Characterisation of hexabundles: Initial results

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ABSTRACT

New multi-core imaging fibre bundles – hexabundles – being developed at the University of Sydney will provide simultaneous integral field spectroscopy for hundreds of celestial sources across a wide angular field. These are a natural progression from the use of single fibres in existing galaxy surveys. Hexabundles will allow us to address fundamental questions in astronomy without the biases introduced by a fixed entrance aperture. We have begun to consider instrument concepts that exploit hundreds of hexabundles over the widest possible field of view. To this end, we have characterised the performance of a 61-core fully fused hexabundle and 5 unfused bundles with 7 cores each. All fibres in bundles have 100 micron cores. In the fused bundle, the cores are distorted from a circular shape in order to achieve a higher fill fraction. The unfused bundles have circular cores and five different cladding thicknesses which affect the fill fraction. We compare the optical performance of all 6 bundles and find that the advantage of smaller interstitial holes (higher fill fraction) is outweighed by the increase in FRD, cross-talk and the poor optical performance caused by the deformation of the fibre cores. Uniformly high throughput and low cross-talk are essential for imaging faint astronomical targets with sufficient resolution to disentangle the dynamical structure. Devices already under development will have 100-200 unfused cores, although larger formats are feasible. The light-weight packaging of hexabundles is sufficiently flexible to allow existing robotic positioners to make use of them.

Key words: instrumentation: miscellaneous:hexabundles – techniques: miscellaneous - methods: observational - instrumentation: spectrographs - techniques: imaging spectroscopy.

1 INTRODUCTION

Current and planned cosmological surveys in the optical and infrared have fundamental limitations. Multi-fibre [e.g.: 2dF(Colless et al. 2001) and SDSS(York et al. 2000)] and multi-slit [e.g.: DEIMOS(Faber et al. 2003) and VIMOS(Le Fevre et al. 2003)] surveys have or will amass large catalogues of galaxies in order to deduce their global properties. However these suffer from biases introduced when a fixed angular size aperture such as a single fibre is used to observe galaxies, irrespective of the size, distance or morphology (see for example, fig.8 in Ellis et al. 2005). On the other hand, integral field units (IFUs) or image slicers such as SINFONI (Eisenhauer et al. 2003) and NIFS (McGregor et al. 2003) spatially sample the spectra, giving morphological and dynamical information. However, current IFUs are restricted in the number of objects that can be observed. The ideal is to combine multi-object spectroscopy (MOS) positioning technology with IFUs. Hexabundles can do exactly that.

Hexabundles have up to many hundreds of closelypacked fibres to allow spatially resolved spectroscopy. They have several practical advantages. Firstly, they are not as sensitive as single-fibre devices to seeing and positioning errors and are unaffected by seeing losses. Secondly, they can be used with AO-corrected or natural seeing and in the optical or infrared. Thirdly, there is no need for microlens arrays, and the plate scale can be changed simply with a single macro lens. Fourthly, they can be used with conventional fibre positioning technology as imaging bundles to obtain spatial information in a survey of many thousands of galaxies. The resulting scientific gains over existing large galaxy surveys would then include the ability to investigate AGN triggering and feedback including outflows, galaxy merger rates and merger-induced processes, the substructure in gravitational lenses, stellar populations and abundance gradients, as well as tracing the build up of dark matter, stellar mass and angular momentum in galaxies. Decomposition of bulge and disk components would be possible for thousands of galaxies. Hexabundles are particularly effective for galaxies with asymmetries, multiple components, mergers and sub-

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structures including high redshift galaxies that are not yet formed into spheroids or disks but consist of clumpy merging components which would be poorly sampled with a single fibre spectrum. Differential binning of the fibres can also be applied, particularly for more distant objects where the brightness decreases rapidly away from the nucleus.

A 100,000 galaxy survey out to a redshift of 0.2 will be possible with hexabundles in the proposed FIREBALL instrument on ESOs Very Large Telescope (VLT). Currently the FLAMES instrument uses OzPoz positioners to place 132 single fibres across a 24' field, which then feed into the GIRAFFE spectrograph. The proposed FIREBALL upgrade would involve fifty hexabundles, each sampling ~ 0.42" with around 100-cores.

