

A “Polywell” $p+^{11}\text{B}$ Power Reactor

Joel G. Rogers, Ph.D.
rogersjg@telus.net

Aneutronic fusion is the holy grail of fusion power research. A new method of operating Polywell was developed which maintains a non-Maxwellian plasma energy distribution. The method extracts down-scattered electrons and replaces them with electrons of a unique higher energy. The confined electrons create a stable electrostatic potential well which accelerates and confines ions at the optimum fusion energy, shown in the graph below. Particle-in-cell(PIC) simulations proceeded in two steps; 1) operational parameters were varied to maximize power balance(Q) in a small-scale steady-state reactor; and 2) the small scale simulation results were scaled up to predict how big a reactor would need to be to generate net power. Q was simulated as the ratio of fusion-power-output to drive-power-input. Fusion-power was computed from simulated ion density and ion velocity. Power-input was simulated as the power required to balance non-fusing ion losses. The predicted break-even reactor size was 13m diameter. Bremsstrahlung losses were also simulated and found manageable.

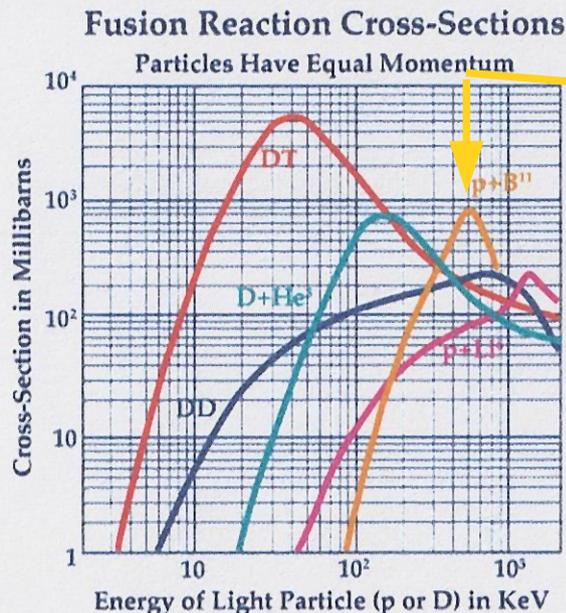


Figure 5 — Typical Fusion Reaction Cross Sections

The yellow line is for the cross section of $p + ^{11}\text{B}$ aneutronic fusion, whose peak cross section is at 560 KV. It is impossible to achieve this energy with a plasma having with a Maxwellian energy distribution since most of its electrons and ions are emitting Bremsstrahlung radiation. *(This radiation is caused by the acceleration of a charged particle, such as an electron, when deflected by another charged particle, such as an atomic nucleus.)*

Robert W. Bussard, “Should Google Go Nuclear”,
<http://askmar.com/Fusion.html>, November, 2006

Fig. 2 - "Polywell" Patent Pending

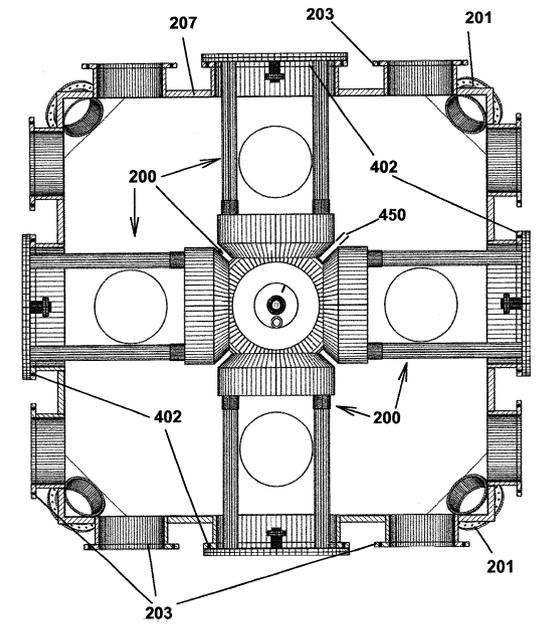
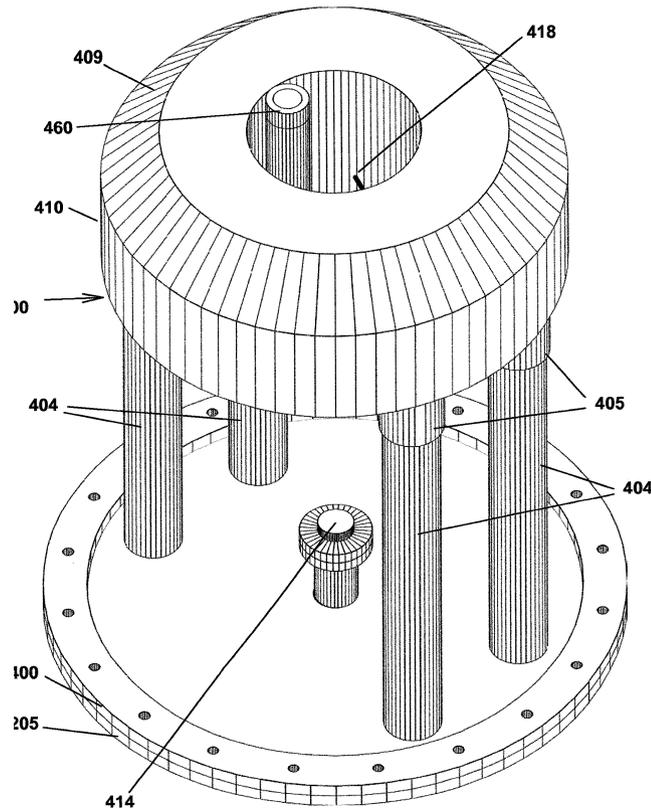
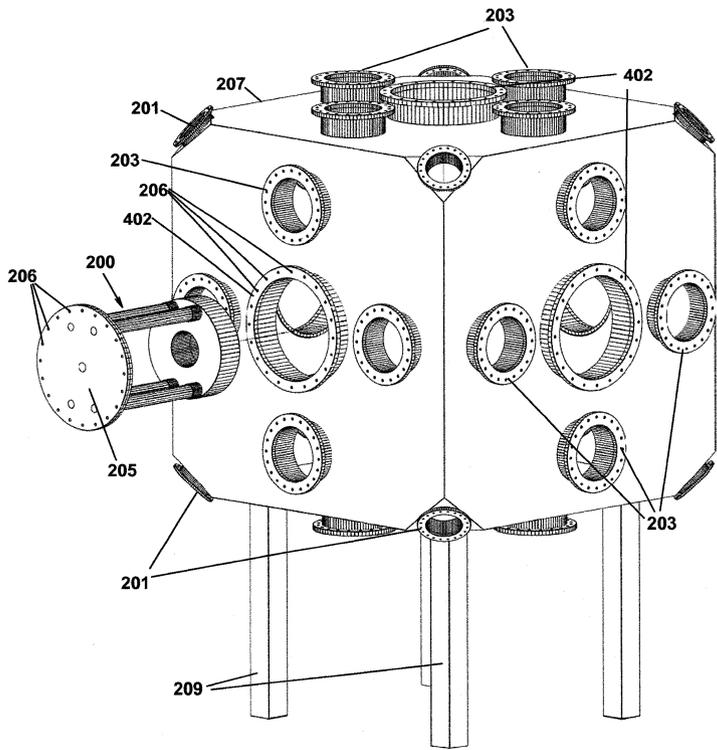


