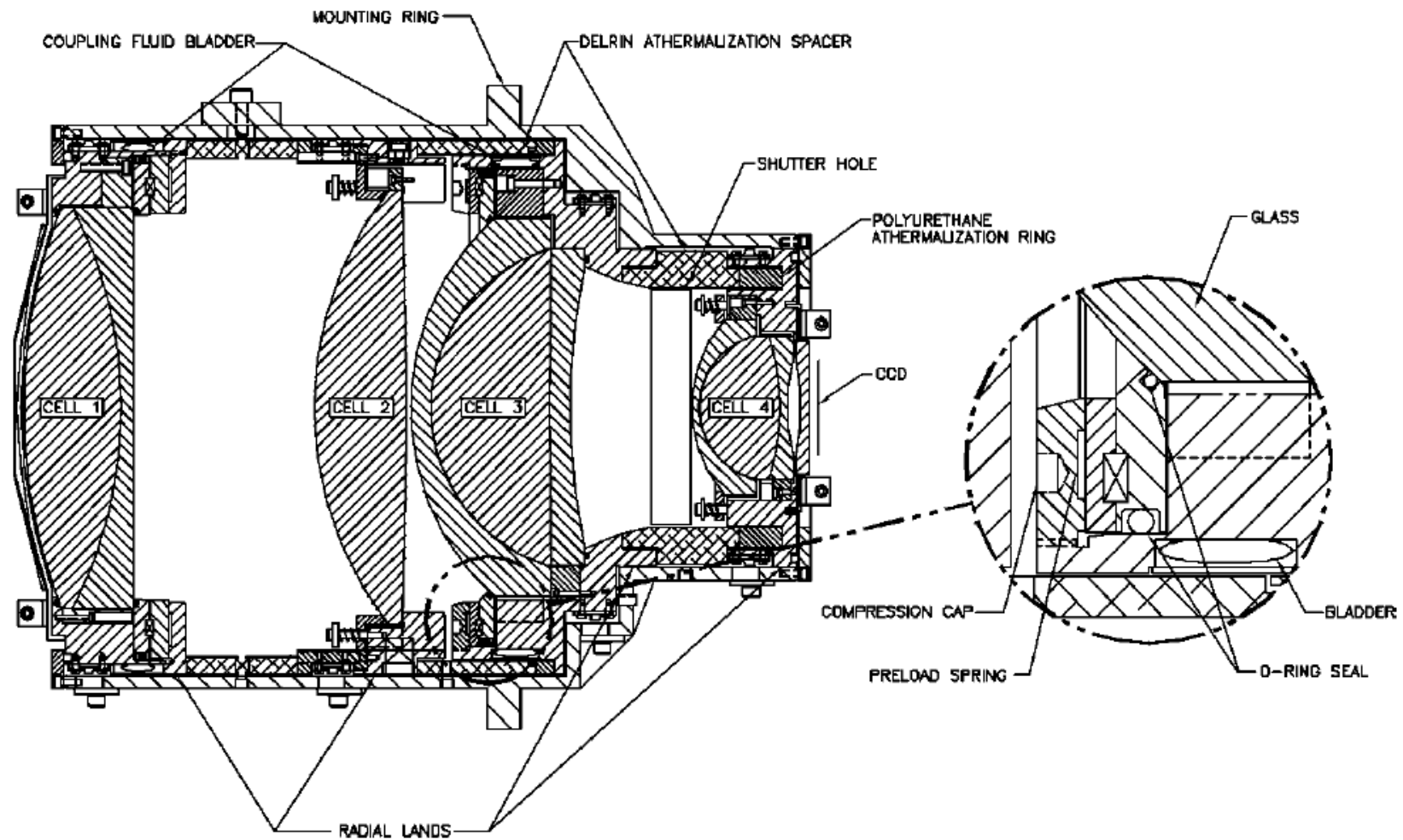
ESI Refractive camera



Epps and Miller, 1999SPIE Vol. **3355**, 255b

Epps, 1999SPIE Vol. **3355**, 111e

ESI Refractive camera



Sheinis et al, *Proc. SPIE* Vol. **3786**, p. 413-426.1999.

Catadioptric Cameras

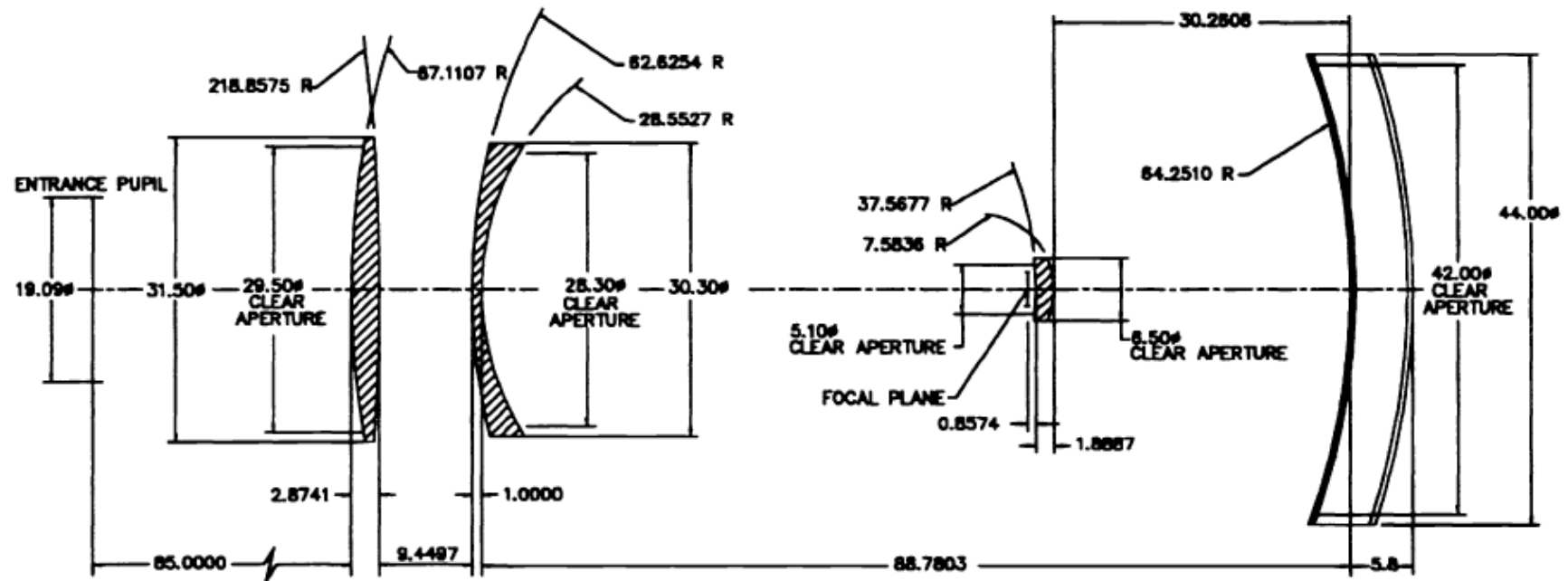
- Pro's

- Schmidt cameras variations provide wide field coverage in straightforward design
- Few surfaces
- Can be all-spherical

- Con's

- Obscurations
- Hard to mount detectors
- Smaller effective field size.

Hires, Catadioptric Camera



ALL DIMENSIONS ARE IN INCHES

ALL SPHERICAL SURFACES

End lecture 1