Hexabundles are not limited in the number of cores in each bundle, beyond the physical size of the bundle holder. So far we have made bundles up to 61 cores, but larger devices of several hundred cores would be suitable for multiobject positioners. In anticipated applications, the core will have 0.4 - 0.7'' per core. Then 61-core and 367-core bundles would have imaging areas of 4 - 6'' and 9 - 15'' respectively. The main trade-off with the design of hexabundles is to have the largest fill-fraction (ratio of core area to total bundle area) possible without compromising the optical performance. The fill-fraction is affected by both the cladding thickness and how the fibres are packed together. Fibres that are fused together have fewer gaps between cores giving a fill-fraction of over 90%, but are significantly distorted from a circular shape. On the other hand, unfused fibres remain circular but have larger gaps between them, resulting in fillfractions less than 87%.

This paper describes the performance tests of our first fused and unfused hexabundles. Details of the development and manufacture of the hexabundles is discussed in Bland-Hawthorn et al. (2010).

2 HEXABUNDLE DEVICES

Six new hexabundle devices have been characterised. In each device, one end has multimode fibres fused into a single element, which is the hexabundle, while the fibres at the other end are loose. The fibres used in each bundle have numerical apertures (NA) of 0.22. The first of these hexabundles consists of 61 fully fused fibres without interstitial holes (Fig. 1) giving a fill-fraction of > 90%. However, all but the central fibre are significantly distorted from a circular shape. The fibres are 4.5 m long and each fibre had core and cladding diameters of 105 microns and 125 microns respectively, before the cladding was etched away over a 2 - 3 cm length where the fibres were then fused (further details of the manufacturing process can be found in Bland-Hawthorn et al. 2010). The resulting hexabundle has a diameter of ~ 900 micron. On output, the 61 fibres are lined up in V-grooves between glass plates with three rows of 15 and one row of 16 fibres. The fibres in the same glass plate are separated by 500 microns.

The remaining five hexabundles have seven unfused fibres (with small interstitial holes) with cladding thicknesses of 1, 2, 4, 6 and 8 microns. The main differences to the previous bundle are that the fibres are circular rather than distorted in shape (see Fig. 2), resulting in lower fill-



Figure 1. The 61-core fused hexabundle with core numbers marked. Cores 1 - 16, 17 - 31, 32 - 46 and 47 - 61 were grouped together at output on four glass plates. Each of the cores are 100 microns in diameter. The cores are distorted from circular in order to increase the fill-fraction.

fractions. In these bundles, the output fibres are loose and were mounted into 35 parallel V-grooves on a plate. We aim to investigate the effect of circular cores on the optical performance and consider the trade-off with fill-fraction. The different cladding thicknesses are used to assess the ideal balance between minimising cross-talk while maximising fillfraction.

3 EXPERIMENT METHOD AND DATA REDUCTION

Each of the bundles were tested for cross-talk, throughput and focal ratio degradation (FRD). It was crucial for the cross-talk tests in particular, to ensure that no stray light was getting into any core other than the intended target. Originally laser light was focussed into the individual fibre (output) end of the fibres while the hexabundle end was imaged with the camera. This has the advantage that the fibres could be separated so that no stray light from the laser could go into adjacent fibres. However, the light coming out of the multimode fibres at the hexabundle has a speckle pattern that is larger than the size of the core. This is because the different modes focus in slightly different planes outside of the polished bundle face so that all of the light out of the fibre cannot be focussed at the same time, resulting in an imaged spot size that has an apparent diameter of approximately 125% of the core diameter. An example of this effect is shown in Fig. 3. This made it impossible to do photometry on the different fibres in the resulting image in order to measure cross-talk.