Fig. 3 - PIC Simulation Flowchart

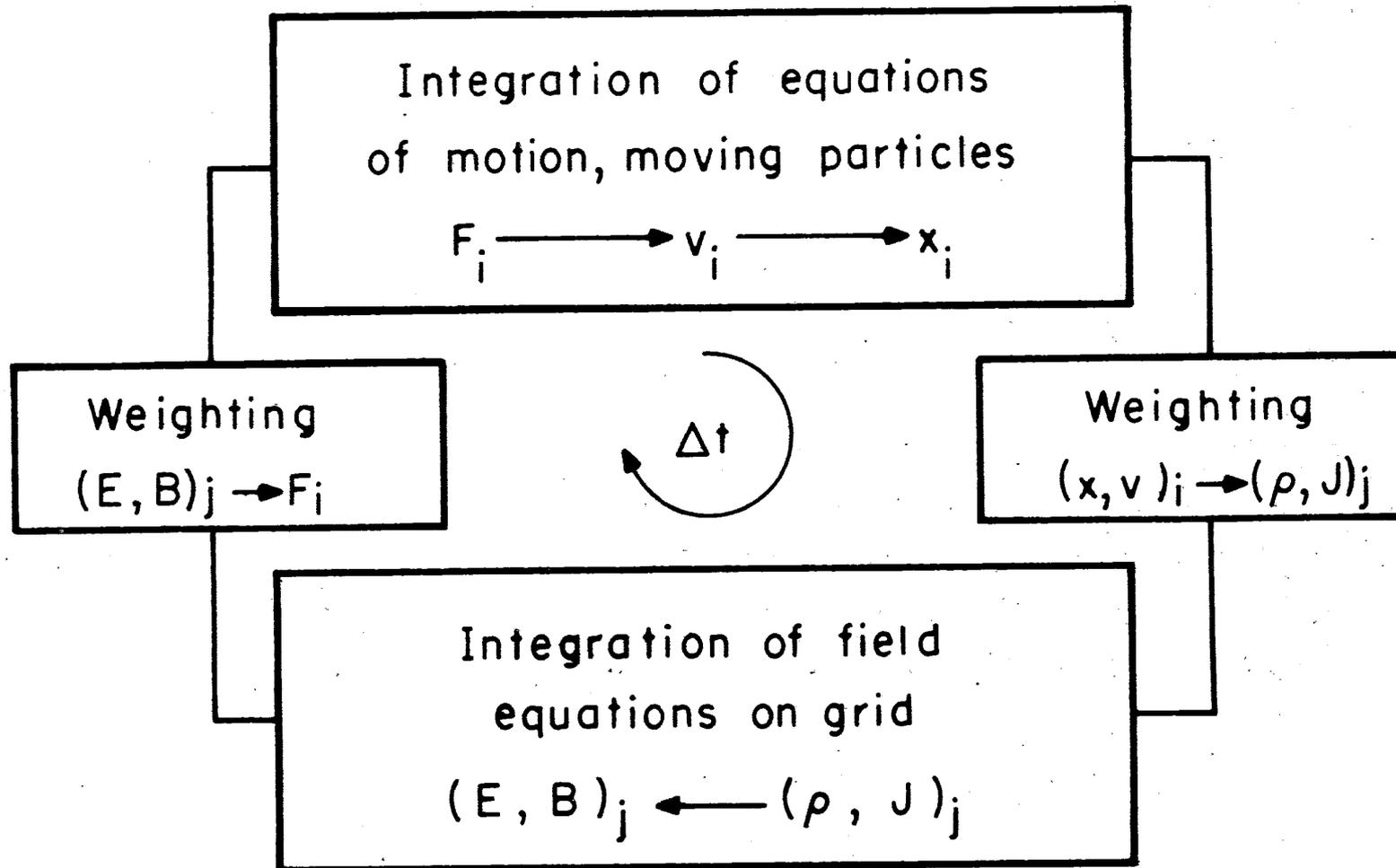


Figure 2-3a A typical cycle, one time step, in a particle simulation program. The particles are numbered $i = 1, 2, \dots, NP$; the grid indices are j , which become vectors in 2 and 3 dimensions.