The final method adopted, as shown in Fig. 4, used an Oriel LED light source which was focussed into a 50 micron core fibre with a 60 micron diameter including cladding. This fibre was then butt-coupled to the 100 micron hexabundle



Figure 2. The 7-core unfused hexabundles, shown with different magnifications. The left-hand column gives the cladding thickness after etching, while the right-hand column lists the core-to-core separation. The images shown here are before the interstitial holes were filled with soft, low refractive index glue. In each of these bundles the cores are 100 microns diameter. These unfused bundles are each the same size as the central 7 cores of the 61-core bundle shown in Fig. 1.

cores (reversing the direction of the light through the fibres compared to the previous method - this is the direction the hexabundles will be used in astronomical applications). We mounted the butt-couple (input) fibre in a V-groove on a narrow plate that was attached to a tilt/rotation stage off to the side so that the fibre could be adjusted to align perpendicular to the hexabundle face. The narrow plate could then slot in from the side between the hexabundle and a microscope with the fibre bending abruptly away to the side. This allowed the microscope to be positioned close enough to image the hexabundle and input fibre at high enough magnification to be sure the input fibre was centred on a chosen fibre core within the hexabundle. The input fibre needed to be less than 100 microns from the hexabundle face to prevent light straying into adjacent fibres. The small outer diameter of the butt-coupled fibre was essential in order to not obscure the view of the hexabundle cores. Two other microscopes mounted above and side-on were used to ensure

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Figure 3. When coherent light is input into the output multimode fibres of a hexabundle, the light coming out of the hexabundle has a speckle pattern that at best focus, appears larger than the core of the fibre. credit: Peter Skovgaard.

that the fibre was perpendicular to the hexabundle face in both axes. The output fibres were each imaged through a pair of large camera lenses onto an SBIG camera. A micrometer stage allowed the camera to be shifted to a specific back-focus position.

For all the measurements, the LED source light level was kept constant. Each measurement was done twice, once with a Bessel blue filter (centred on 0.45 microns) then with a Bessel red filter (centred on 0.65 microns) between the LED source and the focussing assembly. Time variation in the input light intensity plus variations in the SBIG camera response, were quantified with repeated images through one core of the bundle at time periods ranging from second to hours. The maximum variation in resulting integrated counts was < 1.0% with typical values of ~ 0.2%.

The throughput of every fibre in each bundle was measured by centring the input light on each fibre. For cross-talk measurements, the light was centred on a core while the surrounding fibres were imaged. FITS images from the SBIG camera were processed using the IRAF astronomical data reduction software (Tody 1986). Firstly each image was flat fielded. Then the total integrated counts were measured in IRAF RADPROF by fitting the barycentre of the fibre image and selecting a fixed aperture size for all fibres that was large enough to include all the output from the fibre. The target fibre and the surrounding fibres were measured through the same size aperture.

Focal ratio degradation (FRD) causes the opening angle of the output beam to be larger than that of the input beam. The FRD will vary with the angle of the input beam. Therefore we have used an input beam that fills the NA of the fibres, and then measured the energy distribution across the output image in the back-focal plane. Worse FRD will result in a wider encircled energy distribution (see Fig. 5).

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Figure 4. Equipment setup to test the hexabundles. Clockwise from top left: The light from an LED source passes through a filter holder and is focussed into a 50 micron core fibre. This fibre is butt-coupled in turn to each core of each hexabundle. The five metal tubes lined up are the unfused 7-core hexabundles (the fused 61-core hexabundle was in the same position when being tested). An xyz stage allows the bundle cores to be accurately aligned with the butt-couple fibre. An alignment microscope allows us to see which hexabundle core the input fibre is butt-coupled to. A top and side microscope are used to check the butt-couple fibre is within 100 microns of the bundle face. The view from the top microscope is inset, showing the butt-couple fibre aligned with a hexabundle. The second butt-couple fibre in this image was a spare, and not used. Each of the 5 bundles has 7 fibres coming out, giving 35 fibres mounted in V-grooves 2 mm apart on an xyz stage. However, when the fused bundle was being tested, the 61 output fibres were aligned on four glass plates on the xyz stage. The output fibres are imaged through a pair of matching lenses onto a camera.

The camera was shifted to a known back-focal distance; selected to give sufficient pixels across the output fibre image to accurately fit an encircled energy profile. Using the known pixel size of the camera, an NA value was calculated from $\sin \theta$ of the cone angle. This gives the effective output NA at each point across the image of the fibre. After flat fielding, IRAF RADPROF was used to fit the centre position along with the background and peak counts in each image profile. These initial values were then input into IRAF PPROFILE, and the radially-collapsed encircled energy profile was fit interactively. An iterative procedure was used to determine the background value to subtract and the peak counts in the profile until the background was flat and the encircled energy levelled at 100%. The encircled energy values could then be matched to the NA calculated for each radial pixel position in the image. The resulting plots of NA vs encircled energy will therefore be shifted to the right for a larger output cone angle, indicating worse FRD.