The Figure(above) and caption were scanned from the textbook, Birdsall and Langdon, "Plasma Physics via Computer Simulation", McGraw Hill, New York, 1985, pg. 11.

Fig. 4 - Electrons' 2D Positions

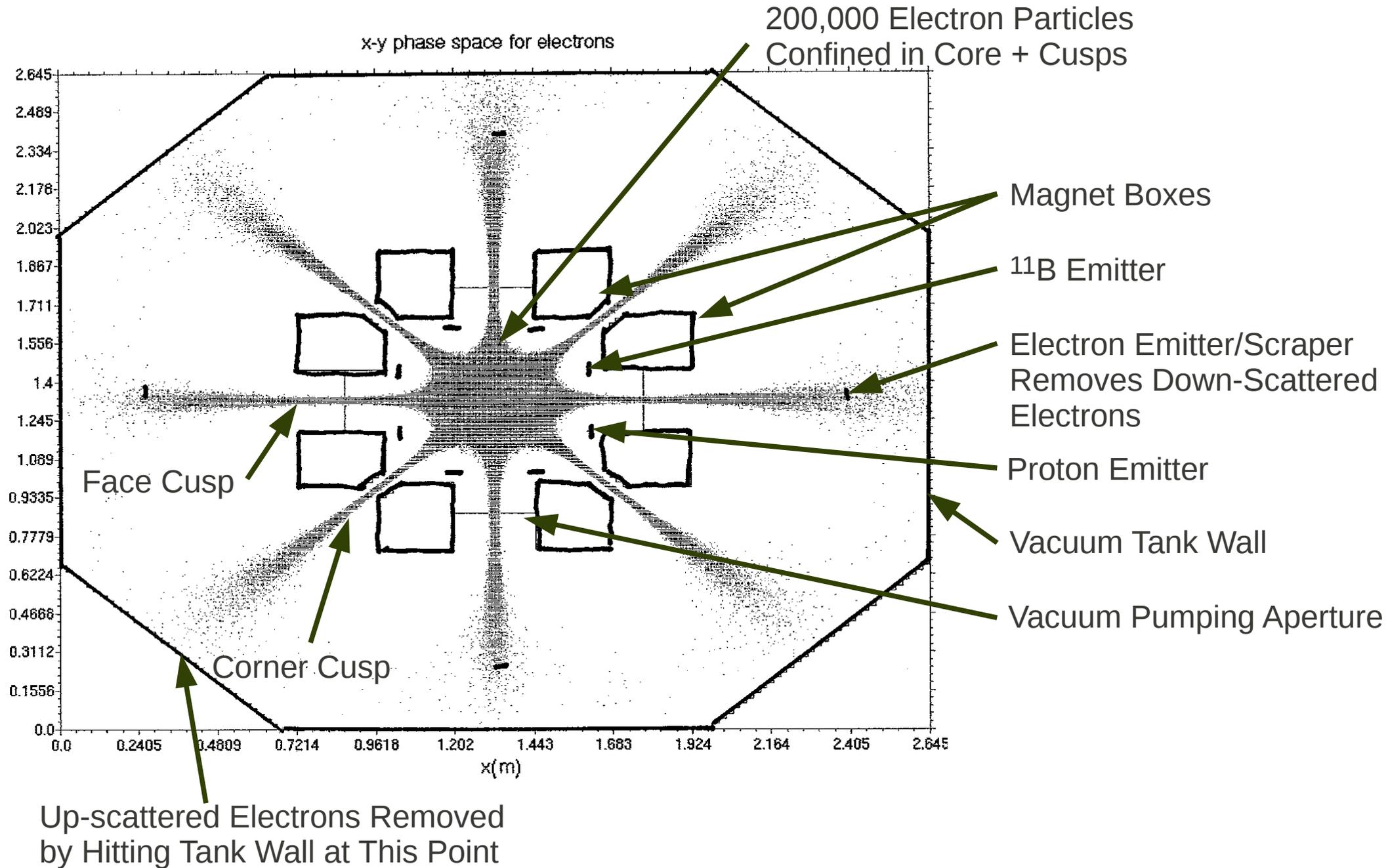


Fig. 5 - Confining Electrostatic Potential

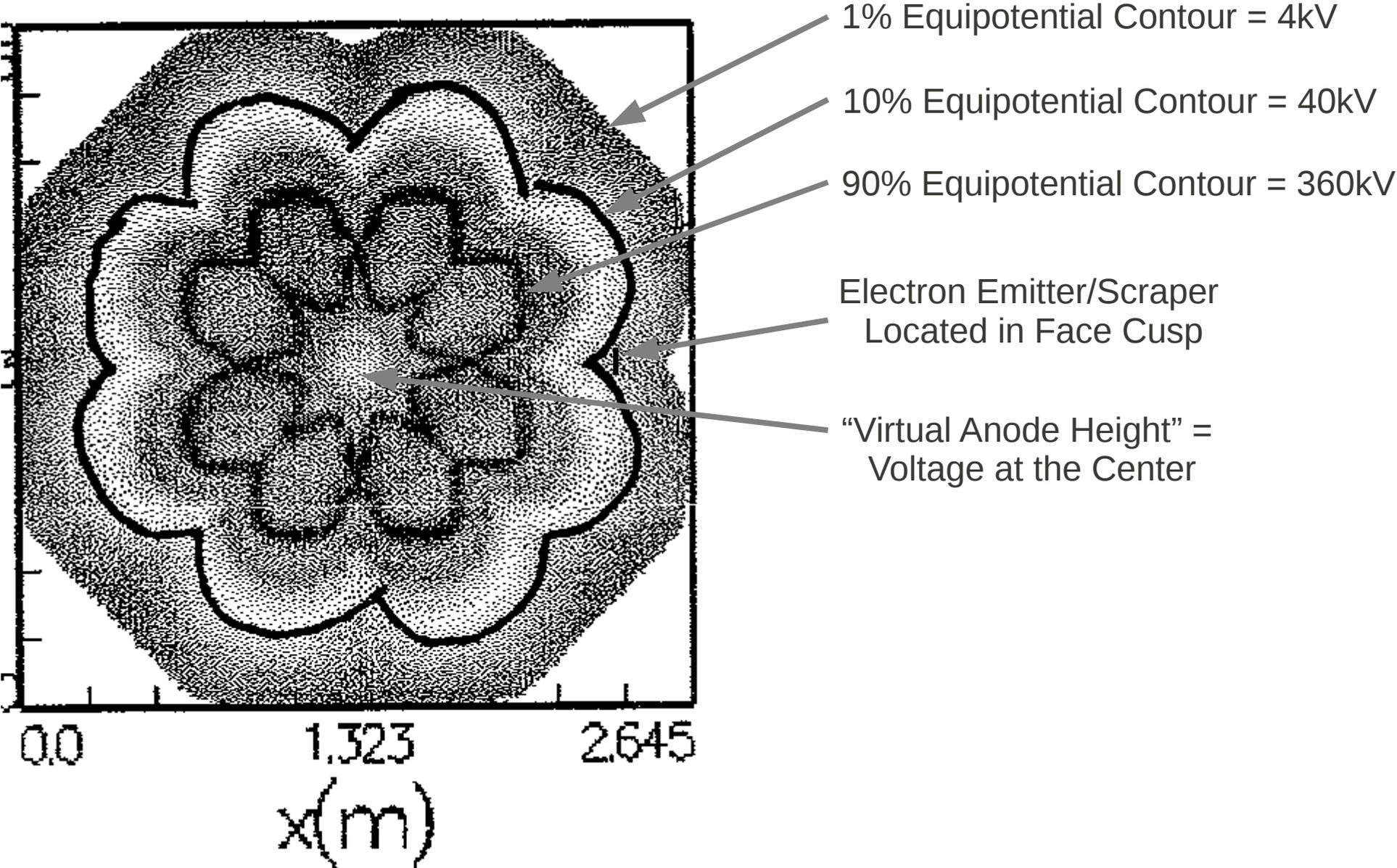
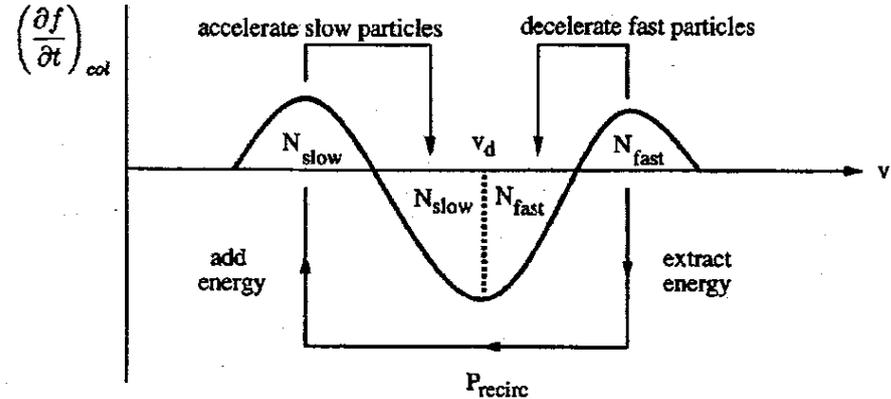


Fig 6 - Rider's 2005 Analysis of IEC

Required Power to Maintain Nonequilibrium Plasma

$$P_{\text{recirc}} \equiv \int_0^{\infty} (dv 4\pi v^2) \left(\frac{1}{2} m v^2 \right) \left(\frac{\partial f}{\partial t} \right)_{\text{col}} \Theta[J(v)], \quad (14)$$