4 61-CORE HEXABUNDLE PERFORMANCE

4.1 Encircled energy profiles

The encircled energy profile of each of the 61 fibres was measured against the output NA. Fig.6 shows the encircled energy profiles through both the Bessell blue $(0.45\mu m)$ and red $(0.65\mu m)$ filters. The profiles through the red filter are at a lower NA than those through the blue filter because the shorter wavelengths have more modes and therefore a higher NA. While the average profiles of 16 cores get worse as the range of core numbers gets further from the bundle centre, there is a very large variation in encircled energy profiles from fibre-to-fibre, which will give inconsistent performance across the bundle for imaging and spectroscopy. In order to quantitatively compare the encircled energy profiles, the drop in encircled energy compared to the central fibre was calculated for a nominal NA of 0.20. The resultant drop in encircled energy ranges from less than 1% up to more than 25% for different fibres in the bundle. At 90% encircled energy, the up-conversion of NA is 0.10 for the worst fibre in both the blue and red filters.

To see if the deformation of each fibre affects the encircled energy profiles, the deformation was measured by fitting circles to the image shown in Fig. 1. The largest circle that does not include any cladding, and the smallest circle that includes all the core were fit to each core. The ratio of the diameters of these circles was used to define a 'deformation ratio'. While this measure is subjective, the fibres with the highest deformation ratio tend to have the largest encircled energy drop, indicating the worst FRD as shown in Fig. 7.



Figure 5. FRD increases the output cone angle θ . Therefore the comparative FRD in the fibres within a bundle can be assessed from plots of encircled energy vs numerical aperture (NA), where NA is $\sin\theta$. Worse FRD shifts the profile to the right (dashed line).



Figure 6. Fused fibre bundle results. (Top) The encircled energy vs numerical aperture (NA) at output for the central fibre (solid line) and the average of all the core numbers 1 - 16, 17 - 31, 32 - 46 and 47 - 61 (short dashed, long dashed, dotted, dash-dot respectively) (Bottom) The same profiles but for the individual fibres 1 - 16, to show the scatter around the average values. The plots on the left are through the blue $(0.45\mu m)$ filter and those on the right are through the red $(0.65\mu m)$ filter. The arrow indicates how we defined encircled energy drop from the central fibre to the worst fibre.

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4.2 Cross-talk and throughput

Cross-talk was measured for 14 random fibres in the bundle by measuring the integrated counts in each adjacent fibre while the light was centred on the target fibre. The loss was not equally distributed into the adjacent fibres, with most target fibres showing the majority of the cross-talk into one or two of the adjacent fibres while in some cases the counts were more than 100 times lower in other adjacent fibres. This was due partly to significant differences in the contact area and cladding width between different fibres. Such differences arise from the distortion of the fibres in the fused bundle. The total loss into adjacent fibres was predominantly in the range of 0.11 - 1.2% (0.005-0.06dB) with one fibre at 4.2%with the blue filter, and one at 4.4% (0.2dB loss) in the red filter. The total cross-talk could not be evaluated in the outer row of the hexabundle because we have shown that the loss is unevenly distributed to adjacent fibres and therefore could not be assessed where there were no adjacent fibres on the outer edge. As the outer row of fibres include some of the most distorted profiles, the total cross-talk is likely to be above 0.2dB for some of those fibres. For example, the cross-talk from fibre 56 into just 55 and 57 is already a total of 0.17dB alone and therefore would be much higher if the losses could be measured on all sides.

In Fig. 7 there is an anti-correlation between the drop in encircled energy (FRD) and the throughput, indicating that the fibres with less throughput have the worst FRD. With the exception of one fibre with very high cross-talk, that performed differently to the others in every test, the encircled energy drop was also correlated with cross-talk. It can also be seen that the throughput varied by a factor of five between each of the 61 cores which would have an impact on the accuracy of photometry in extended astronomical sources. It is clear that the more distorted fibres have lower throughput, worse cross-talk and higher encircled energy drop (indicating worse FRD).