Idealized System for Recirculating Power to Maintain a Nonequilibrium Plasma

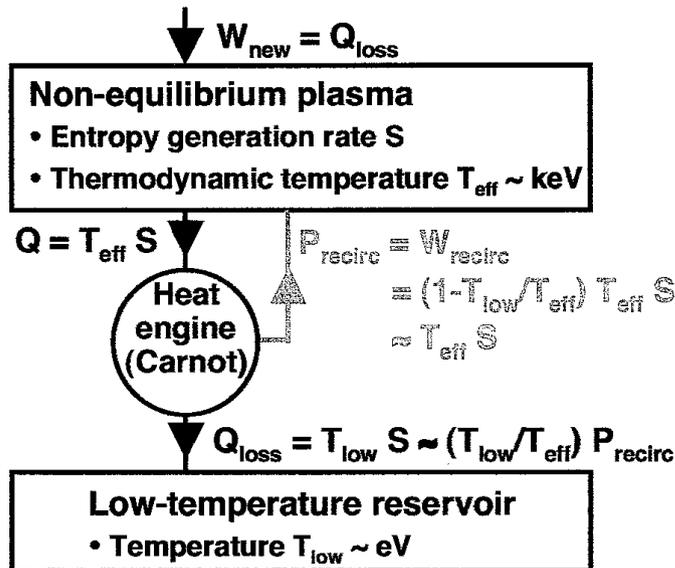


FIG. 2. A schematic diagram showing how to calculate the minimum recirculating power required to maintain a given non-Maxwellian isotropic velocity distribution shape. This particular example shows the recirculating power needed to sustain a distribution qualitatively similar to that in Fig. 1(b), but this general method may be extended to any isotropic but otherwise arbitrary velocity distribution, as described in Eq. (14).

- $P_{\text{recirc}}/P_{\text{fus}} \sim 5\text{-}50$ for most interesting cases
- Direct electric converters, resonant heating, etc. would lose too much power during recirculation
- Need novel approaches (e.g., nonlinear wave-particle interactions) that
 - Are >95% efficient
 - Recirculate the power *inside the plasma* without running $P_{\text{recirc}} \gg P_{\text{fus}}$ through external hardware
 - Are resistant to instabilities

T. H. Rider, *Phys. Plasmas* 4, 1039 (1997) and Ph.D. thesis, MIT (1995)—don't overlook Appendix E

THR-16
4/1/05

Fig. 7 - Scraping Down-Scattered e's

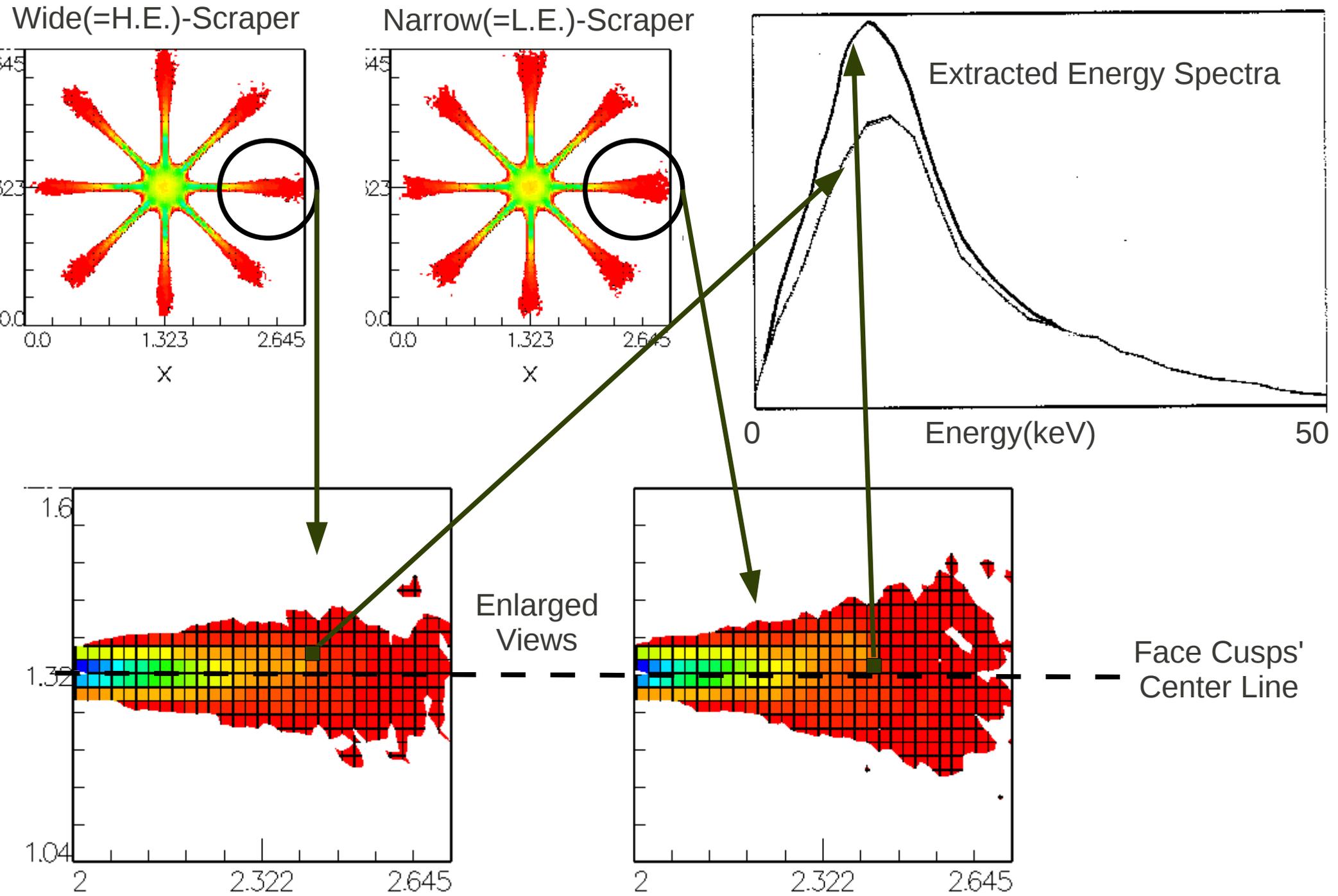


Fig. 8 - Ion Loss Power Calculation

- $P_{in} \equiv$ proton energy-loss-rate + boron energy-loss-rate (through corner cusps)

 $=$ (# slabs/cube) (# cusps/slab) $\{\Sigma[\text{Particle Loss-energy}][\text{Particle loss-rate}]\}$

 $= (L/\lambda_D) (4) \{[\frac{1}{2}(956\text{MeV})(8e6)^2/c^2][\frac{1}{2}(114-110)(9e10)/(11e-6s)]$

 $\quad + [\frac{1}{2}(11)(931\text{MeV})(5.4e6)^2/c^2][\frac{1}{2}(114-110)(1.2e10)/[(11e-6s)]}\}$

 $= (30)(4) \{[(340\text{keV})(1.6e16/s)] + [(1700\text{keV})(2.2e15/s)]\} = 6.5e23 + 4.5e23$
- $P_{in} = 1.1e24 \text{ eV/s}$