4.3 Cladding scatter

It was also noticed that when the input light was directed at the cladding between fibre cores, that light was then dispersed through the entire bundle. In an astronomical application, the component of an extended source that hit the cladding would result in all positional information being lost and the spectrum of that component of the object being added to every fibre across the field. By centring the light on the cladding between fibres 11 and 12, then measuring the counts in 6 fibres that were not adjacent, the counts were 0.1 - 0.2% of the counts in fibre 12 when the light was directed into fibre 12. Fibre 12 was chosen because the throughput counts in that fibre are average compared to the counts in each of the other 61 fibres. Based on an estimate of the cladding area covered by the light in this test compared to the total cladding area, up to 25% of the light in any one fibre could be scattered from cladding elsewhere in the bundle. This fraction would lead to unacceptable confusion in the spectroscopic imaging of an extended astronomical source.

The original aim of fully-fusing the bundle was to increase the fill-fraction to > 90%. However, based on this performance, the gain in coverage across an object being

imaged is outweighed by the confusion in the spatial origin of the light at the spectrograph due to cross-talk and cladding scatter. Also, inaccuracies in photometry will result from the extreme differences in throughput across an image.

The next step was to consider the improvement in this performance if the hexabundle was not fused so that the fibres remain circular at the expense of a slightly smaller fill-fraction.

5 PERFORMANCE OF THE 7-FIBRE NON-FULLY-FUSED HEXABUNDLES

We had five hexabundles made with cores that are unfused. These have the advantage that the fibres are not distorted and therefore should perform better. In order to compare cross-talk for a given fill-fraction, they were made with cladding thicknesses of 1, 2, 4, 6 and 8 microns (see Bland-Hawthorn et al. 2010, for a discussion on the issues surrounding the manufacture of bundles with these cladding thicknesses). The aim was to test how thin the cladding could be before the losses became too large.

5.1 Encircled Energy profiles

Fig. 8 shows the encircled energy profiles for the unfused bundles. The profiles of each of the 7 cores in the 2, 4 and 8-micron clad bundles agree within errors, indicating consistent FRD performance across the bundle. This is in contrast to the large variation between cores in the fused bundle (see Fig. 6). Each of the profiles in Fig. 8 have lower NA than the central fibre (best FRD) of the fused bundle, indicating better FRD in the unfused bundles. The 1 micron cladding bundle has a distribution of encircled energy profiles for the 7 cores that is slightly larger than errors, which may be due to mode coupling induced by the higher cross-talk. In this case the central core has worse NA than the other cores as would be expected from mode coupling based on the symmetry of the bundle.

5.2 Cross-talk and throughput

For each of the unfused hexabundles, the throughput was measured for each of the 7 fibres, and the cross-talk was measured by losses into the surrounding 6 fibres when light was directed down the central core.

Table 1 shows the cross-talk performance through the B- and R-band filters compared to the fill-fraction. While the hexabundles with 4, 6 and 8-micron clad fibres had no cross-talk down to the limit we could measure in our images, they also have a lower fill-fraction. The cross-talk was worse for the 1 micron clad bundle than for the 2 micron clad bundle, as expected. In the anticipated uses of these hexabundles (eg: FIREBALL) the fibres would be 0.4 - 0.7''/core. For 0.4'' cores, in average seeing at an excellent telescope site of 0.8'', 95% of the power from the seeing disk would be in one core, with 5% in the adjacent cores. Therefore we would want the total cross-talk into adjacent cores to be less than a tenth of that and hence we aim for a maximum cross-talk of 0.5%. The 2-micron clad fibre do not. In the



Figure 7. Fused fibre bundle results. Drop in percentage encircled energy compared to the central fibre vs total cross-talk (top left), throughput (top right) and deformation ratio (bottom left). Deformation ratio vs cross-talk (bottom right). In all panels the dot and triangle are for the R-band (0.65 μ m) and B-band (0.45 μ m) respectively.

Table 1. Total cross-talk from the central fibre into all of the 6 surrounding fibres is listed as both a percentage of the integrated counts in the central fibre and as a dB loss. Values are shown for the blue B-band and the red R-band Bessel filters. The first column lists the cladding thickness, then the fill-fraction (ratio of core area to total bundle area) is given for each cladding thickness. Limits listed are set by the image detection thresholds in cases where no emission was detected.