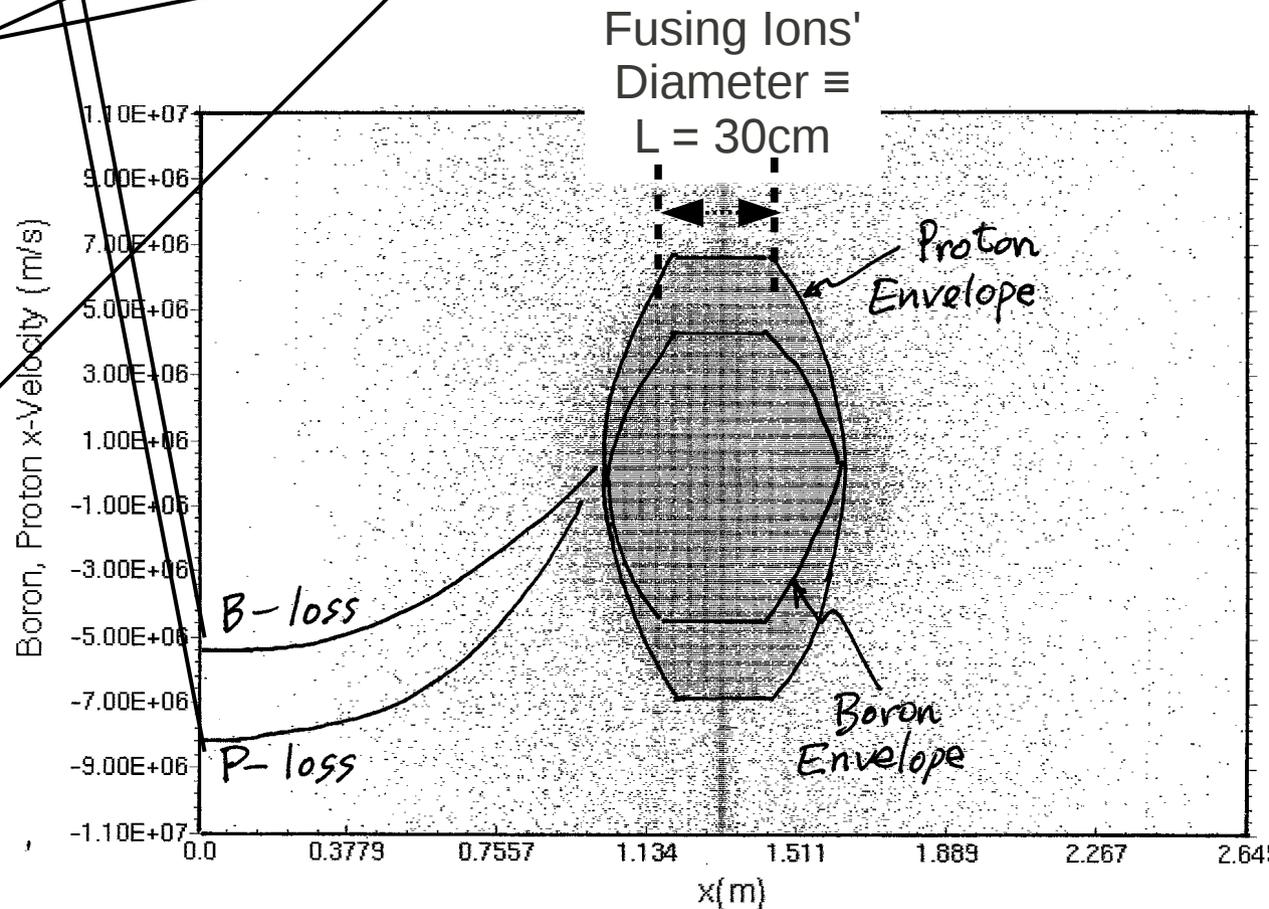
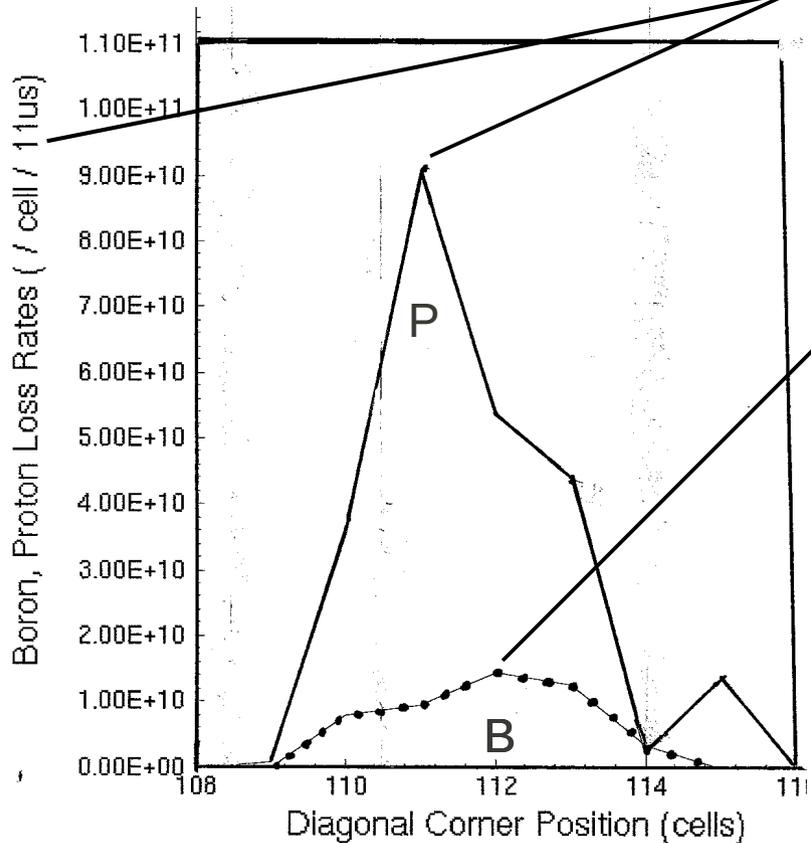


Fig. 9 - Power Balance Q

- Simulated (R = 35cm) power balance: $Q(R) \equiv P_{\text{fus}} / P_{\text{in}}$ where:
 - $P_{\text{fus}} = n_p n_b \langle \sigma_f v \rangle L^3 E_f \text{ eV/s}$ [6]
 - n_p = proton 3D density $\equiv N_p / \lambda_D = 1.1e17/m^3$
 - n_b = boron 3D density = n_p / Z (Proton and boron partial pressures are made equal.)
 - Z = boron charge state from ion gun = 5
 - N_p = simulated (2D) proton density = $1.1e15/m^2$ (Fig. 10)
 - λ_D = Debye length = $7.43e2 E_e^{1/2} n_e^{-1/2} \text{ cm} = 0.01\text{m}$ (Fig.10 & Formulary pg. 28 [7])
 - E_e = maximum electron energy inside well = 400keV (Fig. 10)
 - $n_e = 2n_p$ (Plasma quasi-neutrality is an inherent property of the simulation.)
 - $\langle \sigma \rangle$ = fusion x.c. times c.m. velocity = $8e-29\text{m}^2 \times 1e7\text{m/s} = 8e-22\text{m}^3/\text{s}$ (Title page)
 - L = ion plasma cube dimension in meters = 0.3m (from previous slide)
 - E_f = fusing ion pair energy release in eV = 8.7 MeV (Formulary pg. 44 [7])
 - $P_{\text{fus}} = (1.1e17) (2.2e16) (8e-22) (0.3^3) (8.7e6) \text{ eV/s} = 4.5e17 \text{ eV/s}$
- $Q(R=35\text{cm}) = P_{\text{fus}} / P_{\text{in}} = 4.5e17 / 1.1e24 = 4.1e-7$ (P_{in} from Fig. 8)

[6] Glasstone and Lovberg, "Controlled Thermonuclear Reactions", van Nostrand, 1960, eq. 2.10

[7] NRL PlasmaFormulary, http://wwwpppd.nrl.navy.mil/nrlformulary/NRL_FORMULARY_11.pdf