Clad	Fill	Cross-talk		
	fract.	$B (0.45 \mu \text{m})$	$R (0.65 \mu m)$	
(μm)		% (dB in brackets)		
1	0.87	1.4 (0.06)	4.76(0.21)	
2	0.84	0.25(0.011)	0.39(0.017)	
4	0.78	$< 0.01 \ (< 0.003)$	$< 0.01 \ (< 0.003)$	
6	0.72	$< 0.01 \ (< 0.003)$	$< 0.01 \ (< 0.003)$	
8	0.67	$< 0.01 \ (< 0.003)$	$< 0.01 \ (< 0.003)$	

infrared, longer wavelengths will cause the cross-talk to be worse and thicker cladding would be required, but this has not yet been measured.

When the light was directed at the cladding, there was no detectable transmission of that light into all the cores as was seen in with the "cladding scatter" in the fused bundle (see section 4.3). For the two bundles for which the cross-talk was measurable above the noise limit, the variation in the cross-talk values for the 6 surrounding fibres was at worst a factor of 4. This is significantly lower than the factor of > 100 we found for the 61-core fused hexabundle. We attribute this to the uniformly circular fibres in the unfused bundles which have equal contact areas with adjacent cores.

The even, circular-nature of the fibres in the unfused bundles has also resulted in a much more uniform throughput from fibre-to-fibre. In Fig. 7 the variation in throughput between different fibres in the fused bundle was up to $\sim 500\%$. However, the unfused bundles showed at worst 24% variation between fibres in any bundle for a given filter. Typically the variation was a lot less than this, as shown in Fig. 9.

6 FIRST ON-SKY TESTS

A 1×61 fused fibre bundle has been retrofitted to a spectrograph on the Morehead 0.61 m telescope at the University of North Carolina. The 61 output MMFs were spread across 4 slit blocks that illuminate the collimator directly. The dispersed spectra were imaged onto a cooled CCD with 9μ m pixels which were binned 2×2 . The peak QE is ~ 50% at 450nm. The spectrum of the bright dawn sky in Fig. 10, clearly shows the Fraunhofer spectrum in absorption. The



Figure 8. Unfused fibre bundle results. The encircled energy vs numerical aperture (NA) at output for the unfused bundles with 1, 2, 4 and 8 micron cladding thicknesses. Results through the B-band and R-band filter are in the left and right columns respectively. A short horizontal line at NA=0.15 indicates the measurement error in the profiles at that NA, primarily due to focussing the output from each multimode core onto the camera.

nominal $0.1\,\mathrm{nm}$ spectral resolution is not degraded by the hexabundle.

7 CONCLUSION

We have compared the performance of a 61-core fused hexabundle to that of 5 unfused bundles with varying cladding thickness. The distortion of the cores in the fused bundle was found to significantly increase cross-talk, reduce throughput and increase FRD. The throughput varied by a factor of 5 between different cores in the bundle, while the cross-talk reached over 4% in the worst core. The up-conversion in NA from the best (central) core to the worst was 0.1 at 90% encircled energy. The performance of the unfused cores was better in every respect, and we attribute that to the circular cores. The throughput varied by at most 24% and the FRD results were consistent between the 7 cores in each bundle within errors. After comparing the cross-talk to the cladding thickness, we found that 2 micron cladding met the specification.



Figure 9. Unfused fibre bundle results. Normalised integrated counts (throughput) for each of the 7 fibres in the hexabundles with 2 micron and 8 micron cladding thicknesses. Results for the R-band and B-band are shown as dots and triangles respectively, and are normalised to different values to offset them for clarity.



Figure 10. The 2-D and 1-D extracted spectra from the first onsky tests of our hexabundles. The 2-D spectrum has the spatial direction on the vertical axis, and wavelength along the horizontal axis. The spectrum is of the dawn sky.

cation of < 0.5% cross-talk in the R- and B-bands while still having a fill-fraction of 84%. While the fill-fraction of the fused bundle is > 90%, the superior optical properties of the unfused bundles outweighed the gain in fill-fraction.

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