Fig. 10 - Diagnostics Determining P_{fus}

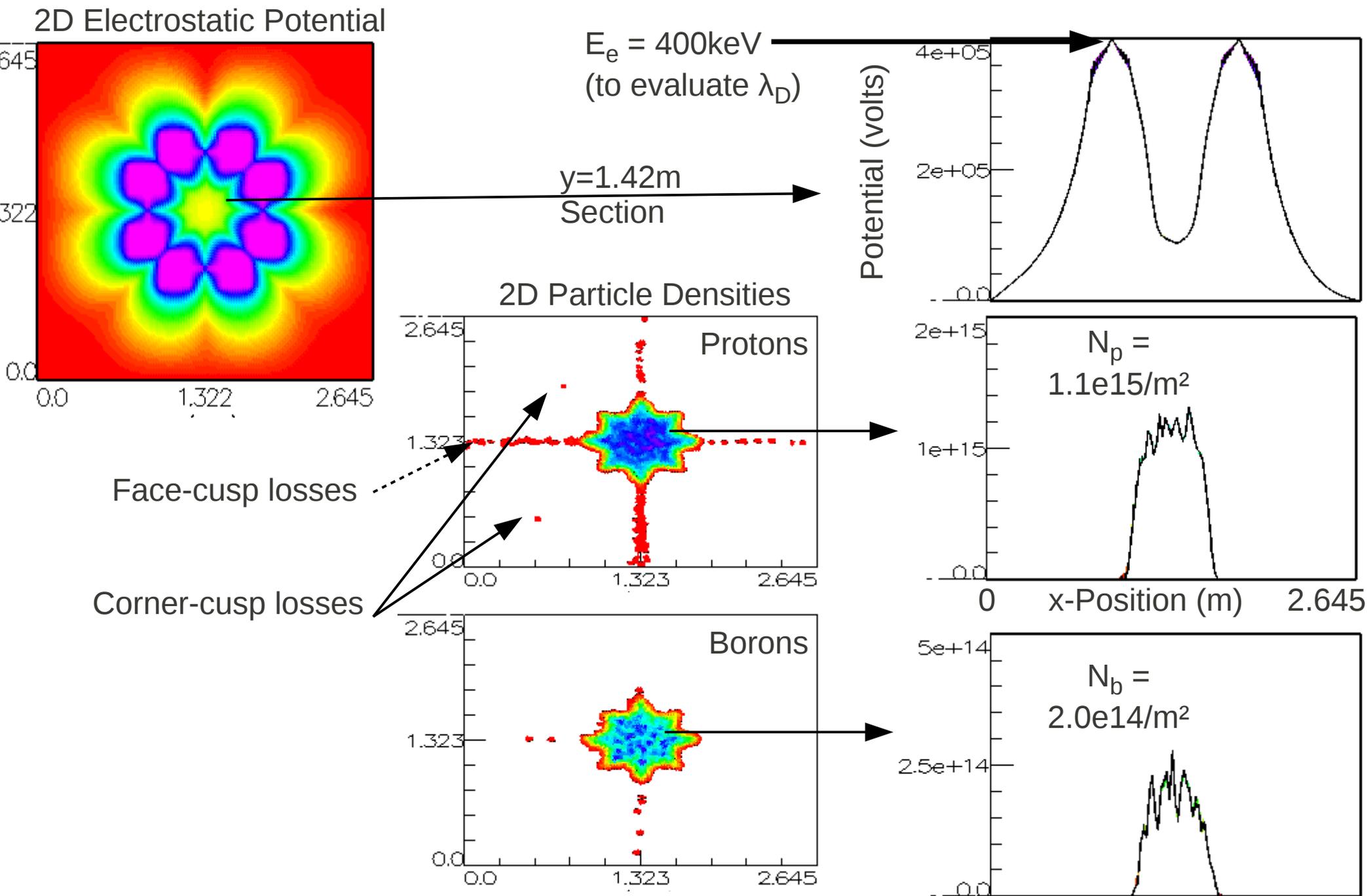


Fig. 11 - Reactor Break-Even Radius

- Bussard's Scaling Formula: $Q_1/Q_2 = (R_1/R_2)^5$ [8]
- Break-Even Formula: $Q(R=35\text{cm})/Q(R_b) = (R/R_b)^5$
 - $Q(R_b) \equiv 1$
- Solving for Break-Even Radius: $R_b = R/Q^{1/5}$
- $R_b = 0.35\text{m}/(4.1\text{e-}7)^{0.2} = 6.6\text{m} = \text{smaller than ITER}$

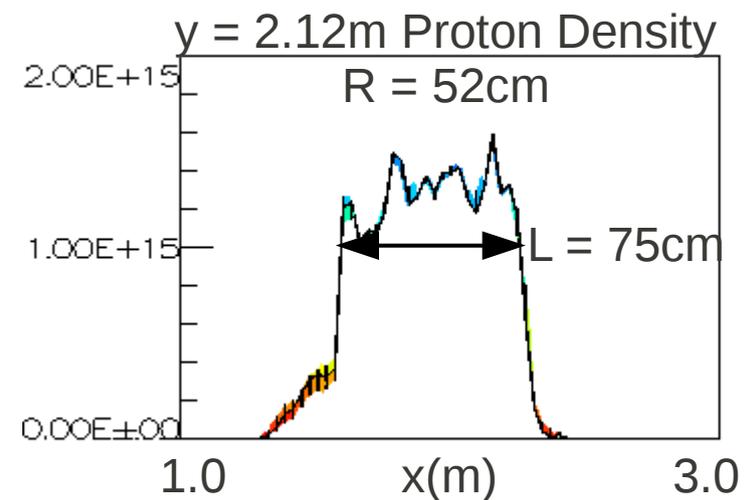
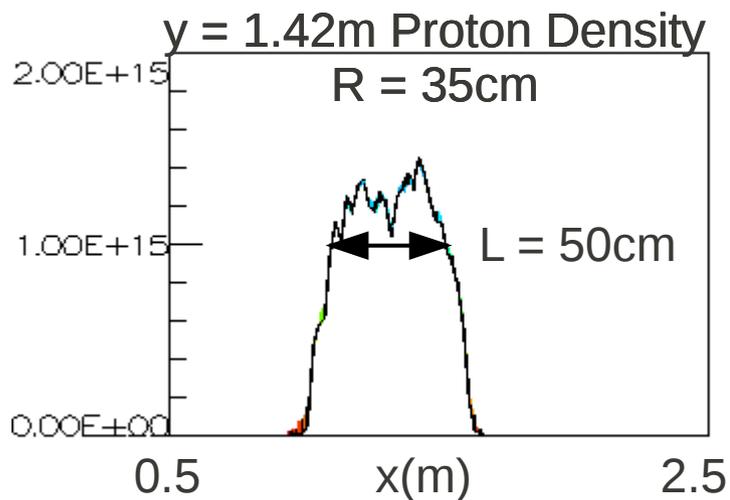


Fig. 12 - Bremsstrahlung Power Loss

- $P_b = 1.69e-32 n_e T_e^{1/2} [n_p + Z^2 n_b] L^3 \text{ W}$ [Formulary p.58]
- $P_b = 1.1e-13 n_e^2 T_e^{1/2} [0.5 + (25)(0.1)] L^3 \text{ eV/s}$
 - $n_e = \text{electron density in cm}^{-3} = 2.2e11/\text{cm}^3$ (Fig. 9)
 - $T_e = \text{electron kinetic energy in eV} = 80\text{keV}$ (Fig 13)
 - $L = \text{electron core edge dimension in cm} = 30\text{cm}$ (Fig. 13)
- $P_b = 1.1e-13 (2.2e11)^2 (8e4)^{1/2} [3.0] (30)^3 \text{ eV/s}$
- $P_b = 1.3e17 \text{ eV/s}$
- $P_b \approx 30\% P_{\text{fus}}$ (Fig. 9)
- **Bremsstrahlung losses $\approx 1/3$ fusion output power**

Fig. 14 - How to Reduce P_b Losses

- $P_b \sim T_e^{1/2} [1 + 25 (n_b/n_p)]$
- To reduce P_b the reactor design can change:
 - Reducing T_e to 1% E_e would reduce P_b by 4.5X. [4]
 - Boron fraction n_b/n_p 20 \rightarrow 10% would reduce P_b by $\sim 2X$.
- Reducing T_e might increase reactor size (R_b).
 - Not yet tested in simulation.
- **Radiation might be reduced to 5% of fusion power.**

Fig. 15 - p + ^{11}B Power; Conclusions

- New method efficiently recycles electron energy.
- Simulation predicts break-even $R_b = 6.6\text{m}$
- Additional design issues still need attention:
 - Electron power drain must be reduced.
 - Bremsstrahlung power drain must be reduced.
- A 3D simulation is needed for more realistic P_{in} .
- **The future of aneutronic fusion power is bright.**